THE PROPERTIES OF THE STAR-FORMING INTERSTELLAR MEDIUM AT z=0.8–2.2 FROM HiZELS: STAR FORMATION AND CLUMP SCALING LAWS IN GAS-RICH, TURBULENT DISKS

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**Received 2012 April 24; accepted 2012 October 19; published 2012 November 16

ABSTRACT

We present adaptive optics assisted integral field spectroscopy of nine H α -selected galaxies at z=0.84-2.23 drawn from the HiZELS narrowband survey. Our observations map the kinematics of these star-forming galaxies on \sim kpc scales. We demonstrate that within the interstellar medium of these galaxies, the velocity dispersion of the star-forming gas (σ) follows a scaling relation $\sigma \propto \Sigma_{\rm SFR}^{1/n}$ + constant (where $\Sigma_{\rm SFR}$ is the star formation surface density and the constant includes the stellar surface density). Assuming the disks are marginally stable (Toomre Q=1), this follows from the Kennicutt–Schmidt relation ($\Sigma_{\rm SFR}=A\Sigma_{\rm gas}^n$), and we derive best-fit parameters of $n=1.34\pm0.15$ and $A=3.4^{+2.5}_{-1.6}\times10^{-4}~M_{\odot}~{\rm yr}^{-1}~{\rm kpc}^{-2}$, consistent with the local relation, and implying cold molecular gas masses of $M_{\rm gas}=10^{9-10}~M_{\odot}$ and molecular gas fractions of $M_{\rm gas}/(M_{\rm gas}+M_{\star})=0.3\pm0.1$, with a range of 10%-75%. We also identify $11\sim$ kpc-scale star-forming regions (clumps) within our sample and show that their sizes are comparable to the wavelength of the fastest growing mode. The luminosities and velocity dispersions of these clumps follow the same scaling relations as local H II regions, although their star formation densities are a factor \sim 15 \pm 5 \times higher than typically found locally. We discuss how the clump properties are related to the disk, and show that their high masses and luminosities are a consequence of the high disk surface density.

Key words: galaxies: evolution – galaxies: high-redshift – galaxies: starburst

Online-only material: color figure

1. INTRODUCTION

The majority of the stars in the most massive galaxies ($M_{\star} \gtrsim$ $10^{11} M_{\odot}$) formed around 8–10 billion years ago, an epoch when star formation was at its peak (Hopkins & Beacom 2006; Sobral et al. 2012b). Galaxies at this epoch appear to be gas-rich ($f_{gas} =$ 20–80%; Tacconi et al. 2010; Daddi et al. 2010; Geach et al. 2011) and turbulent (Lehnert et al. 2009), with high velocity dispersions given their rotational velocities ($\sigma = 30-100 \,\mathrm{km \, s^{-1}}$, $v_{\rm max}/\sigma \sim 0.2$ –1; e.g., Förster Schreiber et al. 2009; Genzel et al. 2008; Wisnioski et al. 2011; Bothwell et al. 2012). Within the dense and highly pressurized interstellar medium (ISM) of these high-redshift galaxies, it has been suggested that star formation may be triggered by fragmentation of dynamically unstable gas (in contrast to star formation occurring in giant molecular clouds (GMCs) in the Milky Way, which continually condense from a stable disk and then dissipate). This process may lead to the formation of massive ($\sim 10^{8-9} M_{\odot}$) star-forming regions (e.g., Elmegreen et al. 2007; Bournaud & Elmegreen 2009) and give rise to the clumpy morphologies that are often seen in highredshift starbursts (Elmegreen et al. 2009).

In order to explain the ubiquity of "clumpy" disks seen in images of high-redshift galaxies, numerical simulations have also suggested that most massive, star-forming galaxies at z=1-3 continually accrete gas from the intergalactic medium along cold and clumpy streams from the cosmic web (Kereš et al. 2005; Dekel et al. 2009; Bournaud & Elmegreen 2009; van de Voort et al. 2011). This mode of accretion is at its most efficient at $z \sim 1-2$ and offers a natural route for maintaining the high gas surface densities, star formation rates, and clumpy morphologies of galaxies at these epochs. In such models, the gas disks

fragment into a few bound clumps which are a factor $10-100 \times$ more massive than star-forming complexes in local galaxies. The gravitational release of energy as the most massive clumps form, torques between in-spiraling clumps, and energy injection from star formation are all likely to contribute to maintaining the high turbulence velocity dispersion of the interstellar medium (ISM; e.g., Bournaud & Elmegreen 2009; Lehnert et al. 2009; Genzel et al. 2008, 2011).

In order to refine or refute these models, the observational challenge is now to quantitatively measure the internal properties of high-redshift galaxies, such as their cold molecular gas mass and surface density, disk scaling relations, chemical make up, and distribution and intensity of star formation. Indeed, constraining the evolution of the star formation and gas scaling relations with redshift, stellar mass and/or gas fraction are required in order to understand star formation throughout the Universe. In particular, such observations are vital to determine if the prescriptions for star formation which have been developed at z=0 can be applied to the rapidly evolving ISM of gas-rich, high-redshift galaxies (Krumholz & Dekel 2010; Hopkins 2012).

To gain a census of the dominant route by which galaxies assemble the bulk of their stellar mass within a well-selected sample of high-redshift galaxies, we have conducted a wide-field (several degree scale) near-infrared narrowband survey (the High-Z Emission Line Survey, HiZELS) which targets H α emitting galaxies in four precise ($\Delta z = 0.03$) redshift slices: z = 0.40, 0.84, 1.47, and 2.23 (Geach et al. 2008; Sobral et al. 2009, 2010, 2011, 2012a, 2012b). This survey provides a large, star-formation-limited sample of identically selected H α emitters with properties "typical" of galaxies which will

likely evolve into $\sim L_{\star}$ galaxies by z=0, but seen at a time when they are assembling the bulk of their stellar mass, and thus at a critical stage in their evolutionary history. Moreover, since HiZELS was carried out in the best-studied extragalactic survey fields, there is a wealth of multi-wavelength data, including 16–36 medium and broadband photometry (from restframe UV—mid-infrared wavelengths allowing robust stellar masses to be derived), Herschel 250–500 μ m imaging (allowing bolometric luminosities and star formation rates to be derived), as well as high-resolution morphologies for a subset from the Hubble Space Telescope CANDELS and COSMOS ACS surveys.

In this paper, we present adaptive optics (AO) assisted integral field spectroscopy of nine star-forming galaxies selected from HiZELS. The galaxies studied here have $H\alpha$ -derived star formation rates of 1–27 M_{\odot} yr $^{-1}$ and will likely evolve into $\sim L^{\star}$ galaxies by z=0. They are therefore representative of the high-redshift star-forming population. We use the data to explore the scaling relations between the star formation distribution intensity and gas dynamics within the ISM, as well as the properties of the largest star-forming regions. We adopt a cosmology with $\Omega_{\Lambda}=0.73$, $\Omega_{m}=0.27$, and $H_{0}=72\,\mathrm{km\,s^{-1}\,Mpc^{-1}}$ in which 0'.12 corresponds to a physical scale of 0.8 kpc at z=1.47, the median redshift of our survey. All quoted magnitudes are on the AB system. For all of the star formation rates and stellar mass estimates, we use a Chabrier (2003) initial mass function (IMF).

