

# The properties of the star-forming interstellar medium at $z = 0.84\text{--}2.23$ from HiZELS: mapping the internal dynamics and metallicity gradients in high-redshift disc galaxies

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## ABSTRACT

We present adaptive optics assisted, spatially resolved spectroscopy of a sample of nine  $H\alpha$ -selected galaxies at  $z = 0.84\text{--}2.23$  drawn from the HiZELS narrow-band survey. These galaxies have star formation rates of  $1\text{--}27 M_{\odot} \text{ yr}^{-1}$  and are therefore representative of the typical high-redshift star-forming population. Our  $\sim\text{kpc}$ -scale resolution observations show that approximately half of the sample have dynamics suggesting that the ionized gas is in large, rotating discs. We model their velocity fields to infer the inclination-corrected, asymptotic rotational velocities. We use the absolute  $B$ -band magnitudes and stellar masses to investigate the evolution of the  $B$ -band and stellar-mass Tully–Fisher relationships. By combining our sample with a number of similar measurements from the literature, we show that, at fixed circular velocity, the stellar mass of star-forming galaxies has increased by a factor of 2.5 between  $z = 2$  and 0, whilst the rest-frame  $B$ -band luminosity has decreased by a factor of  $\sim 6$  over the same period. Together, these demonstrate a change in mass-to-light ratio in the  $B$  band of  $\Delta(M/L_B)/(M/L_B)_{z=0} \sim 3.5$  between  $z = 1.5$  and 0, with most of the evolution occurring below  $z = 1$ . We also use the spatial variation of  $[\text{N II}]/H\alpha$  to show that the metallicity of the ionized gas in these galaxies declines monotonically with galactocentric radius, with an average  $\Delta \log(\text{O}/\text{H})/\Delta R = -0.027 \pm 0.005 \text{ dex kpc}^{-1}$ . This gradient is consistent with predictions for high-redshift disc galaxies from cosmologically based hydrodynamic simulations.

**Key words:** galaxies: evolution – galaxies: formation – galaxies: high-redshift.

## 1 INTRODUCTION

Numerical simulations indicate that the majority of massive galaxies at  $z = 1\text{--}3$ , the epoch when galaxies were most rapidly growing their stellar mass, are continuously fed by gas which promotes and maintains star formation (Bournaud & Elmegreen 2009; Dekel et al. 2009a; van de Voort et al. 2011, 2012). The accretion of gas from the halo, through minor mergers or by cold streams from the intergalactic medium (IGM), appears to dominate over that from major mergers and suggests that the star formation within the interstellar medium (ISM) of high-redshift galaxies is driven by internal dynamical processes (Kereš et al. 2005). The observational challenge

is now to quantitatively measure the internal properties (e.g. gas surface density, disc scaling relations, chemical abundances, distribution and intensity of star formation) and so test whether the prescriptions developed to describe star formation processes within discs at  $z = 0$  are applicable in the rapidly evolving ISM of gas-rich galaxies at high redshift (Krumholz & McKee 2005; Hopkins, Quataert & Murray 2012).

High spatial resolution observations of star-forming galaxies around  $z \sim 1\text{--}2$  have shown that a large fraction of the population have their ionized gas in large, rotating discs (e.g. Förster Schreiber et al. 2006, 2009; Genzel et al. 2006; Stark et al. 2008; Jones et al. 2010b; Wisnioski et al. 2011). In contrast to low redshift, these discs have high gas fractions ( $f_{\text{gas}} = 20\text{--}80$  per cent) and so are turbulent, with much higher velocity dispersions given their rotational velocity ( $\sigma = 30\text{--}100 \text{ km s}^{-1}$ ,  $v_{\text{rot}}/\sigma \sim 0.2\text{--}1$ ) compared to the thin discs

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of local spirals (Daddi et al. 2010; Tacconi et al. 2010; Geach et al. 2011; Swinbank et al. 2011).

If low- and high-redshift discs can be linked in a single evolutionary model, then the redshift evolution of disc scaling relations (i.e. between size, luminosity, rotational speed and gas fraction) provides a diagnostic of the relationship between the recent and past average star formation with the dark halo and the dominant mode of assembly.

The pioneering work of Vogt et al. (1996) and Vogt (1999) provided the first systematic study of the evolution of the stellar luminosity ( $M_B$ ) versus circular velocity (Tully–Fisher; Tully & Fisher 1977) relation, deriving an increase in luminosity at a fixed circular velocity of  $\Delta L_B = 1.7\times$  up to  $z \sim 1$ , reflecting the change in star formation efficiency over this period (see also Bamford et al. 2005; Fernández Lorenzo et al. 2009; Miller et al. 2011). Since the  $B$ -band luminosity is sensitive to recent star formation, attempts have also been made to measure the evolution of the stellar-mass ( $M_*$ ) Tully–Fisher relation which reflects the relation between the past average star formation history and halo mass. Although the current samples’ sizes are drawn from a heterogeneous mix of populations, evidence is accumulating that there is only modest evolution in the stellar-mass Tully–Fisher relation to  $z \sim 1.5$ , with stronger evolution above  $z \sim 1.5$  (Miller et al. 2012). Theoretical models of galaxy formation have struggled to reproduce the zero-point and slope of the Tully–Fisher relation, tending to produce discs that rotate too fast given their luminosities (e.g. Mo, Mao & White 1998; Benson et al. 2003; Dutton et al. 2011), although some of this discrepancy has been alleviated by improving the recipes for starburst-driven feedback (e.g. Sales et al. 2010; Piontek & Steinmetz 2011; Scannapieco et al. 2011; Tonini et al. 2011; Desmond 2012; McCarthy et al. 2012).

A second potential observational consequence of differences in fuelling mechanisms for disc galaxies is their chemical abundance distributions. The primary indicator of chemical evolution is typically traced by oxygen as its relative abundance surpasses all elements heavier than helium and it is present almost entirely in the gas phase (Snow & Witt 1996; Savage & Sembach 1996).

In the thin disc of the Milky Way and other local spirals, there is a negative radial metallicity gradient (e.g. Searle 1971; Shields 1974; McCall, Rybski & Shields 1985; Vila-Costas & Edmunds 1992; Zaritsky, Kennicutt & Huchra 1994; Ferguson, Gallagher & Wyse 1998; van Zee, Salzer & Haynes 1998). In contrast, the thick disc of the Milky Way displays no radial abundance gradient (Edvardsson et al. 1993; Gilmore, Wyse & Jones 1995; Bell 1996; Robin et al. 1996). Thick discs are ubiquitous in spiral galaxies, and typically contain 10–25 per cent of their baryonic mass, yet the thick disc of the Milky Way contains no stars younger than 8 Gyr (Gilmore & Wyse 1985; Reddy et al. 2006). Thick discs are comparable in many physical properties to the apparently turbulent discs of high-redshift galaxies, and so determining the early form of their abundance gradient (positive or negative) will provide a key indication of how quickly enrichment proceeds in inner and outer regions, as well as the interplay between star formation, clump migration and gas accretion from the halo or IGM (Solway, Sellwood & Schönrich 2012).

Indeed, if the majority of the gas accretion in high-redshift galaxies is via accretion from the IGM along filaments which intersect and deposit pristine material on to the galaxy disc at radii of 10–20 kpc, then the inner discs of galaxies should be enriched by star formation and supernovae whilst the outer disc continually diluted by pristine gas, leaving strong negative abundance gradients (Dekel

et al. 2009a) which will flatten as the gas accretion from the IGM becomes less efficient, and the gas redistributed, at lower redshift.

To gain a complete census of how galaxies assemble the bulk of their stellar mass, it is clearly important to study the dynamics, chemical properties and internal star formation processes in a well-selected sample of high-redshift galaxies. To this end, we have combined panoramic (degree-scale) imaging with near-infrared narrow-band filters, to carry out the High-Z Emission Line Survey (HiZELS), targeting  $H\alpha$  emitting galaxies in four precise ( $\delta z = 0.03$ ) redshift slices:  $z = 0.40, 0.84, 1.47$  and  $2.23$  (Geach et al. 2008; Sobral et al. 2009, 2010, 2011, 2012a,b). This survey provides a large, luminosity-limited sample of *identically* selected  $H\alpha$  emitters at epochs spanning the apparent peak of the cosmic star formation rate density, and provides a powerful resource for studying the properties of representative galaxies (i.e. star formation rates nearly tens of  $M_\odot \text{ yr}^{-1}$ ) which will likely evolve into  $\sim L^*$  galaxies by  $z = 0$ , but are seen at a time when they are assembling the bulk of their stellar mass, and thus at a critical stage in their evolutionary history. One of the key benefits of selecting a high-redshift galaxy population using  $H\alpha$  alone is the simplicity in comparison to similar luminosity-limited samples of star-forming galaxies in the local Universe. Together, these comparison samples can be used to search for differences in the physical properties of the ISM that potentially provide insight into the factors influencing star formation at high redshift.

In this paper, we present adaptive optical assisted ( $\sim$ kpc scale) integral field spectroscopy with the Spectrograph for Integral Field Observations in the Near Infrared (SINFONI) of nine star-forming galaxies selected from the HiZELS survey in the redshift range  $z = 0.84\text{--}2.23$  – the SINFONI-HiZELS (SHiZELS) survey. We use these data to investigate the dynamical properties of the galaxies, the evolution of the luminosity and stellar-mass scaling relations (through the Tully–Fisher relation), and the star formation and enrichment within their ISM. We use a cosmology with  $\Omega_\Lambda = 0.73$ ,  $\Omega_m = 0.27$  and  $H_0 = 72 \text{ km s}^{-1} \text{ Mpc}^{-1}$ . In this cosmology, at the median redshift of our survey,  $z = 1.47$ , a spatial resolution of 0.1 arcsec corresponds to a physical scale of 0.8 kpc. All quoted magnitudes are on the AB system and we use a Chabrier initial mass function (IMF; Chabrier 2003).

## 2 SAMPLE SELECTION, OBSERVATIONS AND DATA REDUCTION

### 2.1 HiZELS

To select the targets for Integral Field Unit (IFU) observations, we exploited the high density of sources in the HiZELS imaging of the COSMOS and UDS fields (Sobral et al. 2012b) to select  $H\alpha$  emitters which are close to bright ( $R < 15.0$ ) stars, such that natural guide star adaptive optics correction could be applied to achieve high spatial resolution. For this programme, we selected 14 galaxies with  $H\alpha$  fluxes from the HiZELS catalogue with fluxes between  $0.7$  and  $1.6 \times 10^{-16} \text{ erg s}^{-1} \text{ cm}^{-2}$  to ensure that their star formation properties and dynamics could be mapped in a few hours. However, of the 14 galaxies in our parent sample, only nine systems yield an  $H\alpha$  detection in the data cubes, which may (in part) be due to spurious detections in the early HiZELS catalogues. At the three redshift ranges of our sample, the average  $H\alpha$  fluxes of our galaxies correspond to star formation rates (adopting the Kennicutt 1998 calibration with a Chabrier IMF) of  $\text{SFR} = 4.6 \times 10^{-44} L_{H\alpha} = 1.7, 6.9$  and  $19.3 M_\odot \text{ yr}^{-1}$  at  $z = 0.83, 1.47$  and  $2.23$ , respectively.

Next we estimate the far-infrared luminosities for the galaxies in our sample. We exploit the *Herschel*/Spectral and Photometric

Imaging Receiver (SPIRE) imaging of these fields which were taken as part of the *Herschel* Multi-tiered Extragalactic Survey (HerMES). The SPIRE maps reach  $3\sigma$  limits of  $\sim 8$ , 10 and 11 mJy at 250, 350 and 500  $\mu\text{m}$ , respectively. None of the SHiZELS galaxies in our sample are individually detected (which is unsurprising given the implied star formation rates from  $\text{H}\alpha$ ), but we can search for an average star formation rate via stacking.

