

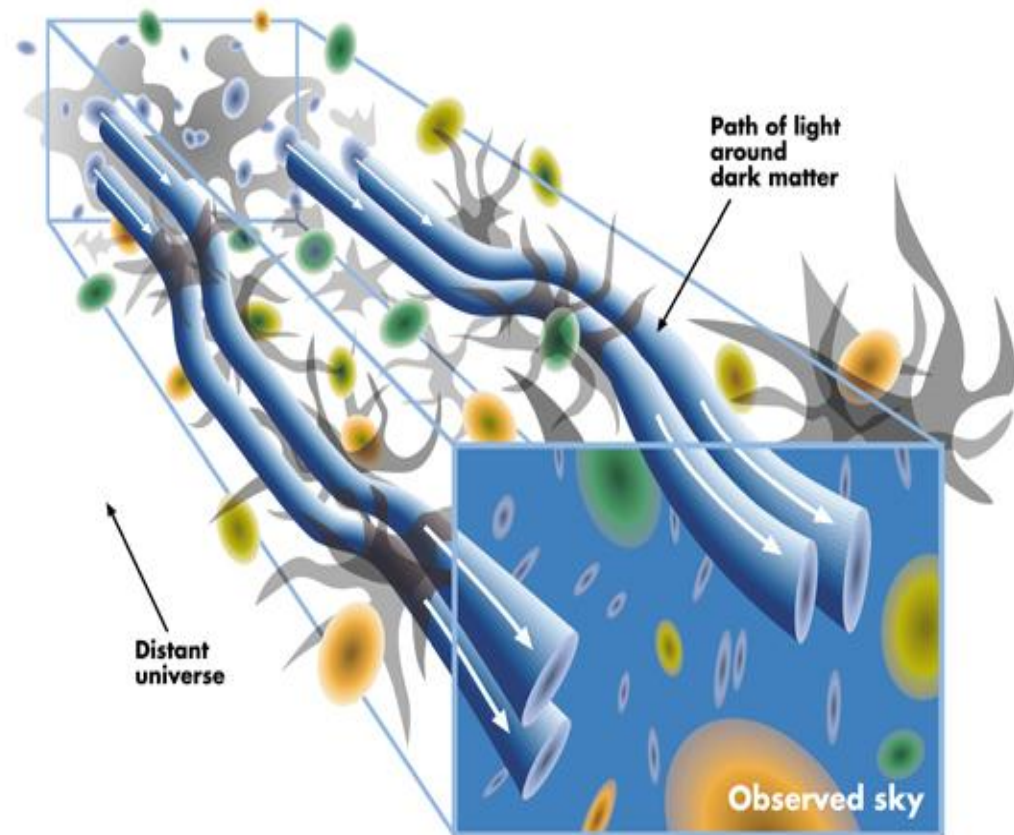
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# COSMIC SHEAR TOMOGRAPHY AND EFFICIENT DATA COMPRESSION USING COSEBIS

# COSMIC SHEAR

- ✘ Structures distort light in its path
- ✘ The shape of the galaxies are the first observable
- ✘ Studying cosmic shear, reveals the cosmological parameters



# The motivation: Future Surveys



- ✘ Better precision
- ✘ Larger fields of view
- ✘ Deeper Images
- ✘ More accurate redshifts

## 2 POINT CORRELATION FUNCTIONS (2PCFS)

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- ✗ On average shear is zero on the sky
- ✗ We need to go to two point statistics and higher
- ✗ The 2PCFs are

$$\xi_{\pm}(\theta) = \langle \gamma_t \gamma_t \rangle (\theta) \pm \langle \gamma_{\times} \gamma_{\times} \rangle (\theta)$$

# E-/B-MODES

- ✗ The E-modes can be generated from lensing  
(The curl free modes)
- ✗ The B-modes have non-lensing origin  
(The divergence free modes)

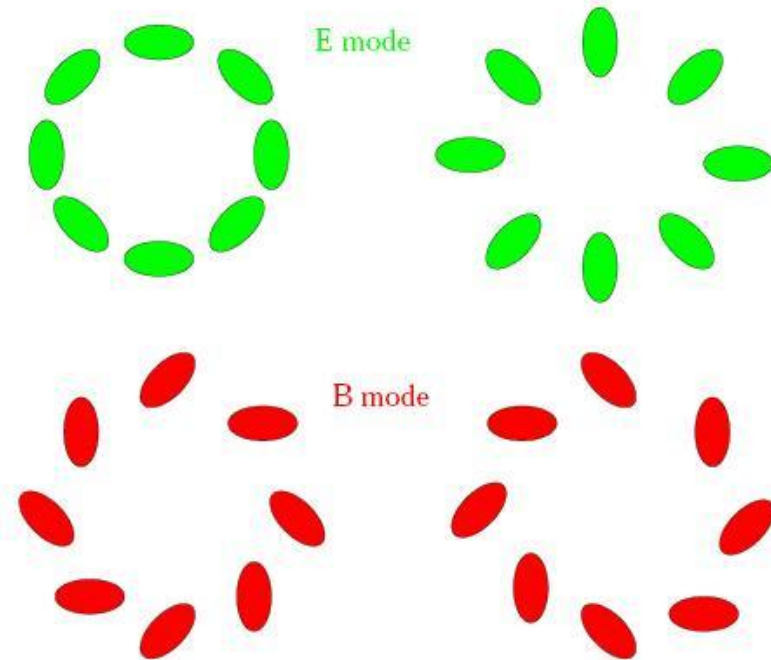
$$\xi_+(\theta) = \int_0^\infty \frac{d\ell \ell}{2\pi} J_0(\ell\theta) [P_E(\ell) + P_B(\ell)]$$