2. OBSERVATIONS

Details of the target selection, observations, and data reduction are given in Swinbank et al. (2012). Briefly, we selected nine galaxies from HiZELS with H α fluxes 0.7–1.6 × 10^{-16} erg s⁻¹ cm⁻² (star formation rates⁶ of SFR_{H α} = 1–27 M_{\odot} yr⁻¹) that lie within 30" of bright (R < 15) stars. We performed natural guide star AO observations with the SINFONI IFU between 2009 September and 2011 April in ~0".6 seeing and photometric conditions with exposure times between 3.6 and 13.4 ks. At the three redshift slices of our targets, z = 0.84[2], z = 1.47[6], and z = 2.23[1], the H α emission line is redshifted to ~1.21, 1.61, and 2.12 μ m (i.e., into the J, H, and K bands, respectively). The median strehl achieved for our observations is 20% and the median encircled energy within 0".1 (the approximate spatial resolution of our observations) is 25%

The data were reduced using the SINFONI esorex data reduction pipeline which extracts, flat-fields, wavelength calibrates, and forms the data cube for each exposure. The final (stacked) data cube for each galaxy was generated by aligning the individual data cubes and then combining them using an average with a 3σ clip to reject cosmic rays. For flux calibration, standard stars were observed each night either immediately before or after the science exposures and were reduced in an identical manner to the science observations.

As Figure 1 shows, all nine galaxies in our SINFONI-HiZELS survey (SHiZELS) display strong H α emission, with luminosities of $L_{\rm H}\alpha \sim 10^{41.4-42.4}$ erg s⁻¹. Fitting the H α and [N II] $\lambda\lambda$ 6548, 6583 emission lines pixel-by-pixel using a χ^2 minimization procedure, we construct intensity, velocity, and velocity dispersion maps of our sample and show these in Figure 1 (see also Swinbank et al. 2012 for details).

Adopting SFR_{H\alpha} = $4.6 \times 10^{-42} L(\text{H}\alpha) \text{ (erg s}^{-1}).$

3. ANALYSIS AND DISCUSSION

3.1. Galaxy Dynamics and Star Formation

As Swinbank et al. (2012) demonstrate, the ratio of dynamical-to-dispersion support for this sample is $v \sin(i)/\sigma = 0.3-3$, with a median of 1.1 ± 0.3 , which is consistent with similar measurements for both AO and non-AO studies of star-forming galaxies at this epoch (e.g., Förster Schreiber et al. 2009). The velocity fields and low kinemetry values of the SHiZELS galaxies (total velocity asymmetry, $K_{\text{tot}} = 0.2-0.5$) also suggest that at least six galaxies (SHiZELS 1, 7, 8, 9, 10, & 11) have dynamics consistent with large, rotating disks, although all display small-scale deviations from the best-fit dynamical model, with $\langle \text{data} - \text{model} \rangle = 30 \pm 10 \text{ km s}^{-1}$, with a range from $\langle \text{data} - \text{model} \rangle = 15-70 \text{ km s}^{-1}$ (Swinbank et al. 2012).

We also use the multi-wavelength imaging to calculate the rest-frame spectral energy distributions (SEDs) of the galaxies in our sample and to derive the stellar mass, reddening, and estimates of the star formation history (Sobral et al. 2011). From the broadband SEDs (Figure 1 of Swinbank et al. 2012), the average E(B-V) for our sample is $E(B-V)=0.28\pm0.10$, which corresponds to $A_v=1.11\pm0.27$ mag and indicates $A_{\rm H\alpha}=0.91\pm0.21$ mag. The resulting dust-corrected H α star formation rate for the sample is SFR_{H $\alpha}=16\pm5\,M_{\odot}$ yr⁻¹, which is consistent with that inferred from the far-infrared SEDs using stacked *Herschel* SPIRE observations (SFR_{FIR}=18 ± 8 M_{\odot} yr⁻¹; Swinbank et al. 2012).}

Next, to investigate the star formation occurring within the ISM of each galaxy, we measure the star formation surface density and velocity dispersion of each pixel in the maps. Since we do not have spatially resolved reddening maps, for each galaxy we simply correct the star formation rate in each pixel using the best-fit E(B-V) for that system. We also remove the rotational contribution to the line width at each pixel by calculating the local $\Delta V/\Delta R$ across the point-spread function (PSF) for each pixel (Davies et al. 2011). In Figure 2, we plot the resulting line-of-sight velocity dispersion (σ) as a function of star formation surface density (Σ_{SFR}) for each galaxy in our sample. We see that there appears to be a correlation between $\Sigma_{\rm SFR}$ and σ , and as Krumholz & Dekel (2010) show, this powerlaw correlation may be a natural consequence of the gas and star formation surface density scaling laws. For example, first consider the Toomre stability criterion, Q, (Toomre 1964).

$$Q = \frac{\sigma \kappa}{\pi G \Sigma_{\text{disk}}},\tag{1}$$

where σ denotes the line-of-sight velocity dispersion, $\Sigma_{\rm disk}$ is the average surface density of the disk, and $\kappa=a~v_{\rm max}/R$, where $v_{\rm max}$ is the rotational velocity of the disk, R is the disk radius, and $a=\sqrt{2}$ for a flat rotation curve. Galaxies whose disks have Q<1 are unstable to local gravitational collapse and will fragment into clumps, whereas those with $Q\gtrsim 1$ have sufficient rotational support for the gas to withstand and collapse. As Hopkins (2012; e.g., see also Cacciato et al. 2012) point out, gas-rich galaxies are usually driven to $Q\sim 1$ since regions with Q<1 begin forming stars, leading to superlinear feedback which eventually arrests further collapse due to energy/momentum injection (recovering $Q\sim 1$). For galaxies with $Q\gg 1$, there is no collapse, no dense regions form, and

⁷ Adopting SFR_{FIR} = $2.7 \times 10^{-44} L_{FIR}$ (erg s⁻¹).

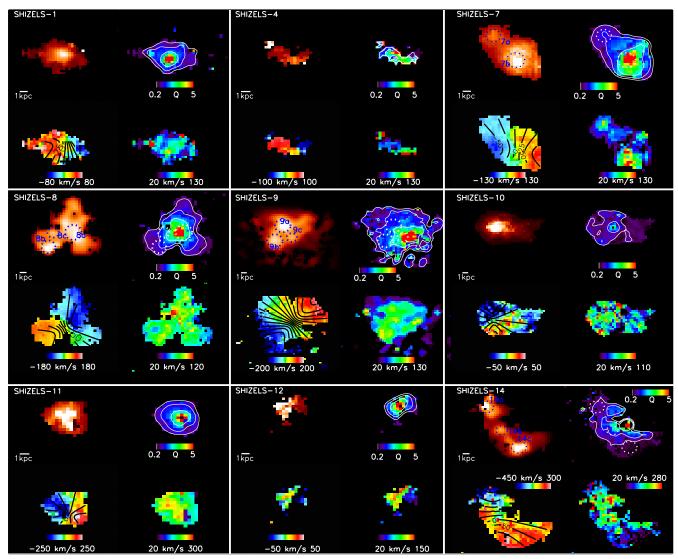


Figure 1. Hα intensity, velocity field, line-of-sight velocity dispersion (σ), and Toomre (Q) maps of the nine SHiZELS galaxies in our sample. Top left: Hα emission line map. In SHiZELS 7, 8, 9, and 14 we identify and label the star-forming regions (clumps). Top right: Toomre Q(x,y) maps of each galaxy, with contours at Q = 0.5, 1.0, and 2.0. In galaxies where we have identified star-forming regions (clumps), we also overlay their positions. These star-forming regions have an average Toomre $Q = 0.8 \pm 0.4$. Bottom left: Hα velocity field of each galaxy (with the best-fit kinematic model overlaid as contours). Bottom right: line-of-sight velocity dispersion (σ), corrected for local velocity gradient ($\Delta V/\Delta R$) across the PSF. At least six galaxies (SHiZELS 1, 7, 8, 9, 10, and 11) have dynamics that indicate that the ionized gas is in a large, rotating disk. A further two are compact (SHiZELS 4 and 12), while the dynamics of SHiZELS 14 indicate a merger. (A color version of this figure is available in the online journal.)