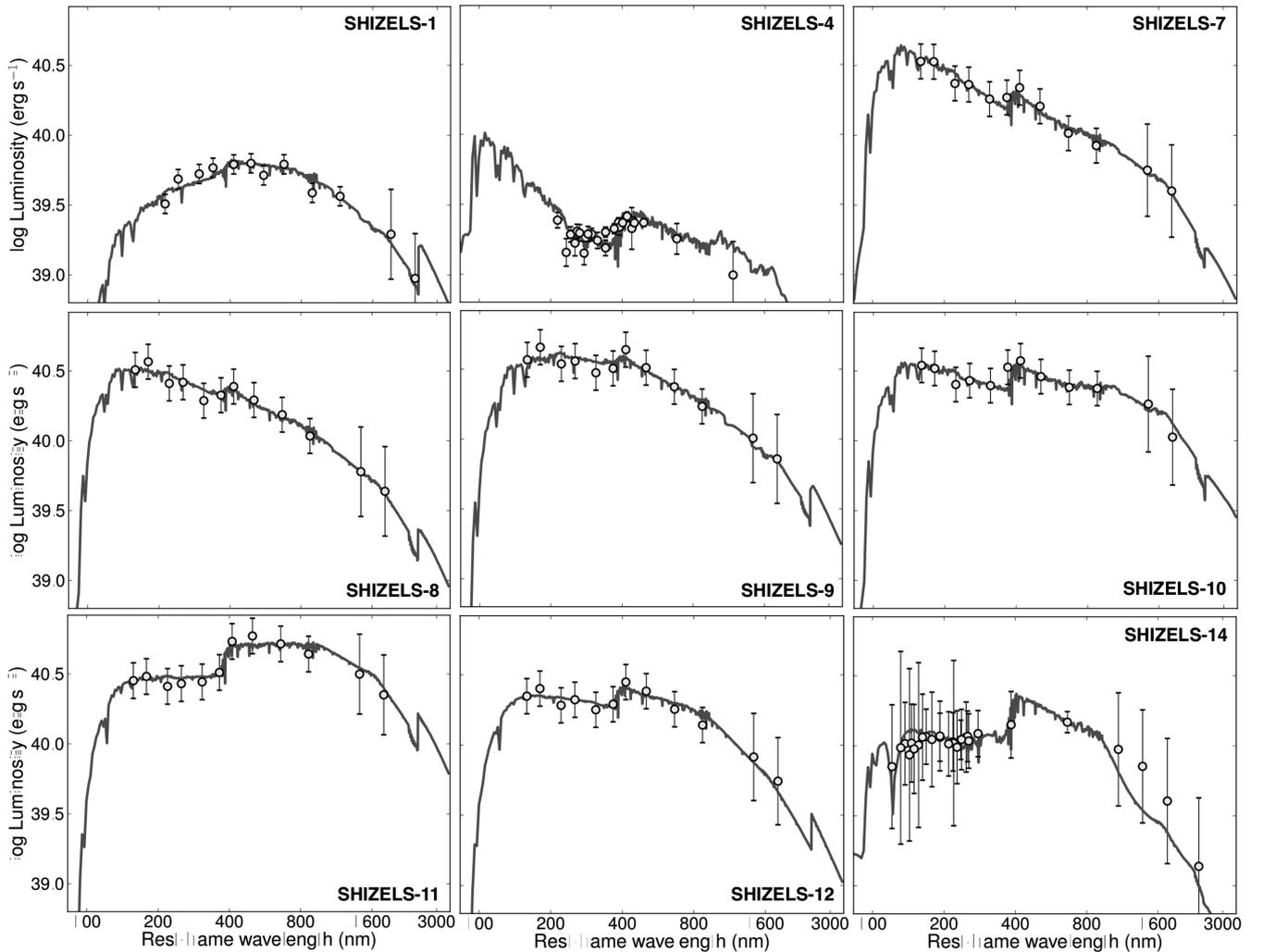
In the following analysis, we restrict ourselves to the  $z = 1.47$  galaxies only to mitigate against redshift effects in the stack on the spectral energy distribution (SED). The 250, 350 and 500  $\mu\text{m}$  stacked fluxes for the  $z = 1.47$  SHiZELS galaxies of  $6.9 \pm 1.7$ ,  $9.0 \pm 1.9$  and  $7.0 \pm 2.4$  mJy at 250, 350 and 500  $\mu\text{m}$ , respectively (or  $7.5 \pm 1.6$ ,  $9.2 \pm 2.2$  and  $7.4 \pm 3.0$  mJy at 250, 350 and 500  $\mu\text{m}$  if we instead stack all nine SHiZELS galaxies in our sample). A simple modified blackbody fit to this photometry (with a dust emissivity of  $\beta = 1.5\text{--}2.0$ ) at the known redshift yields a far-infrared luminosity (integrated between 8 and 1000  $\mu\text{m}$ ) of  $L_{8\text{--}1000\ \mu\text{m}} = 1.8 \pm 0.6 \times 10^{11} L_{\odot}$  and hence a total star formation rate of  $\text{SFR}_{\text{FIR}} = 2.7 \times 10^{-44} L_{\text{FIR}} = 18 \pm 8 M_{\odot} \text{ yr}^{-1}$ .

We note that if we instead stack all 317 HiZELS  $\text{H}\alpha$  emitters from the  $z = 1.47$  parent sample with fluxes  $> 1 \times 10^{-16} \text{ erg s}^{-1} \text{ cm}^{-2}$  in

the UDS and COSMOS fields, then the 250, 350 and 500  $\mu\text{m}$  fluxes are  $6.3 \pm 0.24$ ,  $7.9 \pm 0.25$  and  $5.6 \pm 0.31$  mJy, respectively, suggesting  $L_{\text{FIR}} = 1.5 \times 10^{11} L_{\odot}$  which is consistent with our SHiZELS sample.

Next, for all of the SHiZELS galaxies, we use the broad-band imaging of the galaxies in order to calculate the rest-frame SED, reddening and star formation histories and stellar masses (Sobral et al. 2010). We exploit deep archival multiwavelength imaging from rest-frame ultraviolet (UV) to mid-infrared bands (see Sobral et al. 2010 for references) and follow Sobral et al. (2011) to perform a full SED  $\chi^2$  fit using the Bruzual & Charlot (2003) population synthesis models but including the thermally pulsating asymptotic giant branch (TP-AGB) stellar phase and a Chabrier IMF (see Sobral et al. 2010 for the range of parameters). We use photometry from up to 36 (COSMOS) and 16 (UDS) wide, medium and narrow bands (spanning *GALEX* far-UV and near-UV bands to *Spitzer*/Infrared Array Camera (IRAC); Fig. 1) and in Table 2 we give the best-fitting stellar mass and  $E(B - V)$  for each galaxy.

The average  $E(B - V)$  for our sample is  $0.3 \pm 0.1$  which corresponds to  $A_{\text{H}\alpha} = 0.91 \pm 0.21$  ( $A_V = 1.11 \pm 0.27$ ). Applying this correction to the  $\text{H}\alpha$  luminosities suggests reddening-corrected star



**Figure 1.** Broad-band photometry and SEDs for the nine galaxies in our sample from rest-frame UV to mid-infrared bands (spanning *GALEX* far-UV and near-UV bands to *Spitzer*/IRAC). In all cases, we calculate the rest-frame SED and star formation history and use this information to estimate the stellar masses (Table 2). The SEDs are calculated using a  $\chi^2$  fit using the Bruzual & Charlot (2003) population synthesis models with a Chabrier IMF. The SHiZELS galaxies sample a range of stellar masses from  $\sim 10^9$  to  $10^{11} M_{\odot}$  and specific star formation rates of  $0.1\text{--}10 \text{ Gyr}^{-1}$ .

formation rates  $\text{SFR}_{\text{H}\alpha} = 16 \pm 5 M_{\odot} \text{ yr}^{-1}$ , which is similar to those derived from the far-infrared ( $\text{SFR}_{\text{FIR}} = 18 \pm 8 M_{\odot} \text{ yr}^{-1}$ ).

The rest-frame *B*-band magnitudes (uncorrected for extinction) and stellar masses are given in Table 2 (the  $1\sigma$  errors are drawn from the multidimensional  $\chi^2$  distribution and are typically 0.15 dex). In order that more direct comparisons can be made with other data sets, we also report the rest-frame *B*- and *K*-band magnitudes for each of the galaxies in our sample, and we note that the average inferred light-to-mass ratio is  $L_K/M = 0.58 \pm 0.14$ .

Thus, overall, these galaxies appear to have luminosities consistent with local Luminous Infrared Galaxies (LIRGs), with dust corrections of  $A_V \gtrsim 1$  and star formation rates characteristic of ‘typical’ star-forming galaxies at these epochs (Sobral et al. 2012b). Moreover, the SHiZELS galaxies sample a range of stellar masses from  $\sim 10^9$  to  $10^{11} M_{\odot}$  and specific star formation rates of  $0.1$ – $10 \text{ Gyr}^{-1}$ . Since one of the main high-redshift comparison samples we use throughout this paper is the SINFONI Near-Infrared Galaxy Survey (SINS; Förster Schreiber et al. 2009), we note that our sample has a comparable range of stellar masses, although the SINS sample tend to have higher  $\text{H}\alpha$ -derived star formation rates ( $\text{SFR}_{\text{H}\alpha} = 7 \pm 2$  and  $30 \pm 3 M_{\odot} \text{ yr}^{-1}$  for SHiZELS and SINS, respectively).

## 2.2 SINFONI observations

To map the nebular  $\text{H}\alpha$  emission-line properties of the galaxies in our sample, we used the SINFONI IFU on the European Southern Observatory/Very Large Telescope (ESO/VLT; Eisenhauer et al. 2003). The SINFONI IFU uses an image slicer and mirrors to reformat a field of  $3 \text{ arcsec} \times 3 \text{ arcsec}$  at a spatial resolution of  $0.1 \text{ arcsec pixel}^{-1}$ . At  $z = 0.84, 1.47$  and  $2.23$  the  $\text{H}\alpha$  emission line is redshifted to  $\sim 1.21, 1.61$  and  $2.12 \mu\text{m}$  and into the *J*, *H* and *K* bands, respectively. The spectral resolution in each band is  $\lambda/\Delta\lambda \sim 4500$  [the sky lines have  $4 \text{ \AA}$  full width at half-maximum (FWHM)]. In the remainder of our analysis, emission-line widths are deconvolved for the instrumental resolution. Since each of the targets were selected to be close to a bright adaptive optics (AO) star, we used natural guide star correction. The *R*-band magnitude of the AO stars is  $R = 12.0$ – $15.0$  and they have separations between 8 and 40 arcsec from the target galaxies.

To observe the targets we used ABBA chop sequences, nodding  $1.5 \text{ arcsec}$  across the IFU. We observed each target for between 3.6 and 13.4 ks (each individual exposure was 600 s) between 2009 September 10 and 2011 April 30 in  $\sim 0.6 \text{ arcsec}$  seeing and photometric conditions. The median Strehl achieved for our observations

is 20 per cent (Table 1) and the median encircled energy within  $0.1 \text{ arcsec}$  is 25 per cent (the approximate spatial resolution is  $0.1 \text{ arcsec}$  FWHM or  $850 \text{ pc}$  at  $z = 1.47$  – the median redshift of our survey). Individual exposures were reduced using the SINFONI ESOREX data reduction pipeline which extracts, flat-fields, wavelength calibrates and forms the data cube for each exposure. The final data cube was generated by aligning the individual data cubes and then combined these using an average with a  $3\sigma$  clip to reject cosmic rays. For flux calibration, standard stars were observed each night either immediately before or after the science exposures. These were reduced in an identical manner to the science observations.

## 2.3 Galaxy dynamics

All nine galaxies display strong  $\text{H}\alpha$  emission, with a range of  $\text{H}\alpha$  luminosities of  $L_{\text{H}\alpha} \sim 10^{41.4}$ – $10^{42.4} \text{ erg s}^{-1}$ . In Fig. 2 we show the galaxy-integrated one-dimensional spectrum from each galaxy. In all cases we clearly detect the  $[\text{N II}]\lambda 6583$  emission, the median  $[\text{N II}]/\text{H}\alpha$  for the sample is  $0.3 \pm 0.1$ , with a range of  $0.1 < [\text{N II}]/\text{H}\alpha < 0.6$ . None of the galaxies display strong active galactic nucleus (AGN) signatures in their near-infrared spectra.

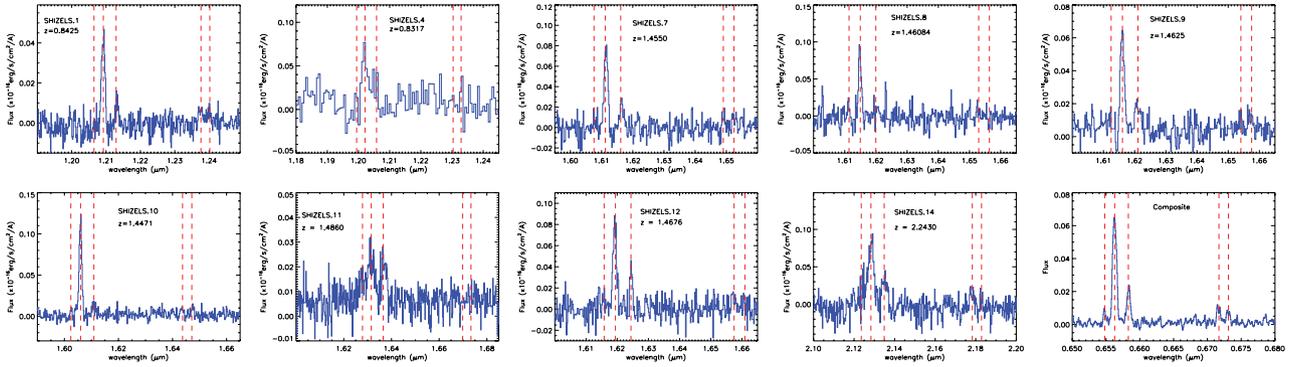
To search for fainter lines, we also transform each of the spectra to the rest frame and co-add them (weighted by flux) and show this stack in Fig. 2. In this composite, the  $[\text{N II}]/\text{H}\alpha = 0.29 \pm 0.02$  is consistent with the average of individual measurements. We also make a clear detection of the  $[\text{S II}]\lambda\lambda 6716, 6761$  doublet and derive a flux ratio of  $I_{6716}/I_{6731} = 1.36 \pm 0.08$  which corresponds to an electron density in the range  $100$ – $1000 \text{ cm}^{-3}$  (Osterbrock 1989) and a mass in the ISM of  $3$ – $30 \times 10^{10} M_{\odot}$  for a half-light radius of  $2 \text{ kpc}$  (Table 2). It is also useful to note that the  $[\text{S II}]\lambda\lambda 6716/\text{H}\alpha$  reflects the ionization strength of the ISM and we derive  $[\text{S II}]\lambda\lambda 6716/\text{H}\alpha = 0.13 \pm 0.04$  which suggests an ionization parameter  $\log(U/\text{cm}^3) = -3.5 \pm 0.3$  (Osterbrock 1989; Collins & Rand 2001). This is comparable to an ionization rate of  $\log_{10}(U/\text{cm}^3) \sim -3.9$  which can be inferred from the average star formation rate volume density of our galaxies and assuming that there are  $3 \times 10^{60}$  ionizing photons per unit solar mass of star formation (Cox 1983).