$$\xi_-(\theta) = \int_0^\infty \frac{d\ell \ell}{2\pi} J_4(\ell\theta) [P_E(\ell) - P_B(\ell)]$$

$$E = \int_0^\infty d\vartheta \vartheta [\xi_+(\vartheta)T_+(\vartheta) + \xi_-(\vartheta)T_-(\vartheta)]$$

$$B = \int_0^\infty d\vartheta \vartheta [\xi_+(\vartheta)T_+(\vartheta) - \xi_-(\vartheta)T_-(\vartheta)]$$

$$\int_0^\infty d\vartheta \vartheta T_+(\vartheta) J_0(\ell\vartheta) = \int_0^\infty d\vartheta \vartheta T_-(\vartheta) J_4(\ell\vartheta)$$



## APERTURE MASS DISPERSION

- × Can be defined as E and B mode estimators
- × The aperture has a finite support inside a circle
- × The correlations must be measured to very small separations

## RING STATISTICS

- × The Ring Statistics filters are defined on a finite interval
- × The Ring Statistics cleanly separates E- and B-modes
- × The signal is low
- × The filter functions are not mathematically beautiful

# OLD METHODS FOR E-/B-SEPARATION

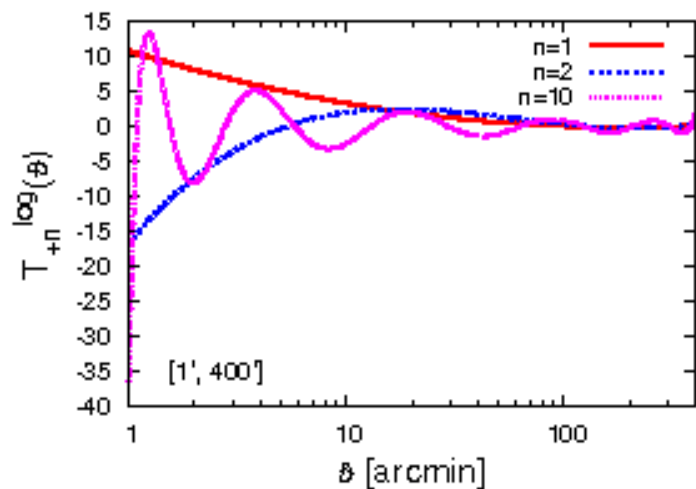
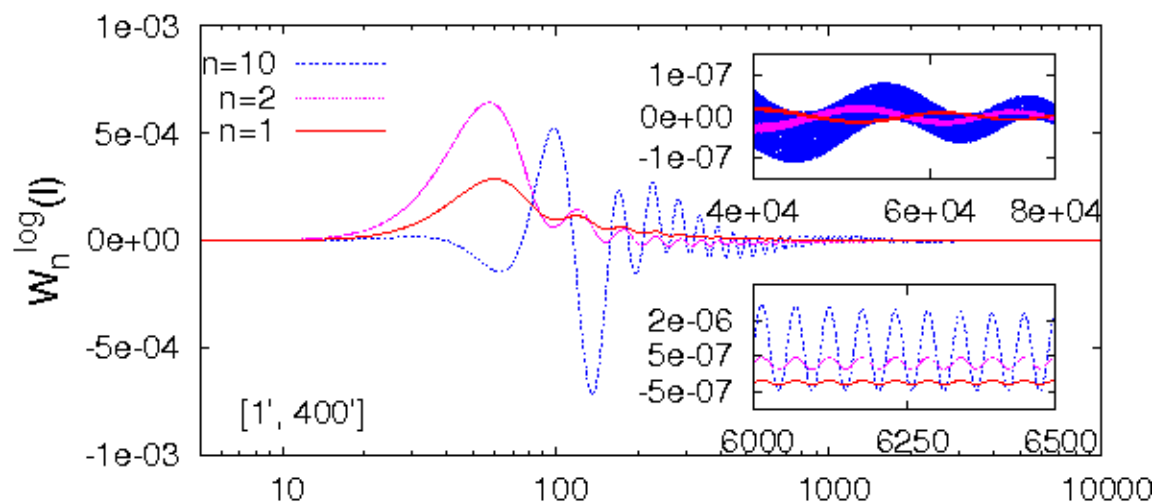
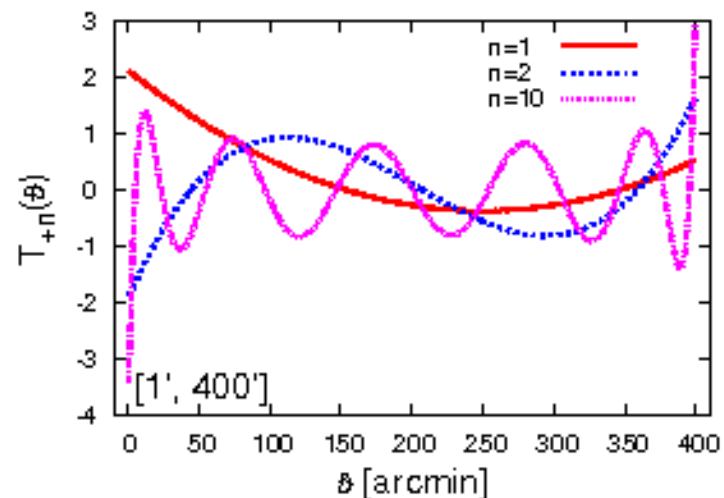
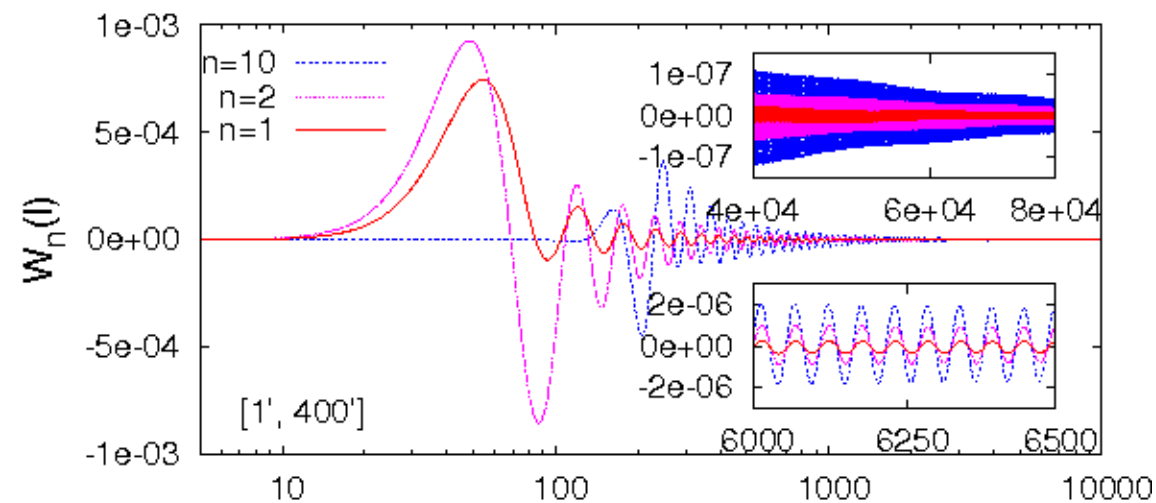
# THE COSEBIS