hence no star formation occurs (and so such galaxies would not be selected as star-forming systems).

Following Rafikov (2001), and focusing on the largest unstable fluctuations, the appropriate combination of gas and stellar surface density ($\Sigma_{\rm gas}$ and Σ_{\star} respectively) is

$$\Sigma_{\text{disk}} = \Sigma_{\text{gas}} + \left(\frac{2}{1 + f_{\sigma}^2}\right) \Sigma_{\star},\tag{2}$$

where $f_{\sigma} = \sigma_{\star}/\sigma_{g}$ is the ratio of the velocity dispersion of the stellar component to that of the gas (see also the discussion in Romeo & Wiegert 2011).

Next, Kennicutt (1998b) shows that the gas and star formation surface densities follow a scaling relation

$$\left(\frac{\Sigma_{\rm SFR}}{M_{\odot}\,{\rm yr}^{-1}\,{\rm kpc}^{-2}}\right) = A\left(\frac{\Sigma_{\rm gas}}{M_{\odot}\,{\rm pc}^{-2}}\right)^{n}.\tag{3}$$

For local, star-forming galaxies, the exponent, $n \sim 1.5$, and the absolute star formation efficiency, $A = 1.5 \pm 0.4 \times 10^{-4}$ (Kennicutt 1998a), imply an efficiency for star formation per unit mass of ~ 0.04 which holds across at least four orders of magnitude in gas surface density.

Combining these relations, the velocity dispersion, σ , should therefore scale as

$$\frac{\sigma}{\text{km s}^{-1}} = \frac{\pi \times 10^6 \, GR}{\sqrt{2} \, v_{\text{max}}} \left(\left(\frac{\Sigma_{\text{SFR}}}{A} \right)^{1/n} + \left(\frac{2}{1 + f_{\sigma^2}} \right) \frac{\Sigma_{\star}}{10^6} \right), \tag{4}$$

where $\Sigma_{\rm SFR}$ and Σ_{\star} are measured in M_{\odot} yr⁻¹ and M_{\odot} kpc⁻², respectively, R is in kpc, $v_{\rm max}$ in km s⁻¹, and $G=4.302\times 10^{-6}$ kpc M_{\odot}^{-1} (km s⁻¹)². With a power-law index of n=1.4, and a marginally stable disk (Q=1), for each galaxy we therefore expect a power-law relation of $\sigma \propto \Sigma_{\rm SFR}^{0.7}$ + constant (Krumholz et al. 2012).

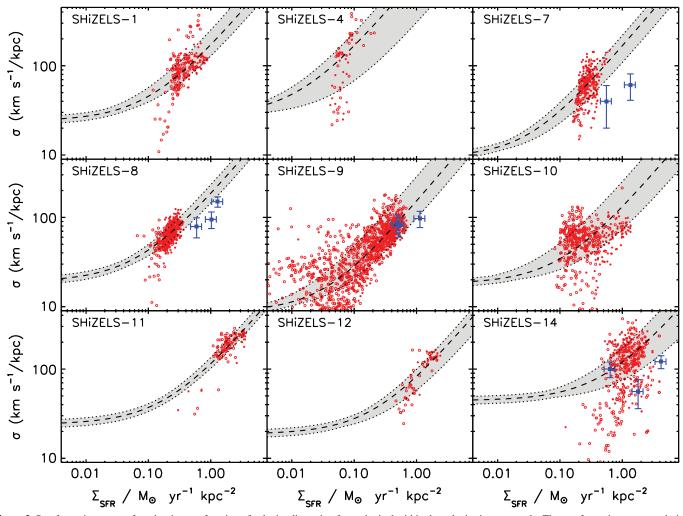


Figure 2. Star formation rate surface density as a function of velocity dispersion for each pixel within the galaxies in our sample. The star formation rates are derived from Hα, corrected for galaxy reddening, and the velocity dispersion has been corrected for a local velocity gradient (Section 3.1). The small solid and open symbols denote measurements within and outside the half-light radius, respectively. The solid squares show the star formation and velocity dispersions of the ~kpc-scale clumps (Table 2) which appear as regions of high star formation density given their velocity dispersion. The gray region denotes the best fit to the Σ_{SFR} – σ relation from combining the Toomre criterion and Kennicutt–Schmidt law (see Equation (4)) with power-law index ranging from n = 1.0 to 1.4 (the dashed curve shows the solution for n = 1.2). Over this range, the data are consistent with an absolute star formation efficiency of $A = 4.1 \pm 2.4 \times 10^{-4} M_{\odot} \text{ yr}^{-1} \text{ kpc}^{-2}$. (A color version of this figure is available in the online journal.)

In order to test whether this model provides an adequate description of our data, we fit the $\Sigma_{\rm SFR}-\sigma$ distribution for each galaxy in our sample. To estimate the stellar surface density, Σ_{\star} , we follow Sobral et al. (2011) and perform a full SED χ^2 fit of the rest-frame UV–mid-infrared photometry using the Bruzual & Charlot (2003) population synthesis models. We use photometry from up to 36 (COSMOS) and 16 (UDS) wide, medium, and narrowbands (spanning *GALEX* far-UV and near-UV bands to *Spitzer/IRAC*) and calculate the rest-frame SED, reddening, star formation history and stellar mass (Sobral et al. 2010). The stellar masses of these galaxies range from $10^{9.7-11.0} M_{\odot}$ (Table 1; see also Swinbank et al. 2012).

Since the stellar masses are calculated from 2" aperture photometry (and are then corrected to total magnitudes using aperture corrections; Sobral et al. 2010) to estimate the stellar surface density in the same area as our IFU observations, we assume that stellar light follows an exponential profile with Sersic index, $n_{\text{serc}} = 1-2$, and calculate the fraction of the total stellar mass within the disk radius, R (which we define as two times the H α half-light radius, r_h). Allowing a range of power-law index from n = 1.0 to 1.8 and a ratio of stellar- to gas-velocity

dispersion of $f_{\sigma}=1$ –2 (Korchagin et al. 2003), we calculate the best-fit absolute star formation efficiency, A, and in Figure 2 we overlay the best-fit solutions. Over the range n=1.0–1.8, the best-fit absolute star formation efficiency for the sample is $A=(4.1\pm2.4)\times10^{-4}\,M_{\odot}\,{\rm yr^{-1}}\,{\rm kpc^{-2}}$ (where the error bar incorporates the galaxy-to-galaxy variation, a range of $f_{\sigma}=1$ –2, and the errors on the stellar masses of each galaxy). We note that at low star formation rates and stellar masses, there is a non-zero velocity dispersion due to the sound speed (c_s) of the gas $(c_s\lesssim10~{\rm km~s^{-1}}$ for the Milky Way at the solar circle), which we have neglected since this is below both the resolution limit of our observations and the minimum velocity dispersion caused the stellar disks in these systems.