To measure the velocity structure in each galaxy, we fit the  $\text{H}\alpha$  and  $[\text{N II}]\lambda\lambda 6548, 6583$  emission lines pixel-by-pixel. We use a  $\chi^2$  minimization procedure, taking into account the greater noise at the positions of the sky lines. We first attempt to identify a line in each  $0.1 \times 0.1 \text{ arcsec pixel}$  [ $\sim 1 \times 1 \text{ kpc}$ , which corresponds to the approximate point spread function (PSF)], and if the fit fails to detect the emission line, the region is increased to  $2 \times 2 \text{ pixel}$ . Using

**Table 1.** Targets and observations.

ID	RA (J2000)	Dec. (J2000)	$z_{\text{H}\alpha}$	$t_{\text{exp}}$ (ks)	Strehl (per cent)	EE (0.1 arcsec) (per cent)
SHiZELS-1	02 18 26.3	−04 47 01.6	0.8425	9.8	15	11
SHiZELS-4	10 01 55.3	+02 14 02.6	0.8317	3.6	10	8
SHiZELS-7	02 17 00.4	−05 01 50.8	1.4550	13.4	27	25
SHiZELS-8	02 18 21.0	−05 19 07.8	1.4608	9.8	21	27
SHiZELS-9	02 17 13.0	−04 54 40.7	1.4625	9.8	24	27
SHiZELS-10	02 17 39.0	−04 44 43.1	1.4471	9.8	20	25
SHiZELS-11	02 18 21.2	−05 02 48.9	1.4858	3.6	13	32
SHiZELS-12	02 19 01.4	−04 58 14.6	1.4676	9.8	20	30
SHiZELS-14	10 00 51.6	+02:33 34.5	2.2418	12.0	12	26

*Note.* EE denotes the encircled energy within a radius of  $0.1 \text{ arcsec}$ .



**Figure 2.** Spatially integrated, one-dimensional spectra around the redshifted  $H\alpha$  emission for each of the galaxies in our sample. In each case, the dashed lines identify the  $H\alpha$ ,  $[\text{N II}]\lambda\lambda$  6583,6548 and  $[\text{S II}]\lambda\lambda$  6716,6731 emission lines. In the final panel, we show the flux-weighted composite spectrum. In all cases, we clearly detect  $[\text{N II}]$  emission and the median  $[\text{N II}]/H\alpha$  for the sample is  $0.3 \pm 0.1$ , with a range of  $0.1 < [\text{N II}]/H\alpha < 0.6$ . None of the galaxies display strong AGN signatures in their near-infrared spectra (e.g. broad lines or strong  $[\text{N II}]/H\alpha$  ratios).

**Table 2.** Integrated galaxy properties.

ID	$f_{H\alpha}$ ( $\times 10^{-16}$ $\text{erg s}^{-1} \text{cm}^{-2}$ )	$\text{SFR}_{H\alpha}$ ( $M_{\odot} \text{yr}^{-1}$ )	$r_{1/2}$ (kpc)	$[\text{N II}]/H\alpha$	$M_B$ (AB)	$M_K$ (AB)	$\log_{10}(M_*)$ ( $M_{\odot}$ )	$E(B - V)$	$\Delta \log(\text{O}/\text{H})/\Delta R$ (dex kpc $^{-1}$ )
SHiZELS-1	$1.0 \pm 0.1$	2	$1.8 \pm 0.3$	$0.2 \pm 0.05$	-18.70	-21.54	$10.03 \pm 0.15$	$0.4 \pm 0.1$	$-0.037^{+0.030}_{-0.058}$
SHiZELS-4	$0.7 \pm 0.1$	1	$1.4 \pm 0.5$	$0.2 \pm 0.1$	-20.68	-21.49	$9.74 \pm 0.12$	$0.0 \pm 0.2$	-
SHiZELS-7	$1.2 \pm 0.1$	8	$3.7 \pm 0.2$	$0.43 \pm 0.05$	-21.12	-22.15	$9.81 \pm 0.28$	$0.2 \pm 0.2$	$-0.019^{+0.019}_{-0.040}$
SHiZELS-8	$1.1 \pm 0.1$	7	$3.1 \pm 0.3$	<0.1	-21.26	-21.90	$10.32 \pm 0.28$	$0.2 \pm 0.2$	$+0.006^{+0.017}_{-0.004}$
SHiZELS-9	$1.0 \pm 0.1$	6	$4.1 \pm 0.2$	$0.27 \pm 0.03$	-21.77	-22.49	$10.08 \pm 0.28$	$0.2 \pm 0.2$	$-0.027^{+0.010}_{-0.018}$
SHiZELS-10	$1.6 \pm 0.2$	10	$2.3 \pm 0.2$	$0.13 \pm 0.04$	-21.15	-21.81	$9.42 \pm 0.33$	$0.3 \pm 0.2$	$-0.031^{+0.016}_{-0.014}$
SHiZELS-11	$1.3 \pm 0.1$	8	$1.3 \pm 0.4$	$0.6 \pm 0.1$	-22.13	-24.44	$11.01 \pm 0.24$	$0.5 \pm 0.2$	$-0.0870^{+0.032}_{-0.006}$
SHiZELS-12	$0.7 \pm 0.1$	5	$0.9 \pm 0.5$	$0.27 \pm 0.03$	-21.34	-22.44	$10.59 \pm 0.30$	$0.3 \pm 0.2$	-
SHiZELS-14	$1.6 \pm 0.1$	27	$4.6 \pm 0.4$	$0.60 \pm 0.05$	-23.55	-24.75	$10.90 \pm 0.20$	$0.4 \pm 0.1$	$-0.024^{+0.012}_{-0.012}$
Median	$1.1 \pm 0.1$	$7 \pm 2$	$2.4 \pm 0.7$	$0.27 \pm 0.08$	$-21.3 \pm 0.20$	$-22.2 \pm 0.3$	$10.25 \pm 0.50$	$0.3 \pm 0.1$	$-0.026 \pm 0.006$

*Note.*  $H\alpha$  fluxes are in units of  $10^{-16} \text{erg s}^{-1} \text{cm}^{-2}$ . The errors on the fluxes are dominated by  $\sim 10$  per cent systematic uncertainties in the flux calibration from the change in Strehl ratio between observing standard stars on-axis and the target galaxies off-axis.  $r_{1/2}$  is the  $H\alpha$  half-light radius and has been deconvolved for the PSF. Errors on  $M_B$  and  $M_K$  are typically 0.15 dex (Sobral et al. 2011).

a continuum fit we required a signal-to-noise ratio (S/N) of  $> 5$  to detect the emission line in each pixel, and when this criterion is met we fit the  $H\alpha$  and  $[\text{N II}]\lambda\lambda$  6548,6583 emission allowing the centroid, intensity and width of the Gaussian profile to vary (the FWHM of the  $H\alpha$  and  $[\text{N II}]$  lines are coupled in the fit). Uncertainties on each parameter of the fit are calculated by perturbing one parameter at a time, allowing the remaining parameters to find their optimum values, until  $\Delta\chi^2 = 1$  is reached.

Even with  $\sim \text{kpc}$ -scale resolution, we note that there is a contribution to the line widths of each pixel from the large-scale velocity motions across the PSF which must be corrected for (Davies et al. 2011). To account for this ‘beam smearing’, at each pixel where the  $H\alpha$  emission is detected, we calculate the local velocity gradient ( $\Delta V/\Delta R$ ) and subtract this in quadrature from the measured velocity dispersion.

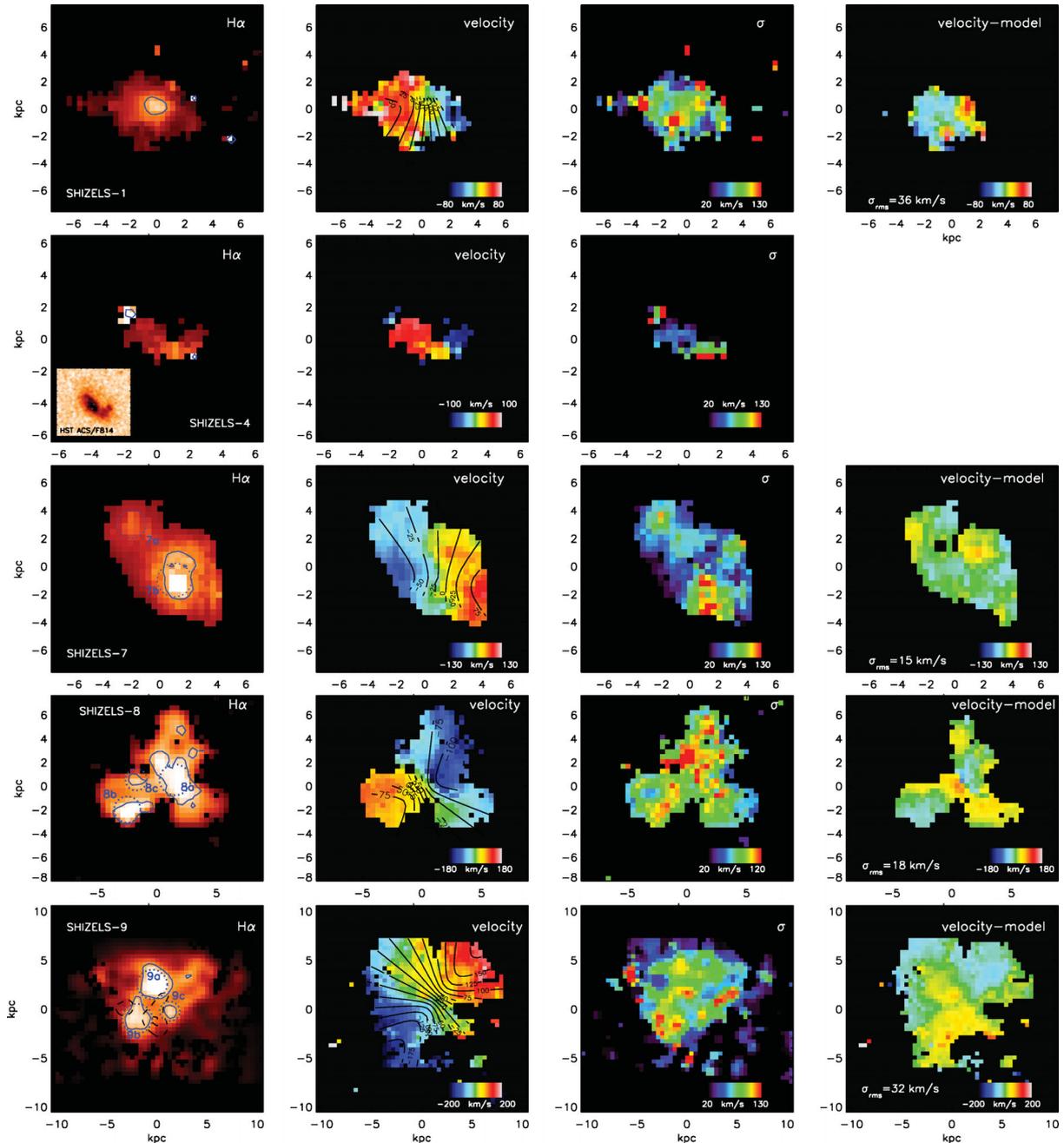
In Fig. 3 we show the  $H\alpha$  intensity, velocity and line-of-sight velocity dispersion maps for the galaxies in our sample. There is clearly a variety of  $H\alpha$  morphologies, ranging from compact (e.g. SHiZELS 11 and 12) to very extended/clumpy (e.g. SHiZELS 7, 8, 9 and 14). For three galaxies, we also include high-resolution broadband imaging thumbnails from *Hubble Space Telescope* Advanced Camera for Surveys (ACS)  $V$  band (SHiZELS 4 and 14) or Wide Field Camera 3 (WFC3)  $H$  band (SHiZELS 11) which shows that the  $H\alpha$  is well correlated with the rest-frame UV/optical morphology.

The distribution and intensity of star formation (and the properties of the star-forming clumps) are discussed in a companion paper (Swinbank et al. 2012). Fig. 3 also shows that there are strong velocity gradients in many cases (e.g. SHiZELS 1, 7, 8, 9, 10, 11 and 12). We will investigate how many of these systems can be classified as ‘discs’ in Section 3.

