Shape Measurement: An introduction to KSB

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DUEL Weak Lensing School
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at the end of the week you’ll be able to....

• Use SExtractor to detect astronomical sources in multi-colour data
• Make simulated astronomical images
• Separate stars from the galaxies and model the PSF
• Measure weak lensing shear using KSB
• Measure photometric redshifts
• Make a dark matter map
Practicalities

- 28 students, 14 computers: find a partner
  - Recommendation - choose someone you don’t know well
- Presentations
  - On Friday, 7 groups of 4 will give 10 minute summary presentations on different parts of the course (assigned randomly on Thurs afternoon)
• Recap: Weak lensing in practice, from galaxy to CCD pixel

• Shape measurement methods - and why we’ll be teaching you KSB

• Recap: KSB

• Introduction to Tuesdays practical - running KSB on simulated images
Recap on week 1

\[ A_{ij} = \frac{\delta \beta_i}{\delta \theta_j} \text{ true position} \]

\[ A = \begin{pmatrix} 1 - \kappa - \gamma_1 & -\gamma_2 \\ -\gamma_2 & 1 - \kappa + \gamma_1 \end{pmatrix}, \]

- The lensing Jacobian maps the source to the image plane.
- The effect depends on the lensing potential, through the shear and convergence terms.
- We want to measure the convergence (mass), but we can only observe the shear.
What happens to a circular source?

\[ I(\vec{\theta}) = I^{(s)} \left[ \vec{\beta}_0 + \mathcal{A}(\vec{\theta}_0) \cdot (\vec{\theta} - \vec{\theta}_0) \right] \]

The observed image = The true image distorted by A

\[ 1 - \kappa + |\gamma| \]

A circle becomes an ellipse.

The minor and major axes given by the inverse of the eigenvalues of A.

The orientation is given by the eigenvectors of A.
Centroids and Quadrupole Moments

- Lensing changes the shapes of galaxies, so we need a statistic with which to quantify their shape.

- The first moment determines an object's centroid

\[
\bar{x} = \int I(x, y) x \, dx \, dy
\]
\[
\bar{y} = \int I(x, y) y \, dx \, dy,
\]

- The second moment (or quadrupole moments determines shape)

\[
Q_{xx} = \int I(x, y) (x - \bar{x})^2 \, dx \, dy
\]
\[
Q_{xy} = \int I(x, y) (x - \bar{x})(y - \bar{y}) \, dx \, dy
\]
\[
Q_{yy} = \int I(x, y) (y - \bar{y})^2 \, dx \, dy.
\]
Quadrupoles, ellipticity and shear

\[ \epsilon \equiv \epsilon_1 + i\epsilon_2 = \frac{Q_{xx} - Q_{yy} + 2iQ_{xy}}{Q_{xx} + Q_{yy} + 2(Q_{xx}Q_{yy} - Q_{xy}^2)^{1/2}}, \]

\[ \epsilon_1 = \frac{a - b}{a + b} \cos(2\theta) \]
\[ \epsilon_2 = \frac{a - b}{a + b} \sin(2\theta). \]

\[ Q^{(s)} = \mathcal{A} Q \mathcal{A}^T \]

Lensing of an elliptical source

\[ \epsilon_{obs} = \frac{\epsilon^s + g}{1 + g^* \epsilon^s} \]
Observables : Galaxy Ellipticity

\[ e^{\text{obs}} = e^{\text{source}} + \gamma \]

\[ \langle e^{\text{source}} \rangle = 0 \]

\[ \gamma = < e^{\text{obs}} > \]

So it’s easy! Measure the ellipticity, you have the shear and all knowledge of cosmology?

Sadly not - instrumental, atmospheric and physical distortions are an order of magnitude larger than the weak lensing signal you want to detect.
Cosmic Lensing

\[ \begin{pmatrix} x_u \\ y_u \end{pmatrix} = \begin{pmatrix} 1 - g_1 & -g_2 \\ -g_2 & 1 + g_1 \end{pmatrix} \begin{pmatrix} x_l \\ y_l \end{pmatrix} \]

Real data:
\[ g_i \sim 0.03 \]
Atmospheric Seeing and telescope PSF

Real data: seeing disk \sim\ Galaxy size
Pixelisation

Sum light in each square

Real data: Pixel size $\sim$ seeing size /3
Noise

Mostly Poisson. Some Gaussian and bad pixels. Uncertainty on total light $\sim 5$ per cent
The Forward Process.