We can improve these constraints further by assuming that star formation in each galaxy behaves in a similar way. We reiterate that this model assumes the star formation is occurring in a marginally Toomre stable disk, where the star formation follows the Kennicutt–Schmidt Law. Over a range $A = 10^{-5}-10^{-2}$ (M_{\odot} yr⁻¹ kpc⁻²) and n = 0.8-2.5, we construct a likelihood distribution for all nine galaxies and then convolve these to provide a composite likelihood distribution, and show

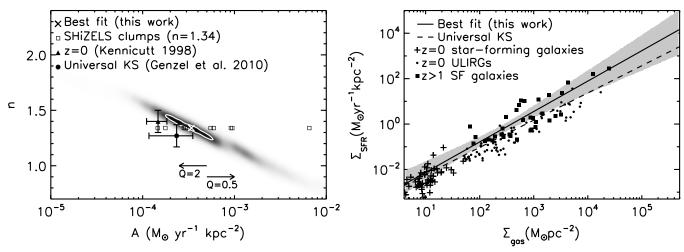


Figure 3. Left: the likelihood distribution for the power-law index (n) and absolute star formation efficiency (A) in the Kennicutt–Schmidt law derived from the $\Sigma_{\rm SFR}-\sigma$ relations in Figure 2 and assuming that the galaxies are marginally unstable, Q=1 (Equation (4)). The best-fit solutions (within the 1σ contour) have $n=1.34\pm0.15$ and $A=3.4^{+2.5}_{-1.6}\times10^{-4}~M_{\odot}~{\rm yr}^{-1}~{\rm kpc}^{-2}$. The arrows show how the absolute star formation efficiency would change if we adopt Q=0.5, or Q=2 (e.g., Leroy et al. 2008). We also plot the position of the clumps (adopting n=1.34). Right: the relation between star formation and gas-surface surface density for local and high-redshift star-forming galaxies and ULIRGs (Genzel et al. 2010). The dashed line and shaded region show the Kennicutt–Schmidt relation with our coefficients of $n=1.34\pm0.15$ and $A=3.4^{+2.5}_{-1.6}\times10^{-4}~M_{\odot}~{\rm yr}^{-1}~{\rm kpc}^{-2}$. The solid line shows that best-fit solution for the "universal" relation from Genzel et al. (2010), which is well matched to our derived values.

Table 1
Targets and Galaxy Properties

ID	R.A. (J2000)	decl. (J2000)	$z_{\rm H\alpha}$	$SFR_{H\alpha}^{a}$ $(M_{\odot} \text{ yr}^{-1})$	$r_{1/2}^{\rm b}$ (kpc)	$\sigma_{\rm H\alpha}^{\ \ c}$ (km s ⁻¹)	$v_{\rm asym}^{ m d}$ (km s ⁻¹)	E(B-V)	$\log(M_{\star}/M_{\odot})$	$\log(M_{\rm gas}/M_{\odot})$
SHiZELS-1	02 18 26.3	-04 47 01.6	0.8425	2	1.8 ± 0.3	98 ± 15	112 ± 11	0.4 ± 0.1	10.03 ± 0.15	9.4 ± 0.4
SHiZELS-4	10 01 55.3	+02 14 02.6	0.8317	1	1.4 ± 0.5	77 ± 20		0.0 ± 0.2	9.74 ± 0.12	8.9 ± 0.4
SHiZELS-7	02 17 00.4	$-05\ 01\ 50.8$	1.4550	8	3.7 ± 0.2	75 ± 11	145 ± 10	0.2 ± 0.2	9.81 ± 0.28	9.8 ± 0.4
SHiZELS-8	02 18 21.0	$-05\ 19\ 07.8$	1.4608	7	3.1 ± 0.3	69 ± 10	160 ± 12	0.2 ± 0.2	10.32 ± 0.28	9.8 ± 0.4
SHiZELS-9	02 17 13.0	-045440.7	1.4625	6	4.1 ± 0.2	62 ± 11	190 ± 20	0.2 ± 0.2	10.08 ± 0.28	9.8 ± 0.4
SHiZELS-10	02 17 39.0	$-04\ 44\ 43.1$	1.4471	10	2.3 ± 0.2	64 ± 8	30 ± 12	0.3 ± 0.2	9.42 ± 0.33	9.9 ± 0.4
SHiZELS-11	02 18 21.2	$-05\ 02\ 48.9$	1.4858	8	1.3 ± 0.4	190 ± 18	224 ± 15	0.5 ± 0.2	11.01 ± 0.24	10.1 ± 0.4
SHiZELS-12	02 19 01.4	-045814.6	1.4676	5	0.9 ± 0.5	115 ± 10		0.3 ± 0.2	10.59 ± 0.30	9.6 ± 0.4
SHiZELS-14	10 00 51.6	+02:33 34.5	2.2418	27	4.6 ± 0.4	131 ± 17		0.4 ± 0.1	10.90 ± 0.20	10.1 ± 0.4
Median			1.46	7 ± 2	2.4 ± 0.7	75 ± 19	147 ± 31	0.3 ± 0.1	10.25 ± 0.50	9.8 ± 0.2

Notes

this in Figure 3. Although the values of n and A are clearly degenerate, the best-fit solutions have $n=1.34\pm0.15$ and $A=3.4^{+2.5}_{-1.6}\times10^{-4}\,M_{\odot}\,{\rm yr}^{-1}\,{\rm kpc}^{-2}$. Our derived values for the absolute star formation efficiency, A, and power-law index, n, are within the 1σ of the values derived for local galaxies (e.g., Kennicutt 1998b; Leroy et al. 2008).

Using the ^{12}CO to trace the cold molecular gas, Genzel et al. (2010) showed that gas and star formation surface densities of high-redshift ($z \sim 1.5$) star-forming galaxies and ULIRGs are also well described by the Kennicutt–Schmidt relation with coefficients $n = 1.17 \pm 0.10$ and $A = (3.3 \pm 1.5) \times 10^{-4} \, M_{\odot} \, \text{yr}^{-1} \, \text{kpc}^{-2}$, which are comparable to the coefficients we derive from our sample.

In Figure 3, we plot the star formation and gas surface density for both local and high-redshift star-forming galaxies and ULIRGs from Genzel et al. (2010) and overlay the range of acceptable solutions implied by our data. We reiterate that we have adopted Q=1 for this analysis and note that if we

adopt Q < 1, then the absolute star formation efficiency will be increased proportionally (as shown in Figure 3). Nevertheless, this shows that the values of n and A we derive are consistent with the local and high-redshift star-forming galaxies and ULIRGs, but are free from uncertainties associated with converting 12 CO luminosities to molecular gas mass, CO excitation, or spatial extent of the gas reservoir.