### 3 ANALYSIS, RESULTS AND DISCUSSION

All nine galaxies display velocity gradients in their  $H\alpha$  kinematics, with peak-to-peak velocity gradients ranging from 40 to 400  $\text{km s}^{-1}$  and a ratio of peak-to-peak difference ( $v_{\text{max}}$ ) to line-of-sight velocity dispersion ( $\sigma$ ) of  $v_{\text{max}}/\sigma = 0.3\text{--}2.9$ . Although a ratio of  $v_{\text{max}}/\sigma = 0.4$  has traditionally been used to crudely differentiate rotating systems from mergers (Förster Schreiber et al. 2009), more detailed kinematic modelling is essential to reliably differentiate rotating systems from mergers (Shapiro et al. 2008). We therefore begin by modelling each velocity field with a rotating disc in order to estimate the disc inclination and true rotational velocity (we exclude SHiZELS 4 and 12 from this analysis as their velocity fields are only marginally resolved by our data).

Although there have been several functional forms to describe rotation curves (such as the ‘multiparameter fit’, e.g. Courteau 1997 or the ‘universal rotation curve’; Persic, Salucci & Stel



**Figure 3.**  $H\alpha$  and kinematic maps of the SHIZELS galaxies. For each galaxy, the left-hand panel shows the  $H\alpha$  emission-line flux. The contours denote an  $H\alpha$ -derived star formation surface density of  $\Sigma_{\text{SF}} = 0.1 M_{\odot} \text{ yr}^{-1} \text{ kpc}^{-2}$ . The central two panels show the velocity field and line-of-sight velocity dispersion ( $\sigma$ ), respectively. The right-hand panel shows the residual velocity field after subtracting the best-fitting kinematic model. The rms of these residuals is given in each panel (for SHIZELS 4 and 12 there are too few resolution elements across the source to meaningfully attempt to fit disc models).

1996), the simplest model which provides a good fit to most rotation curves on  $\sim \text{kpc}$  scales is the arctan fit of the form  $v(r) = (2/\pi)v_{\text{asym}} \arctan(r/r_t)$ , where  $v_{\text{asym}}$  is the asymptotic rotational velocity and  $r_t$  is the effective radius at which the rotation curve turns over (Courteau 1997). To fit the two-dimensional velocity fields of the galaxies in our sample, we construct a two-dimensional kinematic model with six free parameters [ $v_{\text{asym}}$ ,  $r_t$ ,  $[x/y]$  centre, position angle (PA) and disc inclination] and use a genetic algorithm (Charbonneau 1995) to find the best model. During the fitting, we limit the parameter ranges to those allowed by the data (e.g. the  $[x/y]$  centre and turnover radius,  $r_t$ , must be within

the SINFONI field of view; the maximum circular velocity must be  $< 2 \times$  the maximum velocity seen in the data;  $\text{PA} = 0^\circ - 180^\circ$  and  $i = 0 - 90$ ). We then generate  $10^5$  models within random initial parameters between these ranges and find the lowest  $\chi^2_{\text{v}}$ . This process is repeated (up to 100 times), but in each new generation we remove (up to) 10 per cent of the worst fits and contract the remaining parameter space search by up to 5 per cent centred on the best fit. We examine whether the fit has converged by examining whether all of the models in a generation are within  $\Delta\chi^2 = 1$  of the best-fitting model. The errors on the final parameters (Table 3) reflect the range of acceptable models from *all* of the models attempted.

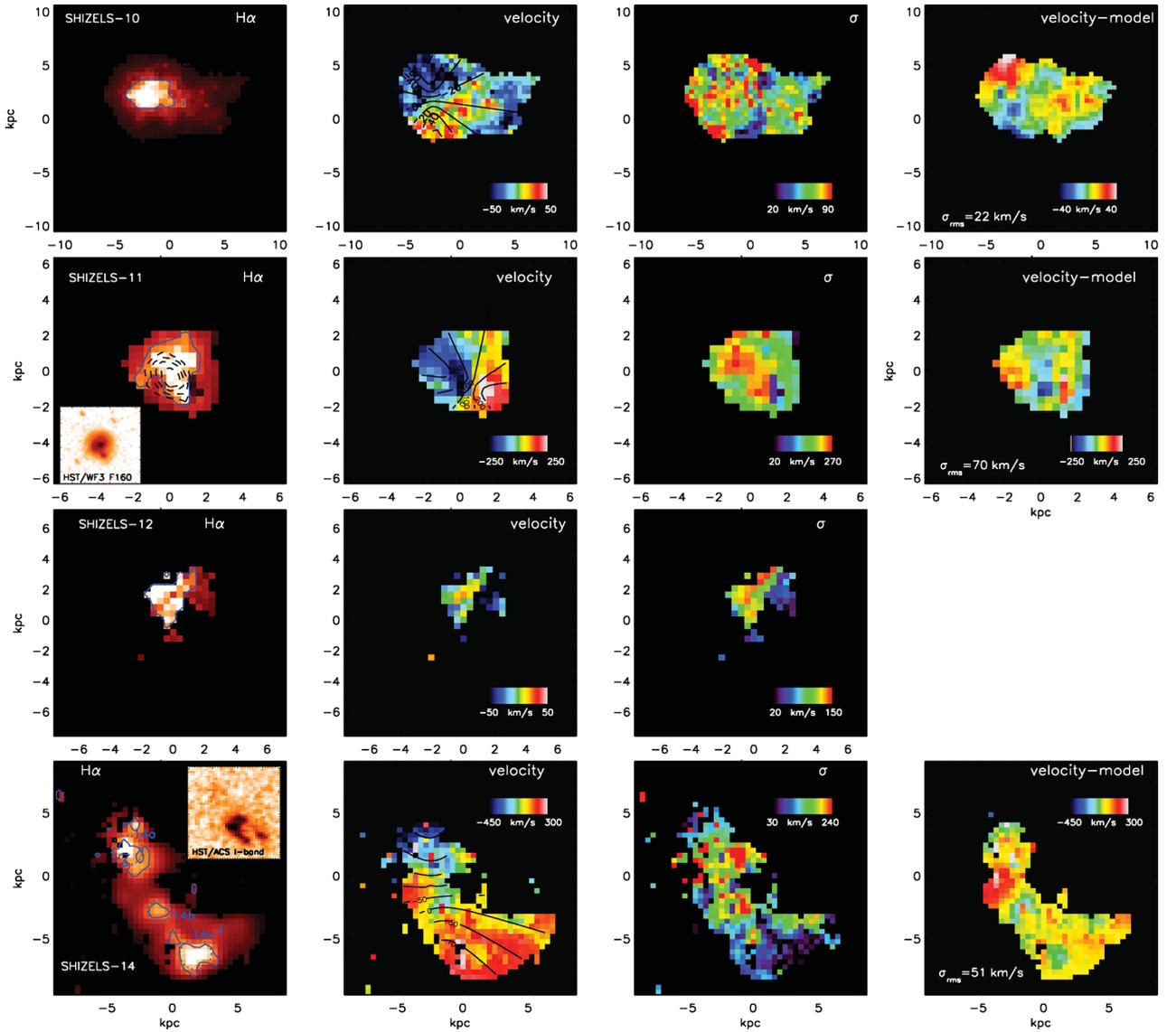


Figure 3 – continued

Table 3. Dynamical properties.

ID	$v_{\text{asym}}$ ( $\text{km/s}^{-1}$ )	$\sigma$ ( $\text{km/s}^{-1}$ )	$V_{2.2}$ ( $\text{km/s}^{-1}$ )	Inc ( $^{\circ}$ )	$K_v$	$K_{\sigma}$	$K_{\text{Tot}}$	$\chi_v^2$	Class
SHIZELS-1	$112 \pm 11$	$98 \pm 15$	$86 \pm 18$	40	$0.12 \pm 0.17$	$0.17 \pm 0.81$	$0.20 \pm 1.03$	4.8	D
SHIZELS-4	–	$77 \pm 20$	–	–	–	–	–	–	C
SHIZELS-7	$145 \pm 10$	$75 \pm 11$	$112 \pm 15$	33	$0.10 \pm 0.08$	$0.35 \pm 0.18$	$0.36 \pm 0.34$	3.1	D
SHIZELS-8	$160 \pm 12$	$69 \pm 10$	$144 \pm 17$	25	$0.20 \pm 0.15$	$0.30 \pm 0.25$	$0.36 \pm 0.40$	3.0	D
SHIZELS-9	$190 \pm 20$	$62 \pm 11$	$155 \pm 24$	54	$0.12 \pm 0.05$	$0.48 \pm 0.20$	$0.49 \pm 0.30$	5.7	D
SHIZELS-10	$30 \pm 12$	$64 \pm 8$	$26 \pm 12$	30	$0.13 \pm 0.05$	$0.83 \pm 0.14$	$0.84 \pm 0.35$	25.5	M
SHIZELS-11	$224 \pm 15$	$190 \pm 18$	$208 \pm 18$	25	$0.16 \pm 0.05$	$0.34 \pm 0.10$	$0.37 \pm 0.16$	5.34	D
SHIZELS-12	–	$115 \pm 10$	–	–	–	–	–	–	C
SHIZELS-14	–	$131 \pm 17$	$190 \pm 25$	58	$0.15 \pm 0.09$	$0.38 \pm 0.23$	$0.40 \pm 0.34$	9.1	M
Median	$147 \pm 31$	$75 \pm 19$	$133 \pm 30$	–	$0.13 \pm 0.01$	$0.37 \pm 0.07$	$0.38 \pm 0.04$	$5.3 \pm 3.0$	–

Note.  $v_{\text{asym}}$  and  $V_{2.2}$  are inclination corrected.  $\sigma$  is the average velocity dispersion across the galaxy image (and the velocity dispersion map has been corrected for ‘beam smearing’ effects due to the PSF, see Section 2.3). The classes in the final column denote disc (D), merger (M) and compact (C) (see Section 3).

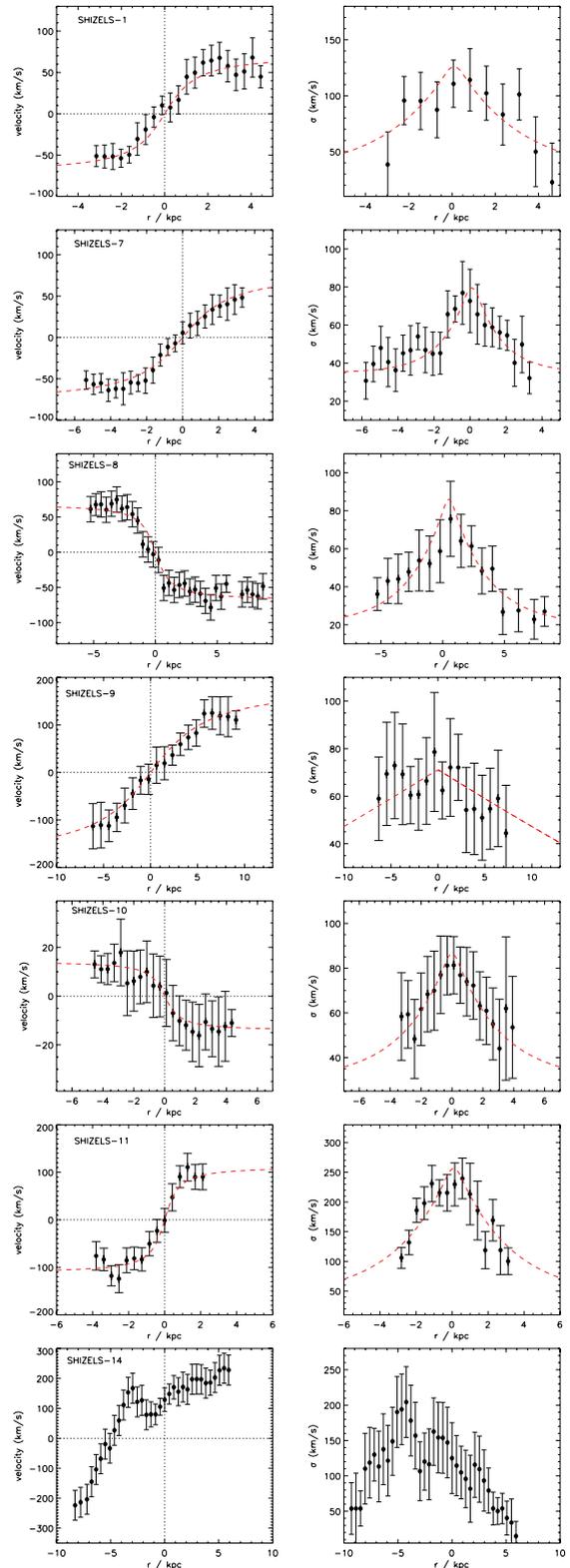
The best-fitting kinematic maps and velocity residuals are shown in Fig. 3, whilst the best-fitting inclinations and disc rotation speeds are given in Table 2, along with the  $\chi^2_v$ . All galaxies show small-scale deviations from the best-fitting model, as indicated by the typical rms,  $\langle \text{data} - \text{model} \rangle = 30 \pm 10 \text{ km s}^{-1}$ , with a range from 15 to  $70 \text{ km s}^{-1}$ . These offsets could be caused by the effects of gravitational instability, or simply due to the unrelaxed dynamical state indicated by the high-velocity dispersions ( $\sigma = 96 \pm 24 \text{ km s}^{-1}$ ). The goodness of fit and small-scale deviations from the best-fitting models are similar to those of 18 galaxies in the SINS survey which show the most prominent rotational support (rms of  $10\text{--}80 \text{ km s}^{-1}$  and  $\chi^2_v = 0.2\text{--}20$ ; Cresci et al. 2009), as well as to the high-resolution studies of gravitationally lensed galaxies from Jones et al. (2010b) and Stark et al. (2008) (which have an average  $\chi^2_v = 3.5 \pm 0.8$ ). We therefore conclude that the disc model provides an adequate fit to the majority of these galaxies and that the velocity fields of most galaxies are consistent with the kinematics of turbulent rotating discs.