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- ✘ Complete Orthogonal Sets of E-/B-Integrals
- ✘ They are constructed by complete sets of bases for the filter function space
- ✘ The linear and logarithmic COSEBIs filters are polynomials
- ✘ The linear COSEBIs filter functions are the Legendre Polynomials of the 4<sup>th</sup> order and higher + two other lower order polynomials.
- ✘ The logarithmic COSEBIs are polynomials in  $\ln(\theta)$
- ✘ A finite number of them is essentially sufficient to get the full information available

# FILTER FUNCTIONS

$$W_n(\ell) = \int_{\vartheta_{\min}}^{\vartheta_{\max}} d\vartheta \vartheta T_{+n}(\vartheta) J_0(\ell\vartheta)$$





# STATISTICAL METHOD: FISHER ANALYSIS

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- ✘ Fisher matrix is related to the log-likelihood function
- ✘ Quantifies the shape and size of the confidence regions

$$F_{ij} = \langle \mathcal{L}_{,ij} \rangle = \frac{1}{2} \text{Tr}[C^{-1} M_{ij}]$$

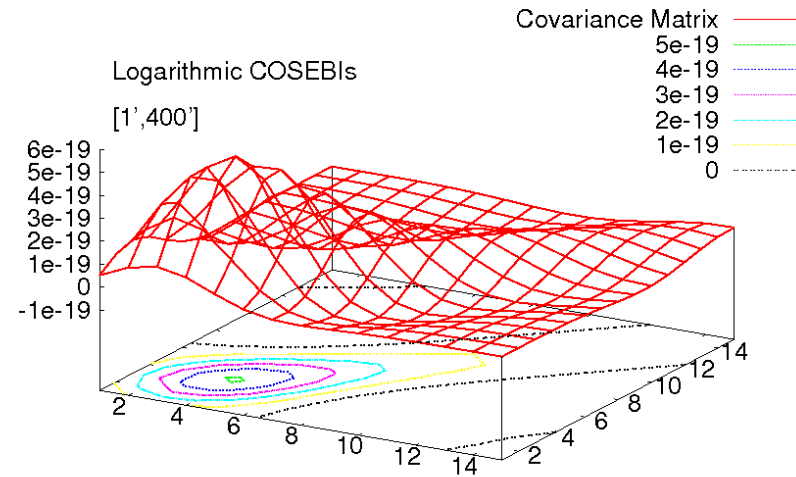
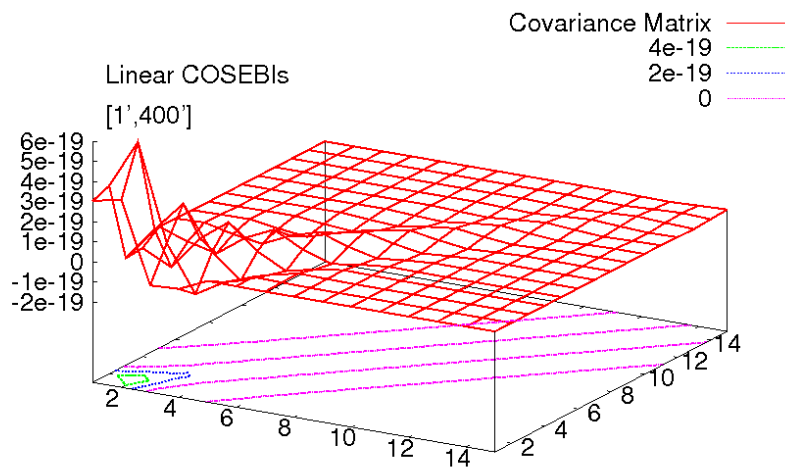
$$M_{ij} = \mathbf{E}_{,i} \mathbf{E}_{,j}^T + \mathbf{E}_{,j} \mathbf{E}_{,i}^T$$

- ✘ Our figure-of-merit is a measure of the geometric mean of the standard deviations of the parameters

$$f = \left( \frac{1}{\sqrt{\det F}} \right)^{1/n_p}$$

# COVARIANCE

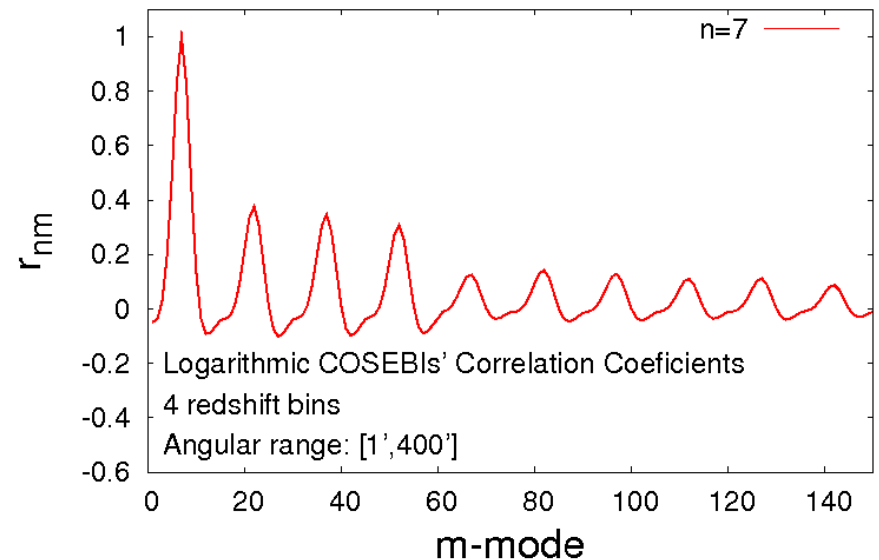
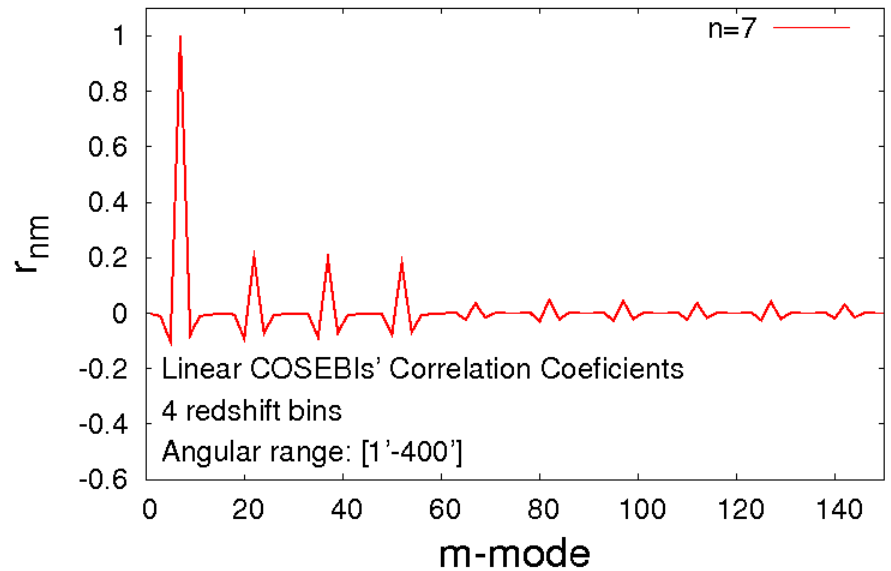
✗ The COSEBs covariance is a band like matrix



$$C_{mn}^X = \frac{1}{\pi A} \int_0^\infty dl \ell W_m(\ell) W_n(\ell) \left( P_X(\ell) + \frac{\sigma_\epsilon^2}{2\bar{n}} \right)^2$$