Using the values of n and A that we have derived, we infer cold molecular gas masses for the galaxies in our sample of $M_{\rm gas} = 10^{9-10} \, M_{\odot}$ with a median $M_{\rm gas} = 7 \pm 2 \times 10^9 \, M_{\odot}$. This suggests a cold molecular gas fraction of $M_{\rm gas}/(M_{\rm gas} + M_{\star}) = 0.3 \pm 0.1$ but with a range of 10%-75%, similar to those derived for other high-redshift starbursts in other surveys (Tacconi et al. 2010; Daddi et al. 2010; Swinbank et al. 2011).

Finally, with estimates of the disk surface density, we can use Equation (1) to construct maps of the spatially resolved Toomre parameter, Q(x, y). Since we set Q = 1 to derive the coefficients n and A, by construction the average Q across the population is

^a Hα star formation rate using the calibration from Kennicutt (1998a) with a Chabrier IMF; SFR_{Hα} = $4.6 \times 10^{-42} L_{Hα}$.

^b H α half-light radius, deconvolved for the PSF.

^c Average velocity dispersion for each galaxy, corrected for beam smearing due to the PSF.

d v_{asym} denotes the best-fit asymptotic rotation speed of the galaxy, and is corrected for inclination (see Swinbank et al. 2012 for details on the kinematic modeling of these galaxies).

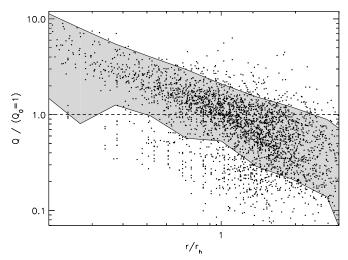


Figure 4. Variation in Toomre parameter (Q(x, y)) within the ISM of the nine galaxies in our sample as a function of (normalized) radius. The solid points denote the measurements at each pixel within each galaxy and the gray region shows the 18 and 81 percentile limits of the distribution. By construction, the average Toomre Q in the sample is Q(x, y) = 1, but varies by a factor ~ 10 within the ISM, with the highest-Q (most stable) in the central regions.

unity, but the relative range of Q(x, y) within the ISM of each galaxy is unaffected by this assumption. In Figure 1, we show the maps of Q(x, y) for each galaxy in our sample (with contours marking Q(x, y) = 0.5, 1.0, and 2.0). This shows that there is a range of Toomre Q across the ISM, and to highlight the variation with radius, in Figure 4 we show the Toomre parameter within each pixel of each galaxy as a function of radius (normalized to the half-light radius, $r_{\rm h}$). This shows that in the central regions, on average, the Toomre Q increases by a factor $\sim 4 \times$ compared to Q at the half-light radius, while a radii greater than $r_{\rm h}$, Q decreases by approximately the same factor.

3.1.1. Identification of Star-forming Regions

As Figure 1 shows, the galaxies in our sample exhibit a range of H α morphologies, from compact (e.g., SHiZELS 11 & 12) to very extended/clumpy (e.g., SHiZELS 7, 8, 9 & 14). To identify star-forming regions on \sim kpc scales and measure their basic properties, we isolate the star-forming clumps above the background (σ_{bg}) by first converting the H α flux map into photon counts (accounting for telescope efficiency) and then searching for $3\sigma_{bg}$ over-densities above the radially averaged background light distribution. In this calculation, we demand that any region is at least as large as the PSF. We identify 11 such regions and highlight these in Figure 1.

It is still possible that selecting star-forming regions in this way may give misleading results due to random associations and signal-to-noise effects. We therefore use the H α surface brightness distribution from the galaxies and randomly generate 10^5 mock images to test how many times a "clump" is identified. We find that only 2 ± 1 spurious clumps (in our sample of 11 galaxies) could be random associations.

Next, we extract the velocity dispersion and luminosity of each clump from using an isophote defining the star-forming region and report their values in Table 2 (the clump velocity dispersions have been corrected for the local velocity gradient from the galaxy dynamics and sizes are deconvolved for the PSF). Using the velocity dispersion and star formation density of each clump, and fixing the power-law index in the Kennicutt–Schmidt relation to n = 1.34, we compute their

Table 2
Physical Properties of the Star-forming Clumps

Galaxy	SFR $(M_{\odot} \text{ yr}^{-1})$	$\sigma_{ m H}\alpha$ (km s ⁻¹)	[N 11]/Hα	r _h (kpc)
SHiZELS-7	0.5 ± 0.1	40 ± 10	0.07 ± 0.03	0.8 ± 0.2
SHiZELS-7	1.3 ± 0.1	61 ± 12	0.34 ± 0.03	1.0 ± 0.2
SHiZELS-8	2.0 ± 0.1	79 ± 10	0.36 ± 0.03	0.7 ± 0.2
SHiZELS-8	1.6 ± 0.2	95 ± 14	0.26 ± 0.04	0.8 ± 0.2
SHiZELS-8	1.9 ± 0.1	140 ± 20	0.21 ± 0.04	0.9 ± 0.2
SHiZELS-9	2.1 ± 0.2	97 ± 15	0.31 ± 0.04	0.7 ± 0.2
SHiZELS-9	2.3 ± 0.1	80 ± 10	0.26 ± 0.03	1.3 ± 0.2
SHiZELS-9	0.9 ± 0.1	86 ± 14	0.40 ± 0.03	< 0.7
SHiZELS-14	0.5 ± 0.1	56 ± 12	0.12 ± 0.04	0.9 ± 0.2
SHiZELS-14	1.1 ± 0.2	121 ± 20	0.24 ± 0.03	< 0.7
SHiZELS-14	0.2 ± 0.1	100 ± 25	-0.03 ± 0.05	0.9 ± 0.3
Median	1.4 ± 0.4	88 ± 9	0.24 ± 0.06	0.85 ± 0.10

Notes. Half-light radius, $r_{\rm h}$, is deconvolved for PSF and the velocity dispersion, σ , is corrected for local velocity gradient (see Section 3.1). The star formation rates (SFRs) are calculated from the H α line luminosity using SFR_{H α} = 4.6 × $10^{-42}~L_{\rm H}\alpha$.

absolute star formation efficiencies, deriving a median $A_{\text{clump}} = 5.4 \pm 1.5 \times 10^{-4}$ (Figure 3). This corresponds to an offset (at fixed *n*) from the galaxy average of $A_{\text{clump}}/A = 1.3 \pm 0.4$. Equivalently, if we fix the absolute star formation efficiency to that of the galaxy-average, then the Toomre parameter in these regions is $Q = 0.8 \pm 0.4$.

3.2. The Scaling Relations of Local and High-redshift Star-forming Regions

The internal kinematics and luminosities of HII regions in local galaxies, derived from the line widths of their emission lines, have been the subject of various studies for some time (e.g., Terlevich & Melnick 1981; Arsenault et al. 1990; Rozas et al. 1998, 2006; Relaño et al. 2005). In particular, if the large line widths of star-forming H II regions reflect the virialization of the gas, then they can be used to determine their masses. However, it is unlikely that this condition holds exactly at any time during the evolution of an H II region due to the input of radiative and mechanical energy, principally from their ionizing stars (e.g., Castor et al. 1975). Nonetheless, the least evolved H II regions may well be within a factor of a few (two to three) of having their kinematics determined by their virial masses (at an early stage, the stellar ionizing luminosities are maximized, whereas the mechanical energy input is minimized; Leitherer et al. 1999). In the case of H_{II} regions close to virial equilibrium, the use of the line-width to compute gaseous masses offers a relatively direct means to study the properties since it is independent of the small-scale structure (density, filling factor, etc.).