We use the best-fitting dynamical model to identify the major kinematic axis, and extract the one-dimensional rotation curve and velocity dispersion profiles, and show these in Fig. 4. We define the zero-point in the velocity using the dynamical centre of the galaxy, whilst the error bars for the velocities are derived from the formal  $1\sigma$  uncertainty in the velocity arising from the Gaussian profile fits to the H $\alpha$  emission. We note that in the one-dimensional rotation curves in Fig. 4 alternate points show independent data. We also note that the data have not been folded about the zero velocity, so that the degree of symmetry can be assessed.

Whilst this modelling provides a useful test of whether the dynamics can be described by disc-like rotation, a better criterion for distinguishing between motion from disturbed kinematics is the ‘kinemetry’ which measures the asymmetry of the velocity field and line-of-sight velocity dispersion maps for each galaxy. This technique has been well calibrated and tested at low redshift (e.g. Krajnović et al. 2006), whilst at high redshift it has been used to determine the strength of deviations of the observed velocity and dispersion maps from an ideal rotating disc (Shapiro et al. 2008). In this modelling, the velocity and velocity dispersion maps are described by a series of concentric ellipses of increasing semi-major axis length, as defined by the system centre, PA and inclination. Along each ellipse, the moment map as a function of angle is extracted and decomposed into its Fourier series which have coefficients  $k_n$  at each radii (see Krajnović et al. 2006 for more details).

In a noiseless, idealized disc, the coefficients of the Fourier expansion would be zero. Any deviations from the ideal case that occur in a disturbed disc (e.g. warps, spiral structures, streaming motions or mergers in the extreme cases) induce strong variations in the higher order Fourier coefficients. To ensure that reliable measurements of the kinemetry parameters can be made, we first construct a grid of 2000 model discs and mergers with noise and spatial resolution appropriate for our SINFONI observations. For the model discs, we allow disc scale lengths and rotation curve turnover lengths ( $r_t$ ) from 0.5 to 3 kpc, rotation speeds and peak velocity dispersions from 10 to  $300 \text{ km s}^{-1}$  and random inclinations and sky PAs. The model mergers typically comprise 2–3 of these galaxy-scale components separated by 1–20 kpc in projection. The dynamics of each of these components randomly ranges from dispersion-dominated to rotating systems.

We then use the kinemetry code from Krajnović et al. (2006) and measure the velocity and velocity dispersion asymmetry for all of these models. Following Shapiro et al. (2008), we define the velocity asymmetry ( $K_v$ ) as the average of the  $k_n$  coefficients with  $n = 2\text{--}5$ ,



**Figure 4.** Left: one-dimensional rotation curves for the seven galaxies in our sample which show strong velocity gradients in their H $\alpha$  dynamics. For the six galaxies whose dynamics resemble rotating systems, we overlay the best-fitting one-dimensional rotation curve. Right: one-dimensional velocity dispersion profiles with the best-fitting line-of-sight profile overlaid for the rotating systems. The observed rotation curve and line-of-sight velocity dispersion are extracted from the two-dimensional velocity fields using a 1 kpc width slit across the major kinematic axis of each galaxy.

normalized to the first cosine term in the Fourier series (which represents circular motion); and the velocity dispersion asymmetry ( $K_\sigma$ ) as the average of the first five coefficients ( $n = 1-5$ ) also normalized to the first cosine term. For an ideal disc,  $K_v$  and  $K_\sigma$  will be zero. In a merging system, strong deviations from the idealized case causes large  $K_v$  and  $K_\sigma$  values, which can reach  $K_v \sim K_\sigma \sim 10$  for very disturbed systems. The total asymmetry,  $K_{\text{Tot}}$  is  $K_{\text{Tot}}^2 = K_v^2 + K_\sigma^2$ . For our mock sample of model discs, we recover  $K_{\text{Tot,disc}} = 0.30 \pm 0.03$  compared to  $K_{\text{Tot,merger}} = 2 \pm 1$  for the mergers.

For the SHiZELS galaxies in our sample, we measure the velocity and velocity dispersion asymmetry (SHiZELS 4 and 12 have too few independent spatial resolution elements across the galaxy so we omit these from the kinemetry analysis). Krajnović et al. (2006) show that an incorrect choice of centre induces artificial power in the derived kinemetry coefficients. We therefore allow the dynamical centre to vary over the range allowed by the family of best-fitting two-dimensional models and measure the kinemetry in each case. We also perturb the velocity and dispersion maps by the errors on each pixel and remeasure the asymmetry, reporting the velocity and dispersion asymmetries ( $K_v$  and  $K_\sigma$ , respectively) along with their errors in Table 3. We use the total asymmetry,  $K_{\text{Tot}}$ , to differentiate discs ( $K_{\text{Tot}} < 0.5$ ) from mergers ( $K_{\text{Tot}} > 0.5$ ). For the galaxies in our sample, five are classified as discs (D), whilst two more indicate mergers (M) and the final two are compact (C).

As expected, the two galaxies that are classified as mergers from the kinemetry (SHiZELS 10 and 14) have the highest  $\chi_v^2$  ( $\chi_v^2 > 9$ ) from the dynamical modelling. Both of these systems are noteworthy; the one-dimensional rotation curve of SHiZELS 10 (extracted from the major kinematic axis) appears regular and suggests rotation, but the two-dimensional velocity field reveals extended ( $\sim 5$  kpc) emission to the east, which may be due to a companion or tidal material. The dynamics of the other galaxy classified as a merger, SHiZELS 14, are clearly more complex. The H $\alpha$  is extended across  $\sim 14$  kpc with a peak-to-peak velocity gradient of  $\sim 480 \pm 40$  km s $^{-1}$ . Qualitatively, the one- and two-dimensional velocity fields of SHiZELS 14 are consistent with an early stage prograde encounter, with each component in the merger displaying approximately equal peak-to-peak velocity gradients. The northernmost component is also more highly obscured than the southern component (as evident from the *HST* I-band imaging; Fig. 3).

Overall, the fraction of rotating systems within our sample,  $\sim 55$  per cent, is consistent with that found from other H $\alpha$  IFU surveys of high-redshift star-forming galaxies (e.g. Förster Schreiber et al. 2009; Jones et al. 2010b; Wisnioski et al. 2011).

### 3.1 The Tully–Fisher relation

Since our two-dimensional dynamical data resolve the turnover in the rotation curves (as evident from Fig. 4), we can use our results to investigate how the disc scaling relations for the galaxies in our sample compare to galaxy discs at  $z = 0$ . The relation between the rest-frame *B*-band luminosity ( $M_B$ ) and rotational velocity and that between the total stellar mass ( $M_*$ ) and rotational velocity define the Tully–Fisher relations (Tully & Fisher 1977). The first of these relations has a strong contribution from the short-term star formation activity whilst the second provides a better proxy for the integrated star formation history. Indeed the latter relationship may reflect how rotationally supported galaxies formed, perhaps suggesting the presence of self-regulating processes for star formation in galactic discs. The slope, intercept and scatter of the Tully–Fisher relations and their evolution are therefore key parameters that any successful galaxy formation model must reproduce (e.g. Cole & Kaiser 1989;

Kauffmann, White & Guiderdoni 1993; Cole et al. 1994; Eisenstein & Loeb 1996; Somerville & Primack 1999; Steinmetz & Navarro 1999; Portinari & Sommer-Larsen 2007; Dutton et al. 2011).

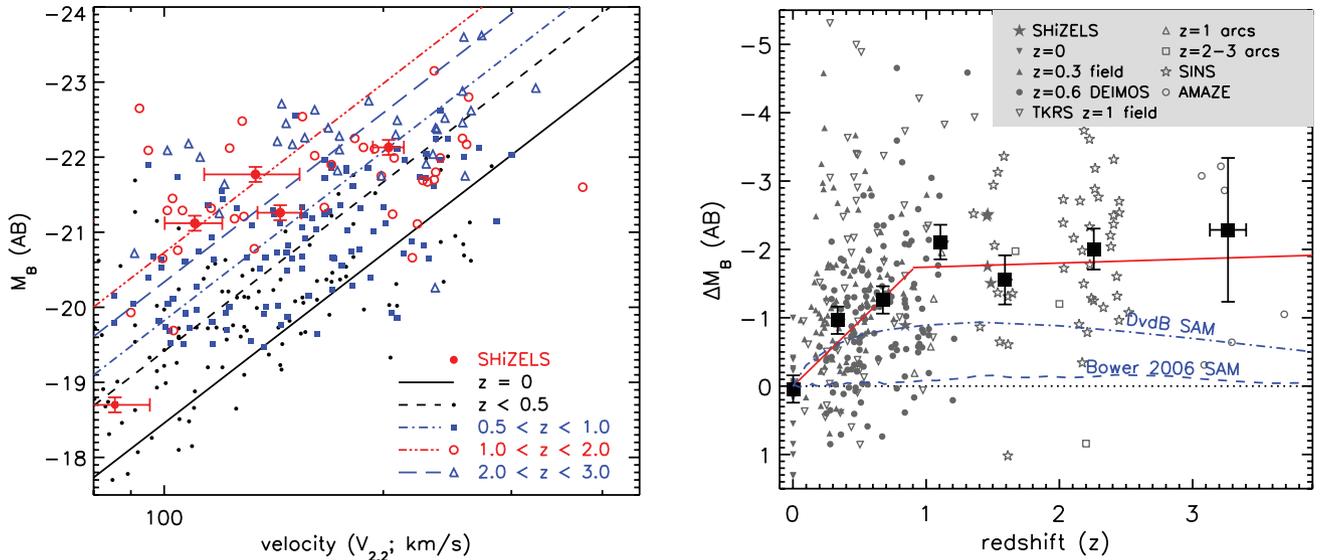
Since we wish to compare our dynamical measurements with those of other high-redshift galaxies where similar data exist, it is important to measure the rotational velocity in a consistent manner. Whilst the *arctan* function is useful for describing the overall shape of the rotation curve (in both one- and two-dimensional data), it provides an extrapolation of the rotational velocity, which may not be warranted especially if the rotation curve does not flatten in the data. Equally, since any measurement of the observed peak-to-peak rotational velocity ( $V_{\text{max}}$ ) is sensitive to the radius at which it has been possible to detect the dynamics, this measurement varies from both object to object depending on both the extent of the galaxy and S/N of the observations and can therefore give biased measurements when comparing samples.

A more robust measurement is that of the velocity at 2.2 times the disc scale length ( $V_{2.2}$ ). This has a better physical basis since it measures the peak rotational velocity for a pure exponential disc (Freeman 1970; Courteau & Rix 1997) and provides the closest match to the radio (21-cm) line widths for local galaxies (Courteau 1997). Of course, the light profile of high-redshift galaxies is unlikely to follow pure exponential disc profiles, but it provides a reasonable estimate of where the rotation curve flattens, and as we will see below, is a good approximation of both  $V_{\text{max}}$  and  $V_{\text{asym}}$  in our data. To measure  $V_{2.2}$  in our data, we therefore measure the H $\alpha$  intensity as a function of radius in our galaxies (centred at the dynamical centre and using the inclination and PA set by the best-fitting two-dimensional kinematic model) and infer the disc scale length (which ranges from 0.7 to 2.7 kpc and has a median of  $1.8 \pm 0.7$  kpc). We then measure the rotational velocity at 2.2 disc scale lengths and report these in Table 3. The errors on these quantities are derived from both the errors on the observed velocity at this radius and the formal errors on the two-dimensional model velocity fields. For reference, we note that owing to the high resolution and S/N of our data, we have been able to resolve the flattening in the rotation curves, the ratio of the maximum (observed) peak-to-peak velocity ( $V_{\text{max}}$ ) to  $V_{2.2}$  in our sample is  $V_{\text{max}}/V_{2.2} = 0.93 \pm 0.05$  whilst the ratio of asymptotic velocity ( $V_{\text{asym}}$ ) to  $V_{2.2}$  is  $V_{\text{asym}}/V_{2.2} = 1.25 \pm 0.08$ .

#### 3.1.1 *B*-band Tully–Fisher relation

In Fig. 5, we show the  $z = 0$  Tully–Fisher relation from Tully & Fisher (1977) and overlay the  $z = 0.84-2.23$  measurements from our sample (using  $V_{2.2}$  as the preferred measure of rotational velocity). We also include the field sample ( $\langle z \rangle = 0.33$ ) from Bamford et al. (2005), the  $z \sim 1$  field samples from Miller et al. (2011) and Weiner et al. (2006), the  $z = 1-3$  lensed samples from Swinbank et al. (2006) and Jones et al. (2010b) and the  $z \sim 2$  and  $z \sim 3$  star-forming galaxies from Förster Schreiber et al. (2009) and Gnerucci et al. (2011), respectively.