# CORRELATION COEFFICIENTS

- ✗ Correlation coefficients are the normalized covariance elements
- ✗ Each pick corresponds to correlations between the same pair of COSEBIs modes
- ✗ 4 redshift bins and 15 COSEBIs modes are used here



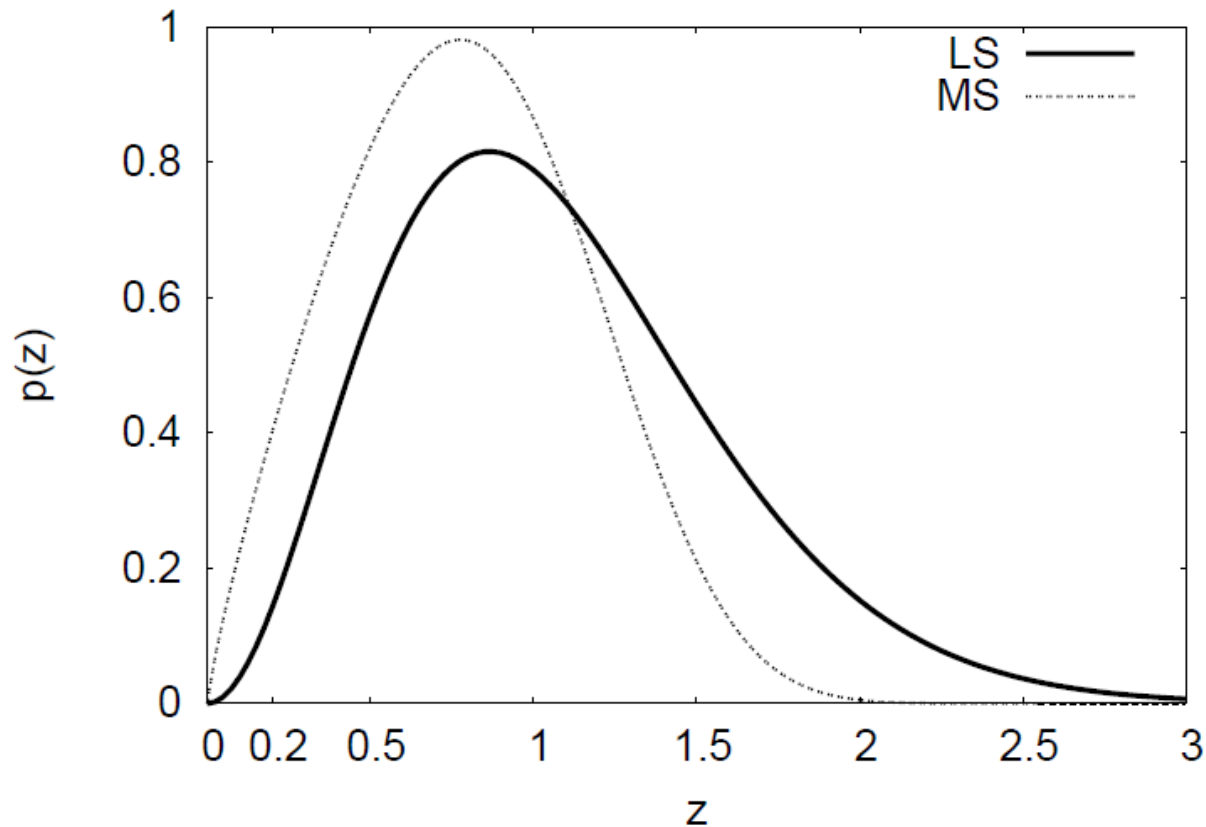
# COSMOLOGICAL MODEL

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- ✗  $\Lambda$ CDM model:
- ✗ Dark energy with an equation of state parameter  $w_0$
- ✗ And cold dark matter
- ✗ 7 free parameters in total with fiducial values of

$\sigma_8$	$\Omega_m$	$\Omega_\Lambda$	$w_0$	$n_s$	$h$	$\Omega_b$
0.8	0.27	0.73	-1.0	0.97	0.70	0.045

# THE 2 SURVEYS: MEDIUM AND LARGE



	z-distribution parameters					survey parameters		
	$\alpha$	$\beta$	$z_0$	$z_{\min}$	$z_{\max}$	$A$	$\sigma_\epsilon$	$\bar{n}$
MS	0.836	3.425	1.171	0.2	1.5	170	0.42	13.3
LS	2.0	1.5	0.71	0.0	2.0	20000	0.3	35