Terlevich & Melnick (1981) showed that the H β luminosity of the most luminous H II regions varies as $L(H\beta) \propto \sigma^{4.0\pm0.8}$. This result suggests that the most luminous H II regions are likely to be virialized, so that information about their masses, and the resultant mass–luminosity relation, could be obtained using the virial theorem (they also claimed a relation between a radius parameter and the square of the velocity dispersion σ for H II regions, as further evidence for virialization). However, more recent studies, in particular by Rozas et al. (2006), suggest that in super-giant H II regions, $L \propto \sigma^{2.9\pm0.2}$ may be a more appropriate scaling (the lower exponent arises since H II regions with the largest luminosities are generally density-bound, which means that a significant fraction of the ionizing radiation escapes

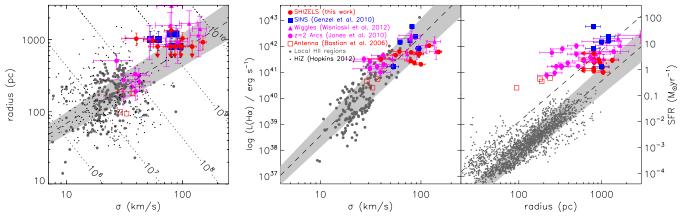


Figure 5. Scaling relations between size, luminosity, and velocity dispersion for the star-forming regions in our high-redshift galaxies compared to those in local GMCs and H II regions. In all of these plots, we baseline our measurements against local data from Terlevich & Melnick (1981), Arsenault et al. (1990), Bordalo & Telles (2011), Fuentes-Masip et al. (2000), and Rozas et al. (2006). Left: the relation between velocity dispersion and size. For the high-redshift star-forming regions, we also include clump measurements from SINS (Genzel et al. 2011), ZWiggles (Wisnioski et al. 2012), and the cluster arc survey from (Jones et al. 2010). We also plot the properties of the HiZ GMCs from the numerical simulations from Hopkins (2012). The dashed line shows a fit to the data of the form $r \propto \sigma^{1.01}$. The dashed lines show lines of constant gas mass (Equation (9)). Middle: the relation between velocity dispersion and luminosity of star-forming regions in high-redshift galaxies compared to those locally. The dashed line denotes $L \propto \sigma^{3.8}$, which provides a good match to both the local and high-redshift data. Right: the scaling relation between size and luminosity of star-forming regions. The high high-redshift star-forming regions have luminosity densities which are a factor $\sim 15 \pm 5 \times$ higher than those typically found locally (see also Wisnioski et al. 2012).

(A color version of this figure is available in the online journal.)

and so does not contribute to the luminosity, making shallower slopes physically possible).

To investigate the scaling relations of star-forming regions, in Figure 5 we show the relations between luminosity, size, and velocity dispersion of the clumps in our sample compared to GMCs and H II regions in the Milky Way and local galaxies (Terlevich & Melnick 1981; Arsenault et al. 1990; Bordalo & Telles 2011; Fuentes-Masip et al. 2000; Rozas et al. 2006). In this plot, we also include the measurements of giant star-forming regions from other high-redshift star-forming galaxies at $z \sim 1$ from Wisnioski et al. (2012), the $z \sim 1$ –2 galaxies from SINS (Genzel et al. 2011), and the clumps identified in strongly lensed $z \sim 1.5$ –3 galaxies from Jones et al. (2010) and Stark et al. (2008).

Despite the scatter, the radius— σ and σ —luminosity relations of the high-redshift clumps approximately follow the same scaling relations as those locally, but extending up to \sim kpc scales. Indeed, including all of the data points in the fits, we derive the scaling between size (r), luminosity (L), and velocity dispersion (σ) of

$$\log\left(\frac{r}{\text{kpc}}\right) = (1.01 \pm 0.08) \log\left(\frac{\sigma}{\text{km s}^{-1}}\right) + (0.8 \pm 0.1) (5)$$

and

$$\log\left(\frac{L}{\text{erg s}^{-1}}\right) = (3.81 \pm 0.29)\log\left(\frac{\sigma}{\text{km s}^{-1}}\right) + (34.7 \pm 0.4).$$
(6)

Equation (5) suggests $\sigma \propto R$. If the clouds are self-gravitating clouds with $\sigma \propto R$, then the virial density is constant. The relation $L \propto \sigma^{3.81\pm0.29}$ is in reasonable agreement with the early work from Terlevich & Melnick (1981) and steeper than that found for super-giant H II regions in local galaxies (Rozas et al. 2006), although the large error bars (on both the local and high-redshift data) preclude any firm conclusions. Clearly, a larger sample is required to confirm this result and/or test whether the scatter in the data is intrinsic.

If the star-forming regions we have identified are short lived, then these scaling relations effectively reflect initial collapse conditions of the clump as it formed, since a clump can not evolve far from those initial conditions (e.g., Ceverino et al. 2010). In this case, the relation between radius, velocity dispersion, and gas mass should follow $r = \sigma^2/(\pi G \Sigma_{\rm disk})$ (see Section 3.3). In Figure 5, we therefore overlay contours of constant gas mass in the r- σ plane, which suggests that the initial gas masses for the clumps is $M_{\rm gas}^{\rm initial} = 2 \pm 1 \times 10^9 \, M_{\odot}$ a factor $\sim 1000 \times$ more massive than the star-forming complexes in local galaxies (e.g., see also Elmegreen et al. 2009; Genzel et al. 2011; Wisnioski et al. 2012). If we assume our gas mass estimates from Section 3.1, then these star-forming regions may contain as much as $\sim 10\%$ -20% of the cold molecular gas in the disk.

Turning to the relation between the size and luminosity of the star-forming regions, it is evident from Figure 5 that the star formation densities of the high-redshift clumps are higher than those locally. Indeed, local star-forming regions follow a scaling relation

$$\log\left(\frac{L}{\text{erg s}^{-1}}\right) = (2.91 \pm 0.15)\log\left(\frac{r}{\text{kpc}}\right) + (32.1 \pm 0.3). (7)$$

We do not have a sufficient number of objects or the dynamic range to measure both the slope and zero point of the size–luminosity relation in the high-redshift clumps, and so instead we fix the slope of the local relation (which is $L \propto r^{2.91 \pm 0.15}$) and fit for the zero point evolution and obtain

$$\log\left(\frac{L}{\text{erg s}^{-1}}\right) = (2.91 \pm 0.15)\log\left(\frac{r}{\text{kpc}}\right) + (33.2 \pm 0.4). (8)$$

This suggests that high-redshift star-forming regions have luminosities at a fixed size that are on average a factor $15 \pm 5 \times$ larger than those locally (see also Swinbank et al. 2009, 2010; Jones et al. 2010; Wisnioski et al. 2012). We note that high luminosities at fixed size have been found in local starbursts, such as in the Antennae (Bastian et al. 2006), while offsets of

factors $\sim 50 \times$ have been inferred for star-forming regions in high-redshift galaxies (e.g., Swinbank et al. 2009; Jones et al. 2010; Wisnioski et al. 2012).