It is clear from Fig. 5 that the  $z = 0$  *B*-band Tully–Fisher relation provides a poor fit to high-redshift data, with most of the high-redshift galaxies lying above the local relation. Since the high-redshift sample represents a heterogeneous mix of populations, all with different and complex selection functions, we limit our search for the evolution in the Tully–Fisher to its zero-point only. We therefore fix the slope to the  $z = 0$  relation and in each of the seven redshift bins from  $z = 0.0$  to 3 we derive the zero-point offset using a non-linear least-squares regression (weighted by the velocity errors in each galaxy) and show these results in Fig. 5.



**Figure 5.** Left: the evolution of the rest-frame  $B$ -band Tully–Fisher relation. We baseline our results against the  $z=0$  measurements from Pierce & Tully (1992). For the high-redshift samples, we combine the observations from this work with a number of other surveys. At  $z \sim 0.1$ –1 we include the field surveys from Bamford et al. (2005) ( $z=0.3$  field), Weiner et al. (2006) (Team Keck Treasury Redshift Survey; TKRS  $z=1$  field) and Miller et al. (2011) ( $z=0.6$  DEIMOS). At  $z \gtrsim 1$  we include the cluster arc surveys of Swinbank et al. (2006) ( $z=1$  arcs) and Jones et al. (2010b) ( $z=2$ –3 arcs) and at  $z \gtrsim 2$  we include the SINS and AMAZE surveys (Förster Schreiber et al. 2009; Gnerucci et al. 2011). The solid line denotes the  $z=0$   $B$ -band Tully–Fisher relation from Pierce & Tully (1992). Right: the evolution of the zero-point of the  $B$ -band Tully–Fisher relation. The open symbols denote individual galaxies and the solid points show the median (and error) in seven redshift bins between  $z=0$  and 3. The curves show the predictions of the evolution of the  $B$ -band Tully–Fisher relation from semi-analytic models by Bower et al. (2006) and Dutton et al. (2011) which both predict the evolution of  $\Delta M_B < 1$  mag between  $z=0$  and 3, less than seen in the observations.

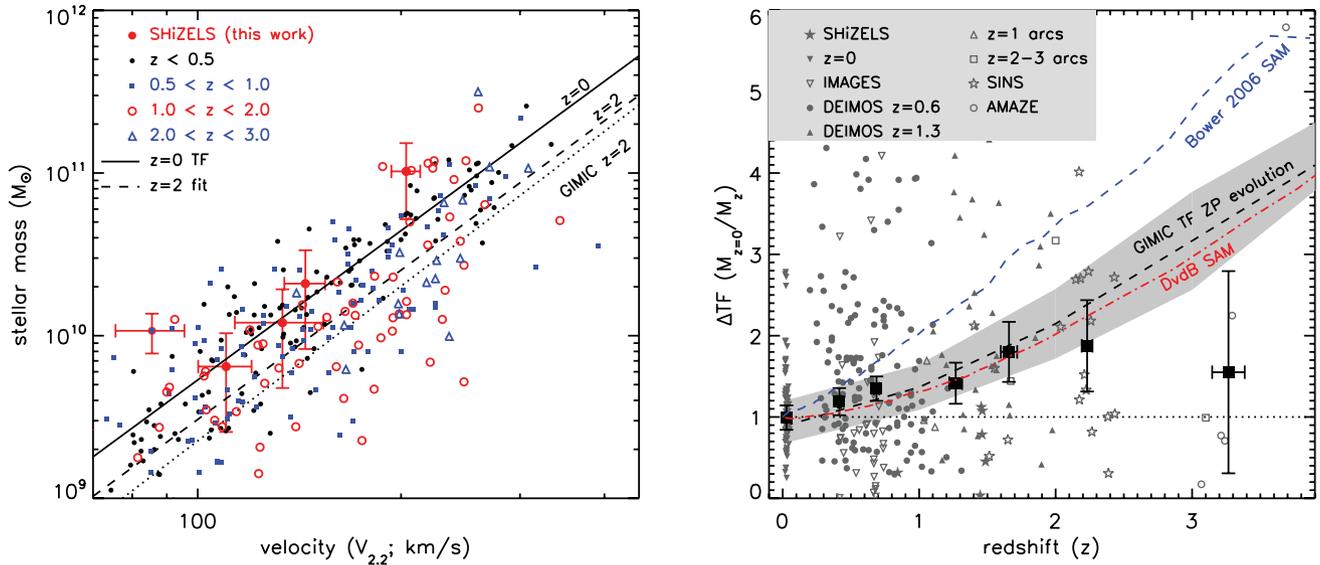
For a fixed slope, the strongest evolution occurs between  $z=0$  and 1, and in this range the zero-point evolution follows  $\Delta M_B(\text{mag}) = (-1.9 \pm 0.3)z$  up to  $z \sim 1$  and then significantly flattens above  $z=1$  to  $\Delta M_B(\text{mag}) = (-0.06 \pm 0.25)z - (1.68 \pm 0.25)$  up to  $z \sim 3$ . Since the rest-frame  $B$  band is dominated by recent star formation activity, the strong evolution in the rest-frame  $B$ -band Tully–Fisher zero-point between  $z=0$  and 1 (2 mag or a factor of  $\sim 6$  in luminosity) and then flattening to  $z \sim 3$ , is consistent with the evolution of the star formation volume density with redshift (Hopkins & Beacom 2006).

We can compare this evolution to galaxy formation models, and in Fig. 5 we also overlay the predicted zero-point offset from the semi-analytic models from Dutton et al. (2011) and Bower et al. (2006). The Dutton et al. (2011) semi-analytic models suggest that for a fixed circular velocity, the luminosity of a galaxy at  $z \sim 1$  should be a factor up to  $\sim 2.5\times$  higher than today (Dutton et al. 2011), although the data are suggestive of markedly stronger evolution than predicted by the models  $z \sim 1$ . In contrast, the predictions from the Bower et al. (2006) model predict very little evolution in the  $B$ -band Tully–Fisher relation ( $\Delta M_B < 0.2$  mag between  $z=0$  and 4). In this model, the apparent lack of evolution in the  $B$ -band Tully–Fisher relation in the galaxy formation models occurs because the specific star formation rate evolves rapidly with both mass and redshift. Although the model approximately matches the evolution of the star formation rate density with redshift, this is offset by an increase in the specific star formation rate in low-mass galaxies. Moreover, since the dark haloes are more concentrated at high redshift, a fixed  $v_{\text{circ}}$  does not select the same mass halo at the two epochs (for a fixed  $v_{\text{circ}}$ , a halo at  $z=0$  is a factor of  $\sim 1.7$  more massive than at  $z=2$ ). This combination of the evolution of the specific star formation rate with mass and redshift, and the evolution in the halo densities for a fixed  $v_{\text{circ}}$  approximately cancel to predict that there should be very little evolution in the  $B$ -band Tully–Fisher relation.

### 3.1.2 The stellar-mass Tully–Fisher relation

The rest-frame  $B$ -band Tully–Fisher relation is sensitive to recent star formation, and so perhaps the more fundamental relation is the stellar-mass Tully–Fisher relation ( $M_*$  versus  $v_{\text{asym}}$ ) which reflects the time-integrated star formation history. The  $z=0$  stellar-mass Tully–Fisher relation is well established (Bell & de Jong 2001; Pizagno et al. 2007; Meyer et al. 2008), and in Fig. 6 we combine the stellar-mass estimates with the inclination-corrected rotation speed of our galaxies to investigate how this varies as a function of redshift. Again, in this plot, we also include a number of high-redshift measurements; at  $z \sim 0.6$  and  $z \sim 1.3$  from Miller et al. (2011, 2012), the  $z=1$ –3 lensed galaxy surveys (Swinbank et al. 2006; Jones et al. 2010b; Richard et al. 2011) as well as the  $z \sim 2$  SINS and  $z > 3$  SINFONI IFU surveys (Cresci et al. 2009; Gnerucci et al. 2011). Where necessary, we have corrected the samples to use  $V_{2,2}$  using  $V_{2,2}/V_{\text{max}} = 0.93$  if only  $V_{\text{max}}$  is given in the literature (see also Dutton et al. 2007).

In comparison to the rest-frame  $B$ -band Tully–Fisher relation, Fig. 6 shows that the redshift evolution in the stellar-mass Tully–Fisher relation is weak. Due to the heterogeneous selection functions of these various surveys, we again restrict the search to the evolution in the zero-point with redshift. We therefore construct the same seven redshift bins from  $z=0$  to 3 as in Section 3.1.1 and measure the zero-point offset in each bin (using a non-linear least-squares regression weighted by the velocity errors in each galaxy; Fig. 6). The data suggest that the zero-point offset from  $z=2.5$  to 0 is  $\Delta M_{*,z=0}/M_* = 2.0 \pm 0.4$  (i.e. at a fixed circular velocity the stellar mass of galaxies has increased by a factor of  $\sim 2.0$  between  $z=2.5$  and 0). The weak evolution in the stellar-mass Tully–Fisher relation (in particular below  $z \sim 1$ ) is due to the fact that individual galaxies evolve roughly along the scaling relation rather than due to weak evolution in the galaxies themselves (e.g. Portinari &



**Figure 6.** Left: the evolution of the stellar-mass Tully–Fisher relation. We baseline the evolution against the  $z=0$  work from Pizagno et al. (2005). The high-redshift points are compiled from the intermediate- and high-redshift ( $z \sim 0.6$  DEIMOS and  $z \sim 1.3$  DEIMOS) observations from Miller et al. (2011, 2012) the  $z=1$  and  $z=2-3$  cluster arc surveys from Swinbank et al. (2006) and Jones et al. (2010b) with stellar masses from Richard et al. (2011); and the  $z \sim 2-3.5$  SINS and AMAZE surveys from Cresci et al. (2009) and Gnerucci et al. (2011). The symbols show individual galaxies. The solid line denotes the correlation at  $z=0$  from Pizagno et al. (2005) (corrected to a Chabrier IMF). The dashed line is best-fitting zero-point to the  $z=2$  sample galaxies (for a fixed  $v_{2,2}$ ) which shows an offset of  $\Delta M_{*,z=0}/M_* = 2.0 \pm 0.4$  between  $z=0$  and 2.5. The dotted lines denote the Tully–Fisher at  $z=2$  from the numerical simulations from Crain et al. (2009) (see also McCarthy et al. 2012), which predict evolution in both the zero-point and slope. Here, we concentrate on the zero-point evolution, and note that the predicted evolution for a disc with circular velocity of  $100-200 \text{ km s}^{-1}$  is an increase in stellar mass by a factor 1.5–3 between  $z=2$  and 0 (equivalently, at high redshift the maximum circular velocity is greater for the same stellar mass which may be consistent with the galaxies being compact at high redshift and larger at low redshift). Right: the evolution of the zero-point of the Tully–Fisher relation. The symbols denote individual points (coded by the survey), whilst the solid symbols denote the average in six redshift bins. We also overlay the redshift evolution of the zero-point of the Tully–Fisher relation from the numerical model from Crain et al. (2009) as well as the semi-analytic models from Bower et al. (2006) and Dutton et al. (2011) (DvdB). These galaxy formation models predict evolution in the zero-point of the Tully–Fisher relation out to  $z \sim 3$  which is consistent with the observed trend given the large uncertainties in the latter.

Sommer-Larsen 2007; Brooks et al. 2011). This indicates that the baryon conversion efficiency,  $\eta = (M_*/M_{200})/(\Omega_b/\Omega_0)$ , is fixed with redshift.

In Fig. 6 we also compare the zero-point evolution in the Tully–Fisher relation to that from semi-analytic models from Bower et al. (2006) and Dutton et al. (2011) and the cosmological hydrodynamic Galaxies–Intergalactic Medium Interaction Calculation (GIMIC; Crain et al. 2009). The Bower et al. (2006) and GIMIC simulations both use the same underlying dark matter distribution, although the GIMIC simulation follows the hydrodynamical evolution of gas, radiative cooling, star formation and chemodynamics, and includes a prescription for energetic feedback from supernovae. In contrast to simulations of small periodic volumes, GIMICs unique initial conditions enable it to follow, at high resolution, cosmologically representative volumes to  $z=0$  (see Crain et al. 2009; McCarthy et al. 2012). To search for evolution in the Tully–Fisher zero-point in the simulations, we only consider galaxies with star formation rates  $> 1 M_{\odot} \text{ yr}^{-1}$  (at all redshifts) so that a reasonable comparison to observational data can be made. Both the semi-analytic and hydrodynamic simulations shown in Fig. 6 predict strong evolution, with the GIMIC simulation suggesting that, at a fixed circular velocity the stellar mass of galaxies should increase by  $2.5 \pm 0.5$  times between  $z=2$  and 0. This evolution is matched by the semi-analytic model from Dutton et al. (2011). However, the semi-analytic model from Bower et al. (2006) predicts somewhat stronger evolution in the stellar mass for a fixed circular velocity.