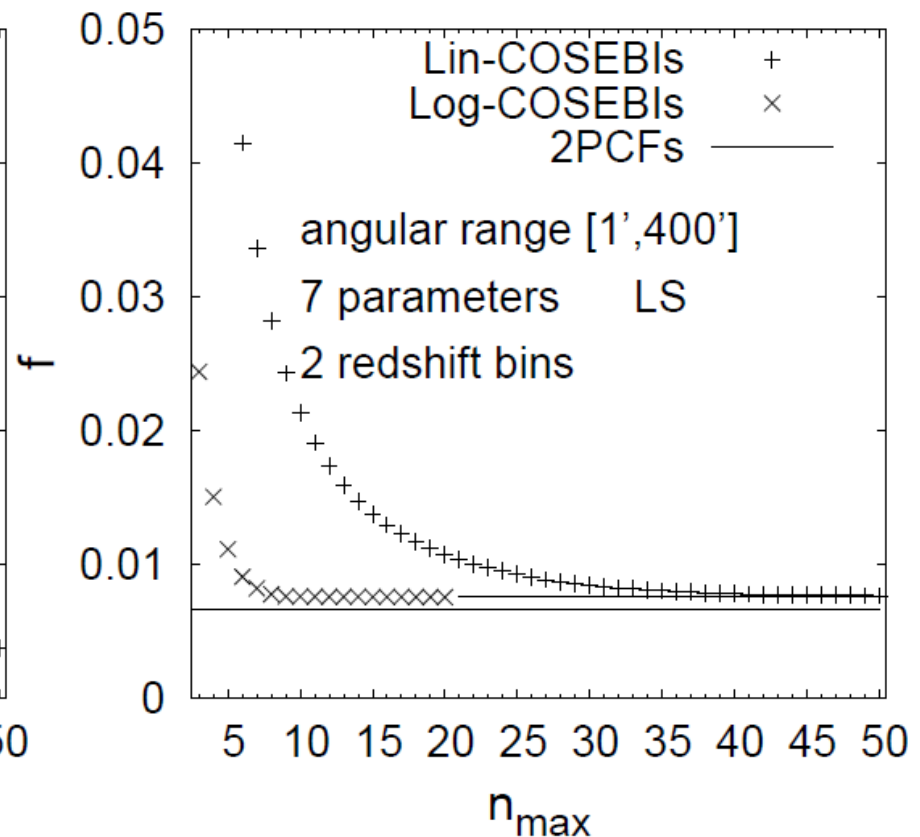
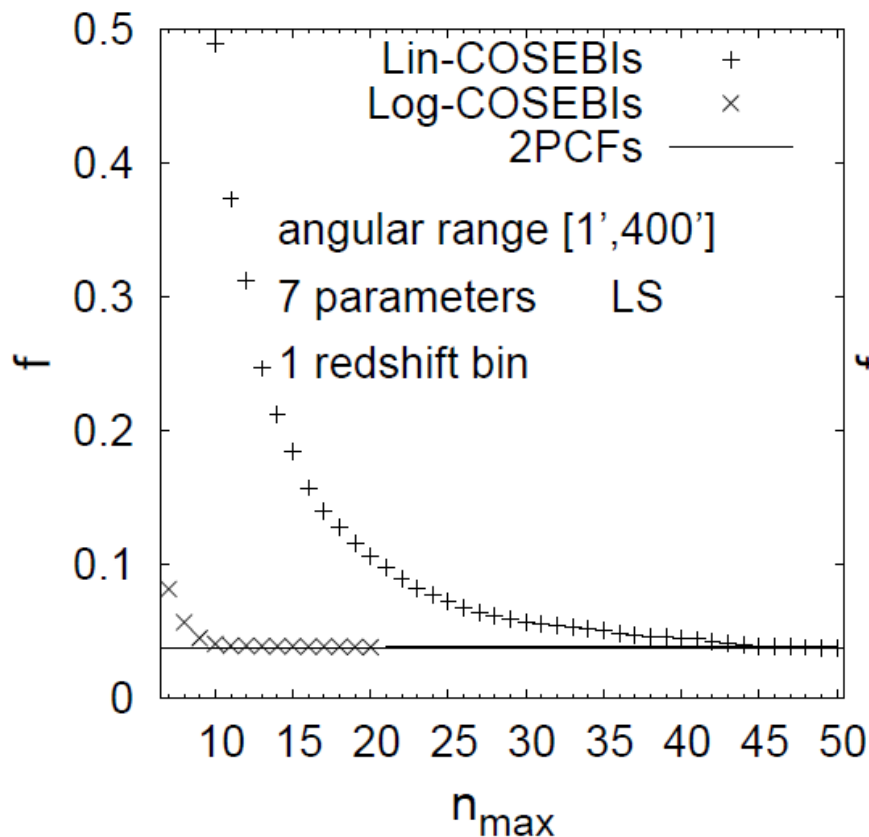
# OTHER CRITERIA

- ✘ Prior: The parameter covariance of WMAP7 from a Population Monte Carlo (PMC) run by Martin Kilbinger is our prior
- ✘ Angular ranges:  $[1':20']$ ,  $[20':400']$ ,  $[1':400']$
- ✘ Handling the parameters: fixing or marginalizing.