3.3. The Relation between the Disk and Clump Properties

It is possible to relate the properties of the clumps to the overall properties of the disk (e.g., Hopkins et al. 2012). For example, the velocity dispersion of the fastest growing Jeans unstable mode which cannot be stabilized by rotation in a gas disk is given by

$$\sigma_t(R)^2 = \pi \ G \Sigma_{\text{disk}} R \tag{9}$$

(e.g., Escala & Larson 2008; Elmegreen 2009; Dekel et al. 2009; Genzel et al. 2011; Livermore et al. 2012). The critical density for collapse (ρ_c) on scale *R* from a turbulent ISM is given by

$$\rho_c = \frac{3}{4\pi R^3} M_{\rm J} \simeq \frac{9}{8\pi R^2 G} \sigma_t(R)^2, \tag{10}$$

where $\sigma_t(R)$ is the line-of-sight turbulence velocity dispersion and M_J is the Jeans mass. The critical density for collapse therefore scales as

$$\rho_c(R) = \frac{9}{8R} \, \Sigma_{\text{disk}}.\tag{11}$$

Assuming that the cloud contracts by a factor $\simeq 2.5$ as it collapses, the post-collapse surface density of the cloud is

$$\Sigma_{\rm cloud} \simeq 10 \, \rho_c R \simeq 10 \, \Sigma_{\rm disk}$$
 (12)

(see also Livermore et al. 2012). Thus, the surface density of the collapsed cloud is independent of radius and proportional to the surface density of the disk, with the normalization set by the collapse factor and under the assumption Q=1. Hopkins (2012) shows that this model provides a reasonable fit to GMCs in the Milky Way and further suggests that the surface density (and hence surface brightness) of clouds should increase with the surface density of the disk.

Using our estimates of the stellar and gas masses and spatial extent of the galaxies in our sample, we derive disk surface densities of $\Sigma_{\rm disk} = 1.1 \pm 0.4 \times 10^9 \, M_{\odot} \, \rm kpc^{-2}$ and hence expect the mass surface densities of the starforming regions that form to have mass surface densities of $\Sigma_{\rm clump} \sim 10^{10}\,{\rm M_\odot~kpc^{-2}}$. It is instructive to compare this to the average mass surface density of the clumps. For example, assuming that their velocity dispersions are virial and adopting $M_{\text{clump}} = C\sigma^2 r_h/G$, and using the average velocity dispersion and size of the clumps (Table 2), we derive an average clump mass surface density of Σ_{clump} = 8 \pm 2 imes $10^9 M_{\odot} \text{ kpc}^{-2}$ with C = 5 (appropriate for a uniform density sphere). Although this calculation should be considered crude as it is unclear whether the velocity dispersions we measure are virial, it is encouraging that the predicted surface mass densities of the clumps are similar to those inferred from their velocity dispersions and sizes.

Finally, Hopkins (2012; see also Escala & Larson 2008 and Livermore et al. 2012) shows that for a marginally stable disk of finite thickness, density structures on scales greater than h will tend to be stabilized by rotation which leads to an exponential cutoff of the clump mass function above

$$M_0 \simeq \frac{4\pi}{3} \rho_c(h) h^3 = \frac{3\pi G^2}{2} \frac{\Sigma_{\text{disk}}^3}{\kappa^4}$$
 (13)

01

$$\frac{M_0}{M_\odot} = 8.6 \times 10^3 \left(\frac{\Sigma_{\text{disk}}}{10 \, M_\odot \, \text{pc}^{-2}}\right)^3 \left(\frac{\kappa}{100 \, \text{km s}^{-1} \, \text{kpc}}\right)^{-4}.$$
(14)

This suggests that the most massive clumps that can form in a disk ("the cutoff mass") depend strongly on the disk surface density—increasing the disk surface density increases mass of the clumps that are able to form (e.g., Escala 2011). However, there is also a competing (stabilizing) factor from the epicyclic frequency such that at a fixed radius, higher circular velocities reduce the mass of the largest clumps able to form.

Applying Equation (14) to the Milky Way, with a cold molecular gas fraction of 10%, $f_{\sigma} = 2$ (Korchagin et al. 2003), the average surface density is $\Sigma_{\rm disk} = 35\,M_{\odot}\,{\rm pc}^{-2}$ and for $\kappa = 220~{\rm km~s}^{-1}/8$ kpc (Feast & Whitelock 1997) the cutoff mass should be $M_0 \sim 10^7\,M_{\odot}$, in good agreement with the characteristic mass of the largest galactic GMCs (e.g., Stark & Lee 2006).

How does the cutoff mass for our high-redshift sample compare to local galaxies? For $f_{\sigma}=2$, and using the scaling relations derived in Section 3.1 to estimate the gas mass (Table 1; $A=3.4\times 10^{-4}\,M_{\odot}\,{\rm yr^{-1}\,kpc^{-2}}$ and n=1.34), we derive a range of cutoff masses of $M_0=0.3$ –30 $\times 10^9\,M_{\odot}$ (with a median and error of the sample of $M_0=9\pm 5\times 10^9\,M_{\odot}$). This is similar to the mass inferred for the brightest star-forming regions seen in high-resolution images of other high-redshift galaxies (Elmegreen 1989; Elmegreen et al. 2007, 2009; Bournaud & Elmegreen 2009; Förster Schreiber et al. 2011b; Genzel et al. 2011; Wisnioski et al. 2012), and a factor $\sim 1000\times$ higher than the largest characteristic mass of a star-forming region in the Milky Way.

In Figure 6, we plot our estimates of the cutoff mass versus the clump star formation densities for the galaxies in our sample (see also Livermore et al. 2012). We use the H α -derived star formation rate for each clump, corrected for galaxy reddening (note that we do not have reddening estimates for individual clumps and so we assume a factor 2× uncertainty in their star formation surface density). We also include estimates of the cutoff mass and star formation surface density from the SINS survey of $z \sim 2$ galaxies from Genzel et al. (2011; with dynamics measured from Förster Schreiber et al. 2009 and Cresci et al. 2009), as well as measurements from the lensing samples of Livermore et al. (2012; $z \sim 1$) and Jones et al. (2010; $z \sim 2$). Although the error bars on individual measurements are large (particularly due to the uncertainties in deriving the gas surface density from the Kennicutt–Schmidt law), as can be seen from Figure 6, galaxies with high cutoff masses tend to have higher clump luminosity surface densities.