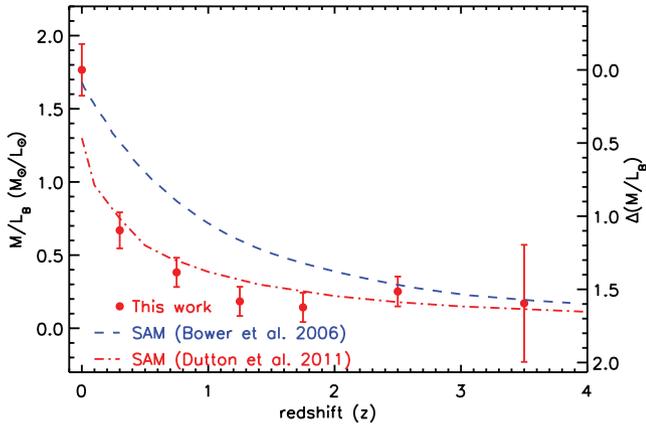
It is interesting to note that the GIMIC simulation predicts that the scatter in the Tully–Fisher relation should not evolve strongly

with redshift (for a fixed circular velocity, the scatter is  $25 \pm 5$  per cent over the redshift range  $z=0-3$ ). Our dynamical measurements, particularly when combined with those from Weiner et al. (2006) and Miller et al. (2012), are sufficiently large in number to compare to the models, and Fig. 6 shows that the scatter in the observations is consistent with the models (for all but the last bin in redshift where the number of data points is  $< 8$ ), suggesting that the samples may now be sufficiently large (with rotation curves well enough sampled) that the scatter is intrinsic.

### 3.2 The redshift evolution of the mass-to-light ratio

Another route to examine the evolution in the  $B$ -band and stellar-mass Tully–Fisher relations is to combine the offsets and measure the evolution of the mean mass-to-light ratio with redshift. We caution that the conversion of zero-point offsets to offsets in mass-to-light assumes that star-forming galaxies form a homologous family and that the evolution is a manifestation of underlying relations between mass-to-light ratio and other parameters, such as star formation history, gas accretion and stellar feedback.

Under these assumptions, in Fig. 7 we show the evolution of the rest-frame  $B$ -band mass-to-light ratio. As expected from the zero-point Tully–Fisher offsets, this figure shows that the average mass-to-light ratio of star-forming galaxies decreases strongly from  $z=0$  to 1 and then flattens. This behaviour is consistent with the previous demonstration that star-forming galaxies at high redshift have lower stellar masses and higher  $B$ -band luminosities. The strongest evolution occurs up to  $z \sim 1$ ,  $\Delta M_*/L_B = 1.1 \pm 0.2$ , consistent with



**Figure 7.** The  $B$ -band mass-to-light ratio as a function of redshift for star-forming galaxies from this work plus the compilation of studies shown in Figs 5 and 6. The dashed and dot-dashed lines show the predicted evolution of the mass-to-light ratio as a function of redshift from the Bower et al. (2006) and Dutton et al. (2011) semi-analytic models. This figure shows that in both the observations and galaxy formation models there is strong evolution in the mass-to-light ratio of galaxies with redshift. The strongest evolution in the data is seen for  $z=0-1$ , with significant flattening above  $z=1$ .

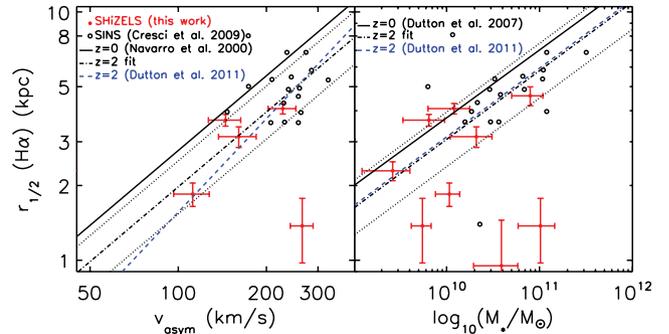
previous studies (Miller et al. 2011) [the fractional change in the mass-to-light ratio over this period is  $\Delta(M/L_B)/(M/L_B)_{z=0} \sim 3.5$  between  $z=1.5$  and 0, with most of the evolution occurring below  $z=1$ ].

We note that we examined whether the evolution in the mass-to-light ratio could be reproduced using simple star formation histories, ranging from (i) a constant star formation rate (with a formation redshift,  $z_f = 4-8$ ) or (ii) a set of exponentially decreasing star formation rates with e-folding times ranging from 0.25 to 10 Gyr (and formation redshifts ranging from  $z_f = 2$  to 10). However, using these simple star formation histories (adopting a Chabrier IMF with 0.5–1 solar metallicities and the Padova 1994 stellar evolution tracks), we are unable to find an acceptable fit with a single star formation history. This could be because the ‘average’ star formation history is more complex than a simple star formation model, or because the current low- and high-redshift data cannot be linked by a simple evolutionary model. However, in Fig. 7 we also overlay the predicted evolution of the  $B$ -band mass-to-light ratio from the semi-analytic models of Bower et al. (2006) and Dutton et al. (2011), both of which predict a sharp decline to  $z \sim 1$  and then flattening to higher redshift, which provides a reasonable match to the observations.

### 3.3 The evolution of the size–rotational velocity relation

In a  $\Lambda$  cold dark matter cosmology, the sizes of galaxy discs and their rotational velocities should be proportional to their parent dark haloes, and since the haloes are denser at higher redshift, for fixed circular velocity the disc sizes should scale inversely with Hubble time (Mo et al. 1998). In this scenario, discs at  $z=1$  and 2 should be 1.8 and 3.0 times smaller, respectively, at fixed circular velocity. With the high-resolution measurements for the galaxies in our sample we can measure the extent of the  $H\alpha$  (and together with the dynamics) and compare these relations at  $z \sim 1.5$  to star-forming discs at  $z=0$ .

In Fig. 8, we show the relation between the  $H\alpha$  half-light radius and rotational velocity for the galaxies in our sample (using the asymptotic velocity as measured from the disc modelling). In this



**Figure 8.** Left: the relation between the circular velocity and  $H\alpha$  half-light radius for high-redshift galaxies. We include the results from the SHIZELS galaxies in our sample as well as those from SINS (Cresci et al. 2009). The solid line shows the  $z=0$  relation from Navarro & Steinmetz (2000) (which is based on a compilation from Mathewson et al. 1992; Courteau 1997). Fitting the local relation (assuming a fixed slope) to the high-redshift points suggests an offset  $\Delta r_{1/2}/r_{1/2,z=0} = 1.4 \pm 0.3$ , which is shown by the dot-dashed line (the scatter is shown by the dotted lines). This evolution is consistent with that predicted by halo–disc scaling arguments (e.g. Dutton et al. 2011; blue dashed line). Right: the relation between stellar mass and half-light radius in the SHIZELS and SINS surveys. The solid line shows the  $z=0$  relation from Dutton et al. (2011) whilst the dot-dashed curve shows the offset of the high-redshift measurements from the local relation (assuming a fixed slope), which shows a  $\Delta r_{1/2}/r_{1/2} = 1.2 \pm 0.3$  offset for a fixed stellar mass. We also show the predicted evolution of  $z=2$  galaxies from the  $z=0$  relation from the Dutton et al. (2011) semi-analytic model.

plot, we also include the measurements from the SINS galaxies from Cresci et al. (2009). First, we note that the  $H\alpha$  half-light radii for the SHIZELS galaxies ( $r_{1/2} = 2.4 \pm 0.8$  kpc) are comparable to the average rest-frame UV/optical half-light radii of star-forming galaxies at this redshift (e.g. Conselice et al. 2003; Law et al. 2007; Swinbank et al. 2010).

In order to compare to  $z=0$  data, we show the measurements of local discs from Navarro & Steinmetz (2000) (which is based on a compilation from Mathewson, Ford & Buchhorn 1992; Courteau 1997), but converting the disc scale length ( $r_d$ ) to half-light radius using  $r_{1/2} = 1.68 r_d$ , as appropriate for a disc with an exponential profile. As can be seen from this figure, the high-redshift galaxies have half-light sizes (deconvolved for seeing) which are smaller for fixed circular velocity than those at  $z=0$ . Fitting the local  $z=0$  relation to the high-redshift data (only allowing a zero-point shift and inverse weighting the fit by the errors on each data point) suggests that this offset is a factor of  $\Delta r_{1/2}/r_{1/2,z=0} = 1.4 \pm 0.3$ , which is consistent (given the smaller number statistics in the high-redshift measurements) with that predicted from halo–disc scaling arguments (Mo et al. 1998; see also Dutton et al. 2011).

The product of the rotational velocity and size of the disc defines the specific angular momentum, and the evolution (at a fixed circular velocity) with redshift also encodes information on the relation between the star formation processes in the disc and the halo spin parameters (e.g. Navarro & Steinmetz 2000; Tonini, Lapi & Salucci 2006). The offsets seen in the  $r_{1/2}-v_{\text{asym}}$  relation compared to local scaling relations in Fig. 8 translate directly into offsets in the specific angular momentum for discs between  $z=0$  and  $z \sim 2$ . Indeed, the offsets in  $r_{1/2}-v_{\text{asym}}$  suggest that, for fixed circular velocity, the specific angular momentum of discs at  $z=2$  is a factor of  $1.4 \pm 0.3$  lower than those at  $z=0$  (Navarro & Steinmetz 2000). Thus, if high-redshift discs evolve into local disc galaxies, then the specific angular momentum must be increased, either by removing material with low specific angular momentum through outflows, or

the galaxy disc must decouple from the halo and acquire angular momentum from accreting gas.

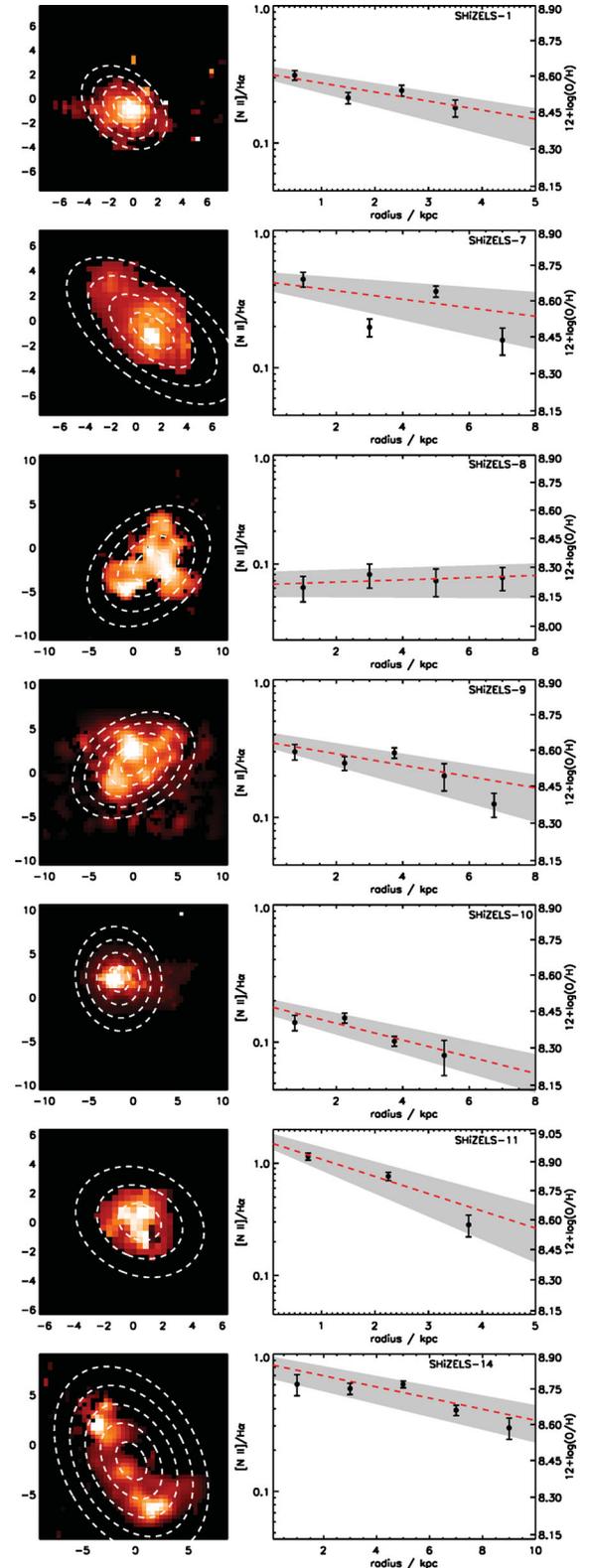
Finally, in Fig. 8 we also show the relation between stellar mass and  $H\alpha$  half-light radius for the galaxies in our sample compared to the  $z=0$  relation from Dutton et al. (2007). The high-redshift galaxies are offset from the local relation by  $\Delta r_{\text{th}}/r_{\text{h}} = 1.2 \pm 0.3$  for a fixed stellar mass. Although this is consistent with no evolution, we note that the predicted evolution for a fixed stellar mass between  $z=0$  and 2 from the semi-analytic model from Dutton et al. (2011) is  $\Delta r_{\text{th}}/r_{\text{h}} = 1.2$ .