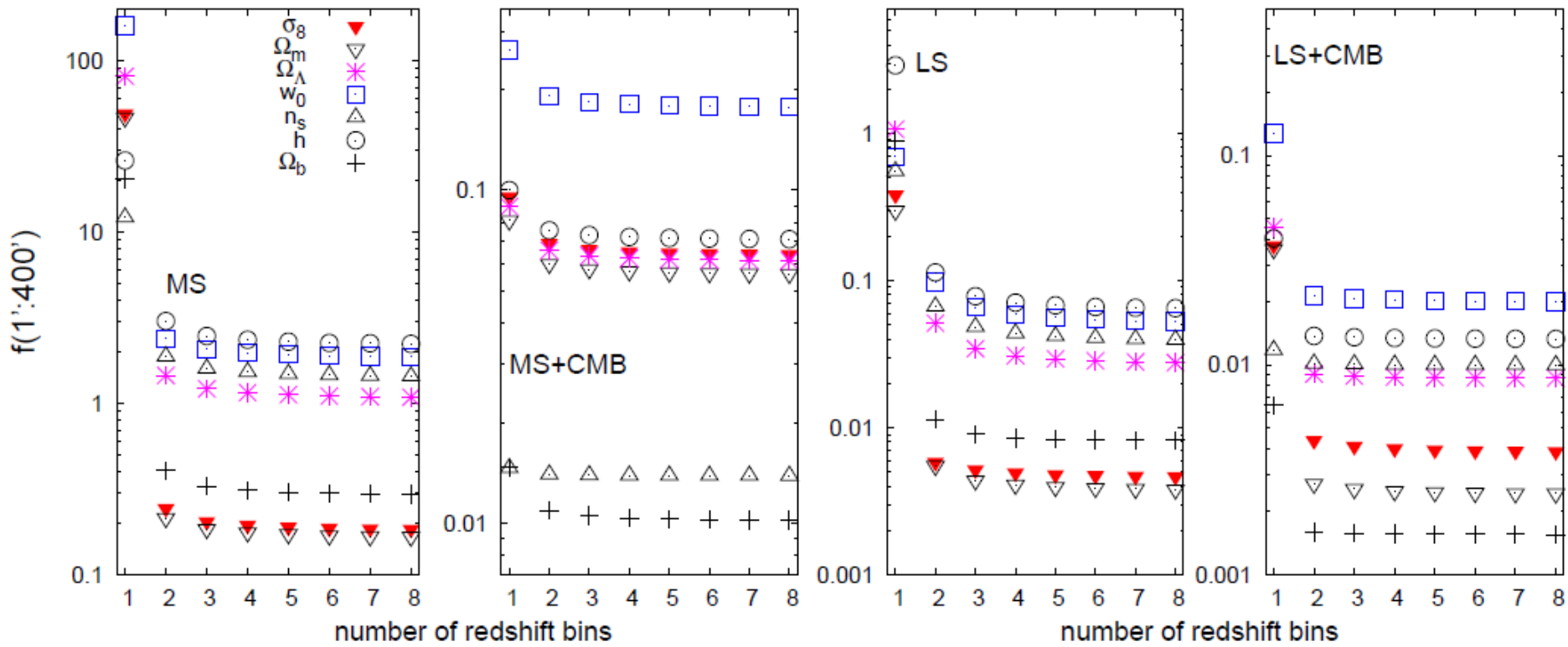
# INFORMATION LEVEL VS. NUMBER OF COSEBIS MODES

- ✗ Fewer Log-COSEBIs are needed to reach a saturated value compared to linear ones
- ✗ The Lin- and Log-COSEBIs reach the same saturated value
- ✗ The 2PCFs value is always lower



# TOMOGRAPHY

- ✗ 3-4 redshift bins are enough to capture all the information
- ✗ Priors do not have a big effect on LS for fixed parameters
- ✗ Priors flatten the curves and tighten the constraints