It is also useful to adopt simple models for the evolution of galaxy disks and gas fraction to investigate how the cutoff mass and clump properties may be expected to evolve with redshift. For example, Dutton et al. (2011) present an analytic model for the evolution of disk scaling relations (size, rotational velocity, and stellar mass with redshift; see Dutton et al. 2011, Table 3). Combining a simple model for the evolution of the gas fraction $f_{\rm gas} \propto (1+z)^b$ with b=1.5-2.5 (Geach et al. 2011) and using Equations (12) and (14), we show the expected evolution of the cutoff mass and clump luminosity surface density with redshift. This shows that as the gas fraction increases (and adopting evolving models for the size, disk, and circular velocity of galaxies), then the cutoff mass should increase by a factor $10-100\times$ over the redshift range

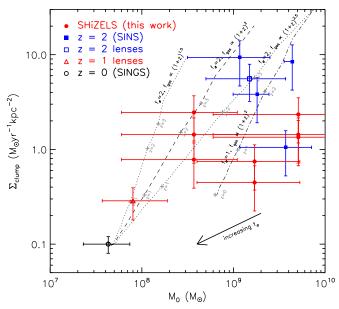


Figure 6. Most massive clumps that can form (the "cutoff mass," M_0) as a function of clump star formation surface density for SHiZELS galaxies. The cutoff mass is related to the disk surface density (Σ_{disk}) and epicyclic frequency (κ) via $M_0 \propto \Sigma_{\rm disk}^3 \kappa^{-4}$. The z=0 observations are derived from the Spitzer Infrared Nearby Galaxy Survey (SINGS; Kennicutt et al. 2003). We also include in the plot measurements of other high-redshift star-forming galaxies from the SINS survey (Genzel et al. 2011) and lensing surveys (Jones et al. 2010; Livermore et al. 2012). This shows that the cutoff mass and star formation surface densities of the high-redshift star-forming regions are (up to) a factor \sim 100× higher than star-forming regions in local galaxies. Using a simple model for galaxies with evolving gas fractions ($f_{\rm gas} \propto (1+z)^{(2\pm0.5)}$) and using the redshift evolution of disk scaling relations (size, rotational velocity, and stellar mass) from Dutton et al. (2011), Equations (12) and (14) can be used to derive model tracks to show how the cutoff mass and clump star formation surface density are expected to evolve with redshift. The dotted lines show how the cut off mass and star-formation surface density evolve with redshift for a ratio of stellar-to gas velocity dispersion for a ratio of stellar-to-gas velocity dispersion, $f_{\sigma} = 2$, but also show how the results change if we instead adopted vary for f_{σ} = 1. These tracks show that the cutoff mass and clump star formation surface density should increase by 1–2 dex between z = 0 and z = 3.

(A color version of this figure is available in the online journal.)

z = 0–2.5, while the star formation density of the clumps should increase by approximately an order of magnitude over the same redshift range. Although this is a simple model, this framework allows us to understand why the properties of the star-forming clumps within the ISM of our sample of high-redshift galaxies are different to those typically found in star-forming galaxies locally.

4. CONCLUSIONS

We have presented resolved spectroscopy of nine star-forming galaxies at z=0.84–2.23 selected from the UKIRT/HiZELS survey. These galaxies have reddening-corrected star formation rates of SFR = $16 \pm 5~M_{\odot}~\rm yr^{-1}$ and so are representative of the high-redshift population (Sobral et al. 2012b). The H α dynamics suggest that the ionized gas in at least six galaxies is in the form of large, rotating disks. We use the inferred rotation speeds of these systems, together with the spatial extent of the H α , to investigate the star formation within the ISM, and we derive the following main conclusions.

1. The star formation and velocity dispersion within the ISM of these high-redshift galaxies follow a power-law relation of the form $\sigma \propto A \Sigma_{\rm gas}^{1/n}$ + constant where the coefficients A

and n are set by the Kennicutt–Schmidt law ($\Sigma_{\rm SFR} = A\Sigma_{\rm gas}^n$) and the constant includes the disk stellar surface density of finite thickness. Assuming the gas disks are marginally stable (Q=1), we combine the solutions for each galaxy and derive best-fit parameters of power-law exponent, $n=1.34\pm0.15$, and absolute star formation efficiency, $A=3.4^{+2.5}_{-1.6}\times10^{-4}~M_{\odot}~\rm yr^{-1}~kpc^{-2}$. These values are consistent with the parameters derived via $^{12}{\rm CO}$ observations for both local and high-redshift star-forming galaxies, but free from any assumptions about $^{12}{\rm CO}$ –H₂ conversion factors, $^{12}{\rm CO}$ excitation, or the spatial extent of the gas reservoir.

- 2. Applying these coefficients, we infer cold molecular gas masses in the range $M_{\rm gas} = 10^{9-10} \, M_{\odot}$ with a median $M_{\rm gas} = 7 \pm 2 \times 10^9 \, M_{\odot}$ and hence a cold molecular gas fraction of $M_{\rm gas}/(M_{\rm gas} + M_{\star}) = 0.3 \pm 0.1$, but with a range of 10%-75%
- 3. Using a simple analytic model, we show that the largest structures that can form within the disk (the cutoff mass, M_0) are set by the disk surface density with a competing (stabilizing) force from the epicyclic frequency such that $M_0 \propto \Sigma_{\rm disk}^3 \kappa^{-4}$. For the galaxies in our sample, we derive cutoff masses of $M_0 \sim 10^9 \, M_{\odot}$, a factor $\sim 1000 \times$ higher than the largest characteristic mass of GMCs in the Milky Way.
- 4. Within the ISM of these galaxies, we reliably isolate 11 ~ kpc-scale star-forming regions and measure their properties. We show that their luminosities and velocity dispersions follow the same scaling relations between size and velocity dispersion as local H II regions. Assuming the line widths are virial, the masses derived for these star-forming regions are consistent with those implied by the cutoff mass. However, we find that the luminosity densities of these star-forming regions are a factor ~15× higher than those typically found locally, which we attribute to the requirement that the surface density of the (collapsed) cloud must be ~10× that of the disk.

Overall, the scaling relations we have derived suggest that the star formation processes in high-redshift disks are similar to those in local spiral galaxies, but occurring in systems with a gas rich and turbulent ISM. Given the paucity of gas-rich, clumpy disk-like high-redshift galaxies (Elmegreen et al. 2007, 2009; Förster Schreiber et al. 2011a), the next step in these studies is to spatially resolve the cold molecular gas via CO spectroscopy in a well-selected sample in order to better constrain the interaction between star formation and gas dynamics. Through comparisons with cosmologically based numerical simulations (e.g., Crain et al. 2009; van de Voort et al. 2011; Ceverino et al. 2010), as well as high-resolution simulations of individual gas-rich disks (e.g., Agertz et al. 2009; Krumholz & Burkert 2010), such observations may begin to differentiate whether the dominant mode of accretion is via three-dimensional cold gas flows accreting from the intergalactic medium, or from twodimensions from outskirts of the disk as gas cools from the hot halo.

We thank the anonymous referee for their constructive report which significantly improved the content and clarity of this paper. We thank Mario van der Ancker for help and support with the SINFONI planning/observations, and Richard Bower, Avashi Dekel, Reinhard Genzel, Rachael Livermore, Natascha Förster-Schreiber, and Phil Hopkins for a number of very useful discussions. A.M.S. gratefully acknowledges an STFC

Advanced Fellowship. D.S. is supported by a NOVA fellowship. I.R.S. acknowledges support from STFC and a Leverhume Senior Fellowship. J.E.G. is supported by a Banting Fellowship, administered by the Natural Sciences and Engineering Research Council of Canada. This research was also supported in part by the National Science Foundation under grant No. NSF PHY11-25915. The data presented here are based on observations with the SINFONI spectrograph on the ESO/VLT under program 084.B-0300.

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