### 3.4 Metallicities and spatially resolved chemical abundances

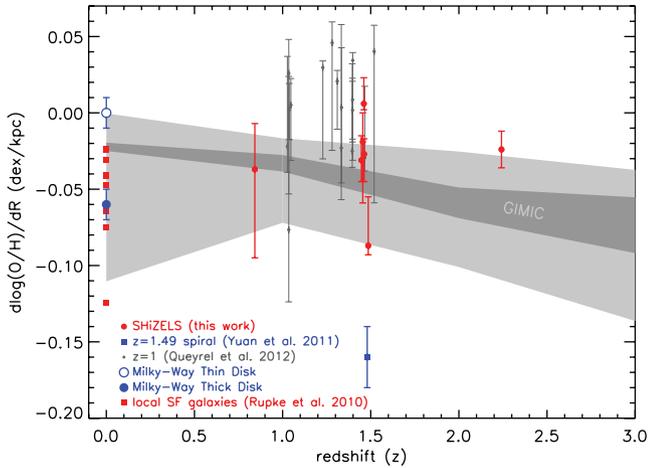
The internal enrichment (and radial abundance gradients) of high-redshift star-forming galaxies provides a tool for studying the gas accretion and mass assembly process such as gas exchange (inflows/outflows) with the IGM. However, the small sizes of high-redshift galaxies (typically  $r_{\text{h}} \sim 2\text{--}3$  kpc; e.g. Law et al. 2007; Smail et al. 2007; Conselice, Rajgor & Myers 2008; Swinbank et al. 2010) mean that sub-kpc resolution observations are required to measure the abundances reliably. At high redshifts the gas-phase metallicity of individual galaxies can only be measured with limited accuracy, usually through the  $[\text{N II}]/H\alpha$  emission-line ratio as an indicator of oxygen abundance and calibrations between gas-phase emission line and stellar absorption metallicities, such as those obtained by Pettini & Pagel (2004). Recently, the first reliable spatially resolved measurements of  $[\text{N II}]/H\alpha$  have been made in two highly amplified galaxies at  $z \sim 1.5\text{--}2.5$ , measuring strong, negative gradients and suggesting that if  $z \sim 2$  starbursts evolve into spiral discs today, then the gradients must flatten by  $\Delta \log(\text{O}/\text{H})/\Delta R \sim 0.05\text{--}0.1$  dex kpc over the last 8–10 Gyr (Jones et al. 2010a; Yuan et al. 2011). Other studies at lower resolution have derived weaker gradients that are negative, or consistent with zero for rotating and interacting galaxies (Cresci et al. 2010; Queyrel et al. 2012). Positive gradients for interacting systems may act as a signature of the redistribution of the metal-rich gas produced from a central starburst (Rupke, Kewley & Chien 2010; Werk et al. 2010), or possibly as a result of inflow of relatively unenriched gas from the halo (or IGM) if it is able to intersect the central regions of the disc galaxy without being disrupted.

With our high-resolution (and high S/N) resolved observations we can measure the spatially resolved emission-line ratios and hence the distribution of chemical abundances. First, we note that the average galaxy-integrated  $[\text{N II}]/H\alpha$  ratio for the galaxies in our sample is  $[\text{N II}]/H\alpha = 0.27 \pm 0.09$ , which corresponds to  $12 + \log(\text{O}/\text{H}) = 8.58 \pm 0.07$  (equivalently,  $\sim 0.73 \pm 0.16 Z_{\odot}$ , where  $Z_{\odot}$  is  $12 + \log(\text{O}/\text{H}) = 8.66 \pm 0.05$ ; Asplund et al. 2004). We caution that the  $[\text{N II}]/H\alpha$  ratio is sensitive to shock excitation, the ionization state of the gas, and the hard ionization radiation field from an AGN (Kewley & Dopita 2002; Kewley et al. 2006; Rich et al. 2010). However, our galaxy-integrated  $[\text{N II}]/H\alpha$  ratios are consistent with star formation throughout the disc (Fig. 2).

Of the nine galaxies in our high-redshift sample, seven have  $[\text{N II}]\lambda 6583$  emission which is sufficiently strong ( $S/N > 10$  in the combined spectra) to allow spatially resolved studies of the chemical abundance gradients. First, we subtract the large-scale velocity motions from the data cube (as defined by the best-fitting dynamical model). We then use the disc inclination and PA to define  $\sim 1$  kpc annuli (centred at the dynamical centre) and integrate the spectrum in each annulus to measure the  $[\text{N II}]/H\alpha$  ratio. In Fig. 9, we show the  $H\alpha$  emission-line maps as well as the spatially resolved  $[\text{N II}]/H\alpha$  ratio and overlay the best-fitting linear regression in each case. We



**Figure 9.** Metallicity gradients for the seven galaxies in our sample where spatially resolved measurements can be made. Left: velocity-integrated  $H\alpha$  emission-line maps. The dashed annuli denote the  $\sim 1$  kpc regions from which the  $[\text{N II}]/H\alpha$  ratios were extracted. Right: the  $[\text{N II}]\lambda 6583/H\alpha$  emission-line ratio as a function of physical radius. We overlay the best-fitting linear regression and report the gradients for individual galaxies in Table 1. In all cases the gradients are negative or consistent with zero, as expected for inside-out growth.



**Figure 10.** Metallicity gradients versus redshift for the galaxies in our sample compared to the Milky Way and other low- and high-redshift observations. The Milky Way thin and thick disc measurements are from Gilmore et al. (1995), Bell (1996), Robin et al. (1996) and Edvardsson et al. (1993), the low-redshift star-forming galaxies are from Rupke et al. (2010) and the  $z=1$ – $1.5$  data are from Yuan et al. (2011) and Queyrel et al. (2012). The median abundance gradient for our SHiZELS sample is  $\Delta \log(\text{O}/\text{H})/\Delta R = -0.027 \pm 0.005 \text{ dex kpc}^{-1}$  which is consistent with the thick disc of the Milky Way. We also show the theoretical evolution of the metallicity gradient with redshift from the GIMIC simulation (Crain et al. 2009; McCarthy et al. 2012). The dark grey shows the range of metallicity gradients for all disc galaxies in the simulation in the mass range  $9.5 < \log(M/M_{\odot}) < 11.5$ , whilst the light grey denotes the  $1\sigma$  scatter at each epoch. The GIMIC simulation predicts that the gradients should be steep around  $z \sim 3$  where gas accretion from the IGM is the most efficient, but should flatten by a factor of  $\sim 2$  between  $z=3$  and 0.

report the gradients individually in Table 2. In all cases, the metallicity gradients are negative or consistent with zero, with an average  $\Delta \log(\text{O}/\text{H})/\Delta R = -0.027 \pm 0.005 \text{ dex kpc}^{-1}$ , and similar to those recently found for a sample of  $z \sim 1$  starbursts (Queyrel et al. 2012). This average gradient is steeper, but consistent with the thick disc of the Milky Way,  $\Delta \log(\text{O}/\text{H})/\Delta R = -0.01 \pm 0.02 \text{ dex kpc}^{-1}$  (Edvardsson et al. 1993; Gilmore et al. 1995; Bell 1996; Robin et al. 1996), which has a mass-weighted age of 8–12 Gyr (equivalently, a formation redshift  $z=2$ – $4$ ; Bensby et al. 2007; Ruchti et al. 2011).

In Fig. 10, we compare the metallicity gradients to those from the GIMIC simulation (which include cold gas accretion from the IGM). We calculate the disc phase metallicity in cylindrical coordinates (along the disc) at  $z=0, 1, 2$  and 3 in radial bins of width 1 kpc for all galaxies in the simulation with masses between  $M_{*} = 10^{9.5}$  and  $10^{11} M_{\odot}$ . At  $z \sim 2$ , the model disc galaxies from the GIMIC simulation display negative metallicity gradients which are consistent with our observations. Moreover, between  $z=2$  and 0 the GIMIC simulation predicts that the gradient should flatten by a factor of  $\sim 2$ . In the simulation, this is a consequence of the outer disc enrichment increasing with decreasing redshift (as the gas inflow rates decline and gas is redistributed) progressively flattening the radial gradient within the thick disc. This is qualitatively similar to the numerical models of Dekel et al. (2009a) and where the ‘cold streams’ (which are most prevalent around  $z \sim 2$ ) penetrate the halo and intersect and deposit relatively unenriched gas on to the galaxy discs at  $\sim 15$  kpc (Dekel et al. 2009a; Dekel, Sari & Ceverino 2009b).

## 4 CONCLUSIONS

We have presented AO-assisted, spatially resolved spectroscopy of nine star-forming galaxies at  $z=0.84$ – $2.23$  selected from the United Kingdom Infrared Telescope, wide-field narrow-band, HiZELS survey (Sobral et al. 2012b). Our main results can be summarized as follows.

(i) Using  $\text{H}\alpha$  emission-line dynamics, we find that the ratio of dynamical-to-dispersion support for the sample is  $v_{\text{max}} \sin(i)/\sigma = 0.3$ – $3$ , with a median of  $1.1 \pm 0.3$ , which is consistent with similar measurements for both AO and non-AO studies of star-forming galaxies at this epoch (e.g. Förster Schreiber et al. 2009). At least six galaxies have dynamics that suggest that their ionized gas is in a large, rotating disc (in at least four of these we detect the turnover in their rotation curves). For these galaxies that resemble rotating systems, we model the galaxy velocity field and derive the inclination-corrected, asymptotic velocity.

(ii) We combine our dynamical observations with a number of previous studies of intermediate- and high-redshift galaxies (in particular from Bamford et al. 2005; Weiner et al. 2006; Förster Schreiber et al. 2009; Jones et al. 2010b; Miller et al. 2011, 2012) to investigate the evolution of the Tully–Fisher relation. We show that there is strong evolution in the zero-point of the rest-frame  $B$ -band Tully–Fisher relations with redshift such that at a fixed circular velocity, the  $B$ -band luminosity increases by  $\Delta M_B = 2$  mag up to  $z \sim 2$  (a change in luminosity of a factor of  $\sim 6$ ; e.g. see also Bamford et al. 2005; Weiner et al. 2006; Miller et al. 2011).

(iii) In contrast, the stellar-mass Tully–Fisher relation shows much more modest evolution; for a fixed circular velocity, the average stellar mass has increased by a factor of  $2.0 \pm 0.4$  between  $z=2$  and 0 (e.g. see also Cresci et al. 2009; Miller et al. 2012). The weak evolution in the stellar-mass Tully–Fisher relation (in particular below  $z \sim 1$ ) is due to the fact that individual galaxies evolve along the scaling relations rather than due to weak evolution in the galaxies themselves (e.g. Portinari & Sommer-Larsen 2007; Brooks et al. 2011; Dutton et al. 2011), and indicates that the baryon conversion efficiency,  $\eta = (M_{*}/M_{200})/(\Omega_b/\Omega_0)$ , is fixed with redshift. The observations also suggest that the scatter in high-redshift Tully–Fisher relation is comparable to that predicted by the models, suggesting that the samples may now be sufficiently large (with rotation curves well enough sampled) that the scatter is intrinsic.

(iv) Combining the rest-frame  $B$ -band and stellar-mass Tully–Fisher relations we show that the mass-to-light ratio of star-forming galaxies evolves strong with redshift, decreasing by  $\Delta M/L_B = 1.1 \pm 0.2$  between  $z=0$  and 1, but then ceases to evolve further above  $z=1$ . This change in mass-to-light ratio in the  $B$  band is a factor of  $\Delta(M/L_B)/(M/L_B)_{z=0} \sim 3.5$ . We show that the evolution in the Tully–Fisher relations and mass-to-light ratio is in line with both cosmologically based hydrodynamic simulations and semi-analytic models of galaxy formation.

(v) Using the  $\text{H}\alpha$  half-light radius and circular velocity, we also find that the SHiZELS galaxies are a factor of  $1.5 \pm 0.3$  smaller for fixed circular velocity than for discs at  $z=0$ . If the  $z \sim 2$  and  $z=0$  discs are linked in a simple evolutionary scenario then high-redshift discs must acquire specific angular momentum, either by removing material with low specific angular momentum (e.g. through outflows), or through acquisition of angular momentum from accreted gas at late times.

(vi) Finally, we measure the spatially resolved  $[\text{N II}]/\text{H}\alpha$  ratio to measure the metallicity gradients. In all cases, the metallicity gradients are negative or consistent with zero, with an average  $\Delta \log(\text{O}/\text{H})/\Delta R = -0.027 \pm 0.005 \text{ dex kpc}^{-1}$ , which is consistent

with that seen in the thick disc of the Milky Way. We show that these metallicity gradients are comparable to those predicted for the gas discs of star-forming galaxies in the cosmologically based hydrodynamic simulations. In these models, the inner disc undergoes initial rapid collapse and star formation with gas accretion (either from the halo and/or IGM) depositing relatively unenriched material at the outer disc, causing negative abundance gradients. At lower redshift (when gas accretion from the IGM is less efficient) the abundance gradients flatten as the outer disc becomes enriched by star formation (and/or the redistribution of gas from the inner disc).

Overall, we demonstrate that well-sampled, dynamical measurements of high-redshift star-forming galaxies can constrain the rotation curves, measure the evolution of the basic disc scaling relations and their radial abundance gradients. We show that the current observational samples with well-resolved data are now approaching sufficiently large samples that it is possible to refine or refute models of disc galaxy formation.

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