**Galaxies:** Intrinsic galaxy shapes to measured image:
- Intrinsic galaxy (shape unknown)
- Gravitational lensing causes a shear ($\text{shear}$)
- Atmosphere and telescope cause a convolution
- Detectors measure a pixelated image
- Image also contains noise

**Stars:** Point sources to star images:
- Intrinsic star (point source)
- Atmosphere and telescope cause a convolution
- Detectors measure a pixelated image
- Image also contains noise

**PSF**
Weak lensing analyses reverse this process.

The Inverse Problem:
Measured images to shear

Intrinsic galaxy shapes can be inferred, but are not used beyond shear estimation.
Steps to creating a shear catalogue

1. Reduce your data well
2. Detect objects
3. Separate stars from galaxies
4. Model the PSF with the stars
5. Remove the effect of the PSF
6. Measure the galaxy shape

Shape Measurement Methods only differ in parts 5 and 6
Classification of different methods

<table>
<thead>
<tr>
<th>PSF correction scheme</th>
<th>Shear measurement method</th>
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<tr>
<td></td>
<td>Passive</td>
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<tr>
<td>Subtraction</td>
<td>Measure a number</td>
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<td>KSB+ (various)</td>
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<td>Reglens (RM)</td>
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<td>RRG*</td>
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<td>Deconvolution</td>
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<td>BJ02 (MJ, MJ2)</td>
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<td>Shapelets (KK)</td>
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<td>BJ02 (RN)</td>
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<td>im2shape*</td>
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STEP started in 2005 to address the question of whether variations in the accuracy of different shear measurement pipelines could be responsible for the discrepancies found between different cosmic shear results.

Cosmological model: $\Lambda$CDM

- upper curve $\sigma_8 = 0.7$
- lower curve $\sigma_8 = 1.0$
STEP parameters: $m$ and $c$

$$(\gamma_{\text{measured}} - \gamma_{\text{true}}) = c + m\gamma_{\text{true}} + q\gamma_{\text{true}}^2$$

The best method has $m=0$ and $c=0$
The Kaiser Squires and Broadhurst method (KSB) is the most widely used method in current weak lensing analyses.

- It uses stars to model the atmosphere and telescope distortion and essentially subtracts it from the data.
- The end product is a shear estimate for each galaxy.
Shear bias as a function of galaxy magnitude and size

- These biases average out when the full sample is combined.

- This result, found in all but one of the tested methods, is a disaster for 3D weak lensing and any hope of measuring dark energy.
KSB (Kaiser, Squires and Broadhurst 1995)

**Reasons to use KSB**

1. It’s several orders of magnitude faster than all other methods
2. It’s accurate to the percent level on average
3. For large high signal-to-noise galaxies it’s very accurate

**Reasons to not use KSB**

1. It is unstable to small changes in the method
2. It has size and magnitude dependent biases
3. For small low signal-to-noise galaxies it’s very inaccurate

**Why are we teaching it to you?**

For a first pass analysis of the data KSB is excellent. Lensfit (see last lecture) is the only method suited to data that surpasses KSB, but it’s still evolving. The steps you’ll take in the KSB analysis are broadly common to all weak lensing methods.
Observables: Galaxy Ellipticity

\[ e^{\text{obs}} = e^{\text{source}} + \gamma \]

\[ \langle e^{\text{source}} \rangle = 0 \]

\[ \gamma = \langle e^{\text{obs}} \rangle \]
Ellipticity and Quadrupole Moments

Objects are parameterised according to their weighted quadrupole moments

\[ Q_{ij} = \frac{\int d^2 \theta \, W(\theta) \, I(\theta) \, \theta_i \theta_j}{\int d^2 \theta \, W(\theta) \, I(\theta)} , \]

where \( I \) is the surface brightness of the object, \( \theta \) is the angular distance from the object centre and \( W \) is a Gaussian weight function of scale length \( r_g \), where \( r_g \) is some measurement of galaxy size.
Quadrupoles, ellipticity and shear

\[ \epsilon \equiv \epsilon_1 + i\epsilon_2 = \frac{Q_{xx} - Q_{yy} + 2iQ_{xy}}{Q_{xx} + Q_{yy} + 2(Q_{xx}Q_{yy} - Q_{xy}^2)^{1/2}}, \]

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\[ Q^{(s)} = \mathcal{A} Q \mathcal{A}^T \]

\[ \epsilon_{ob} = \frac{\epsilon^s + g}{1 + g^* \epsilon^s} \]

Lensing of an elliptical source
• If you do not include a weight, or make the size of the weight function too big, noise will bias your quadrupole moment.

• However including this weight means the simple relationship between shear and ellipticity no longer applies.

• KSB calculate how a weighted ellipticity measure is related to the shear and use the same formalism to remove the effects of the PSF.
Kaiser et al. (1995) show that if the PSF distortion can be described as a small but highly anisotropic distortion convolved with a large circularly symmetric seeing disk, then the ellipticity of a PSF corrected galaxy is given by

$$\varepsilon_{\alpha}^{\text{cor}} = \varepsilon_{\alpha}^{\text{obs}} - P_{\alpha \beta}^{\text{sm}} \rho_{\beta}$$

As the corrected stellar ellipticity must be zero

$$p_{\mu} = (P_{\text{sm}^*})_{\mu \alpha}^{-1} \varepsilon_{\alpha}^{* \text{obs}}.$$
The atmosphere causes circular smearing.

Differences in the optical light path cause shearing.

In principle the distortions introduced by the telescope and detector can be predicted.

In practice many other factors affect the PSF including the angle observed on the sky, the temperature, the filter etc.