# CONCLUSIONS

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- ✗ COSEBIs is a very compact way of cosmic shear analysis
- ✗ A relatively small number of COSEBIs modes is enough to reach the full information level
- ✗ Adding tomography greatly increases the information about the parameters up to a certain number of redshift bins
- ✗ 7 parameters can be constrained simultaneously with the data from the large surveys of the future
- ✗ Most of the cosmic shear information is in small scales
- ✗ There is some independent information in large scales
- ✗ LS constraints are tighter compared to MS
- ✗ LS needs more modes to converge
- ✗ Adding priors helps further tighten the constraints
- ✗ Each parameter behaves differently

$$\langle \hat{\kappa}(\ell) \hat{\kappa}^*(\ell') \rangle = (2\pi)^2 \delta_D(\ell - \ell') P_\kappa(\ell)$$

$$\kappa = \kappa^E + i\kappa^B$$

$$\langle \hat{\kappa}^E(\ell) \hat{\kappa}^{E*}(\ell') \rangle = (2\pi)^2 \delta_D(\ell - \ell') P_E(\ell)$$

$$\langle \hat{\kappa}^B(\ell) \hat{\kappa}^{B*}(\ell') \rangle = (2\pi)^2 \delta_D(\ell - \ell') P_B(\ell)$$

$$\langle \hat{\kappa}^E(\ell) \hat{\kappa}^{B*}(\ell') \rangle = (2\pi)^2 \delta_D(\ell - \ell') P_{EB}(\ell)$$

# CONSTRUCTING PRACTICAL STATISTICS II

## THE FILTER FUNCTIONS DEFINED ON FINITE INTERVALS

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$$\int_0^{\infty} d\vartheta \vartheta T_+(\vartheta) J_0(l\vartheta) = \int_0^{\infty} d\vartheta \vartheta T_-(\vartheta) J_4(l\vartheta)$$

$$T_+(\vartheta) = T_-(\vartheta) + \int_{\vartheta}^{\infty} d\theta \theta T_-(\theta) \left( \frac{4}{\theta^2} - \frac{12\vartheta^2}{\theta^4} \right)$$

$$T_-(\vartheta) = T_+(\vartheta) + \int_0^{\vartheta} d\theta \theta T_+(\theta) \left( \frac{4}{\vartheta^2} - \frac{12\theta^2}{\vartheta^4} \right)$$

- ✘ There are infinite number of functions satisfying these conditions

$$\int_{\vartheta_{\min}}^{\vartheta_{\max}} \frac{d\vartheta}{\vartheta} T_-(\vartheta) = 0 = \int_{\vartheta_{\min}}^{\vartheta_{\max}} \frac{d\vartheta}{\vartheta^3} T_-(\vartheta)$$

$$\int_{\vartheta_{\min}}^{\vartheta_{\max}} d\vartheta \vartheta T_+(\vartheta) = 0 = \int_{\vartheta_{\min}}^{\vartheta_{\max}} d\vartheta \vartheta^3 T_+(\vartheta)$$

# CONSTRUCTING PRACTICAL STATISTICS I

- ✗ Any other estimator should be constructed from the correlations.
- ✗ The general form:

$$E = \int_0^{\infty} d\vartheta \vartheta [\xi_+(\vartheta)T_+(\vartheta) + \xi_-(\vartheta)T_-(\vartheta)]$$

$$B = \int_0^{\infty} d\vartheta \vartheta [\xi_+(\vartheta)T_+(\vartheta) - \xi_-(\vartheta)T_-(\vartheta)]$$

$$\xi_+(\vartheta) = \int_0^{\infty} \frac{d\ell \ell}{2\pi} J_0(\ell\vartheta) [P_E(\ell) + P_B(\ell)]$$

$$\xi_-(\vartheta) = \int_0^{\infty} \frac{d\ell \ell}{2\pi} J_4(\ell\vartheta) [P_E(\ell) - P_B(\ell)]$$

$$\int_0^{\infty} d\vartheta \vartheta T_+(\vartheta) J_0(\ell\vartheta) = \int_0^{\infty} d\vartheta \vartheta T_-(\vartheta) J_4(\ell\vartheta)$$

# THE MATHEMATICAL FORM

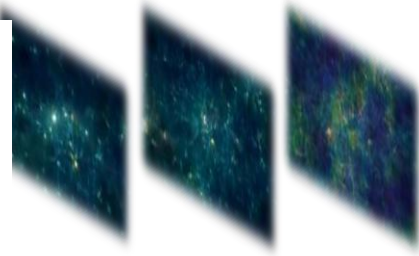
$$E = \int_0^\infty d\vartheta \vartheta [\xi_+(\vartheta)T_+(\vartheta) + \xi_-(\vartheta)T_-(\vartheta)]$$

$$E_n^{ij} = \int_0^\infty \frac{d\ell}{2\pi} \ell P_E^{ij}(\ell) W_n(\ell)$$

$$W_n(\ell) = \int_{\vartheta_{\min}}^{\vartheta_{\max}} d\vartheta \vartheta T_{+n}(\vartheta) J_0(\ell\vartheta)$$

$$P_E^{ij}(\ell) = \frac{9H_0^4 \Omega_m^2}{4c^4} \int_0^{\chi_h} d\chi \frac{g^j(\chi)g^i(\chi)}{a^2(\chi)} P_\delta\left(\frac{\ell}{f_K(\chi)}, \chi\right)$$

$$g^i(\chi) = \int_\chi^{\chi_h} d\chi' p_\chi^i(\chi') \frac{f_K(\chi' - \chi)}{f_K(\chi')}$$



✗  $i=j$   Auto-correlation     $i \neq j$   Cross-correlation

**THIS IS THE TITLE**

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