We therefore have to be able to model the PSF directly from the data using stars.
Example PSFs: CFHT Megacam

- The PSF varies across the image
- The PSF is not Gaussian
- The ellipticity of the PSF varies at different isophotes
- The centroid of the PSF shifts for different isophotes
- The worst PSFs are at the edges of the chip

A CFHT MegaCam image
Example PSFs: ACS on the Hubble Space Telescope

- In space the diffraction spikes become stronger
- You can see the airy pattern
- The ellipticity of the PSF again changes at different isophotal levels
- Here you can also see the effect of different filters
How good is the KSB PSF assumption?

Terrible! But amazingly KSB works incredibly well

ACS PSF
Example measurements of $p$

- This example is taken from the ACS on Hubble.
- $p$ changes as a function of:
  - Position on the chip
  - Filter
  - Time
  - The weight size $W(rg)$
- Fit a polynomial to measurements of $p$ to model variations across the field of view
- These models are time and weight size dependent
Removing the smearing effect of the atmosphere

The isotropic effect of the atmosphere and weight function can be accounted for by applying the pre-seeing shear polarisability tensor correction $P^\gamma$, as proposed by Luppino & Kaiser (1997), such that

$$\varepsilon^\text{cor}_\alpha = \varepsilon^s_\alpha + P^\gamma_{\alpha\beta} \gamma_\beta,$$

Putting it all together:

$$\hat{\gamma}_\alpha = (P^\gamma)^{-1}_{\alpha\beta} \left[ \varepsilon^\text{obs}_\beta - P^\text{sm}_{\beta\mu} p_\mu \right].$$

Note these mysterious tensors are weighted higher order moments of the galaxies light distribution. See Kaiser et al 1995 for details.
Problems with KSB

- $P^\gamma$ should be calculated on the PSF corrected image we don’t have
- The underlying PSF assumption is poor
- $P^{sm}, P^{sh}$ are noisy quantities measured from data so people sometimes approximate
  \[
  (P^{sm})^{-1} = 1/(2 \, Tr(P^{sm})
  \]
- Which weight function to use where? $P^{sm*}, P^{sh*}$ should really be evaluated with the same weight function as the galaxy.
- KSB assumes the centroids are known
- All of these choices lead to huge variations in the performance of KSB as demonstrated by STEP! If you get it right KSB can be accurate to 1%.
1. Use Stuff and SkyMaker to create a simulated image
2. Detect objects in the data (using SExtractor)
3. Separate stars and galaxies
4. Model the PSF using the stars
5. Remove the effects of the PSF on the galaxy image (using KSB)
6. Measure the shear from the PSF corrected image

Analysing real astronomical data with KSBf90:

The IAP DUEL weak lensing summer school 2009 will be hosting a KSBf90 practical session. What follows are the instructions for the students who will be analysing a section of the CFHTLS D1 field.

The weak lensing analysis consists of six steps

1) Install KSBf90 for astronomers
2) Create SExtractor catalogue (see Thomas Erbens catalogue practical)
3) Separate the stars from the galaxies
4) Measure and model the PSF
5) Measure and correct the galaxy shapes
6) Select galaxies for shear measurement
7) Create a mass map

Note for any of the code, you can always use the option ‘-h’ to see what command line input is expected.
1. Separating galaxies and stars

- Stars have a range of magnitudes, but have a constant size given by the width of the PSF.
- You can select stars from their position in a size/magnitude plot.
- We will use ‘Findstars.a’ in the practical to select stars.
Selecting objects based on their half light radius

Type ‘l’ to zoom in
Type ‘s’ to select stellar branch
Double check with the full width half maximum

Checking two size estimates provides a more reliable result

Type ‘n’ to look at the second size estimate
Type ‘s’ to select stellar branch again

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Lecture 1: Shape Measurement: KSB
Findstars.a options

- Use ‘l’ to zoom in to get a clearer view of the stellar branch
- Use ‘s’ to select branch (tip start with the top right corner)
- Use ‘n’ to move on to the next size test and repeat
- Use ‘x’ to save selection and exit
Selecting stars

- The stellar sample does not need to be 100% complete!
- But it needs to be uncontaminated by galaxies or saturated stars
- It needs to be a representative sample of the PSF - it might be necessary to select your stars chip by chip in the CCD.

One chip in the CCD could be misaligned and out of focus producing a second stellar locii.
• Once you’ve selected the stars, the galaxy selection is easy

• Pick only those objects that are larger than the PSF and fainter than the saturation limit

• Anything else will have had all its weak lensing shear information erased
- There are c-shell scripts to run all of the code.
• KSB uses weighted quadrupole moments to calculate shear estimators for each galaxy.

• As an input it needs a stellar catalogue and a galaxy catalogue.

• Findstars.a lets you select stars

• Choose your parameters in KSBf90.param to select how to model the resulting PSF

• Once happy with the PSF model measure the galaxy shapes with rungals.scr

• Finally see how your choices impact on the final shear measurement with gal_select

• The challenge can you measure the shears that you put in?
at the end of the week you’ll be able to:

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